



DICE
ANALYTICS

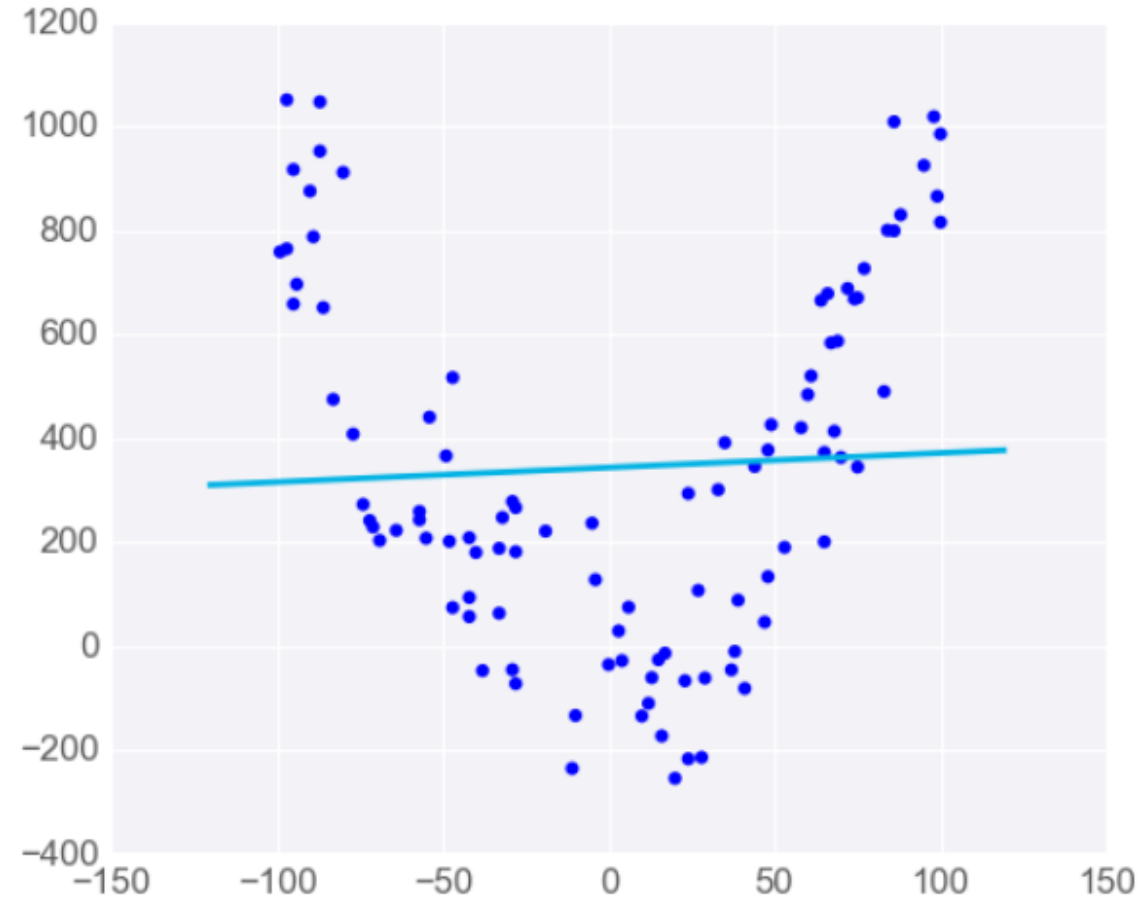
DATA SCIENCE & MACHINE LEARNING COURSE

<https://www.facebook.com/diceanalytics/>
<https://pk.linkedin.com/company/diceanalytics>

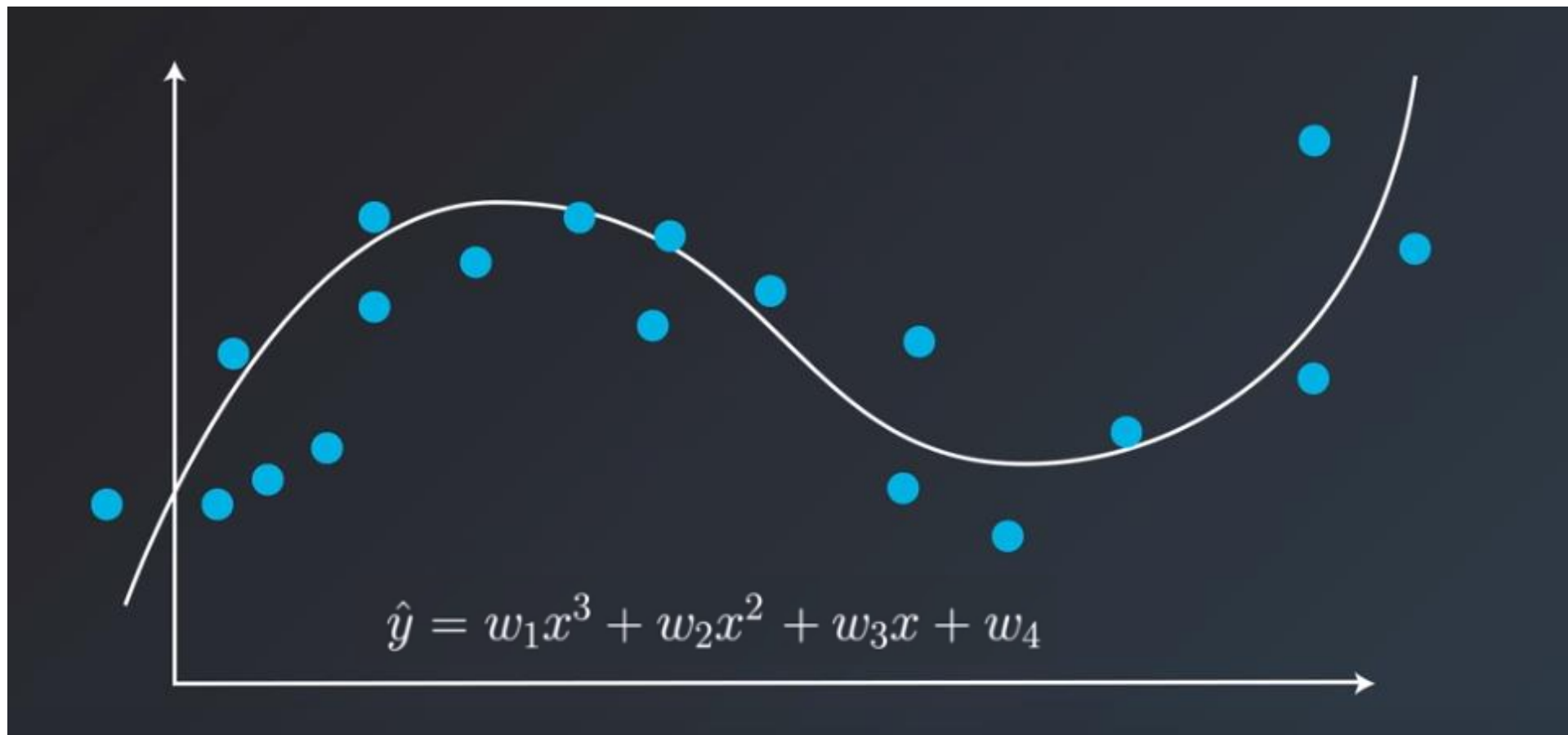
Regression

Polynomial Regression

Linear Regression Works Best When the Data is Linear



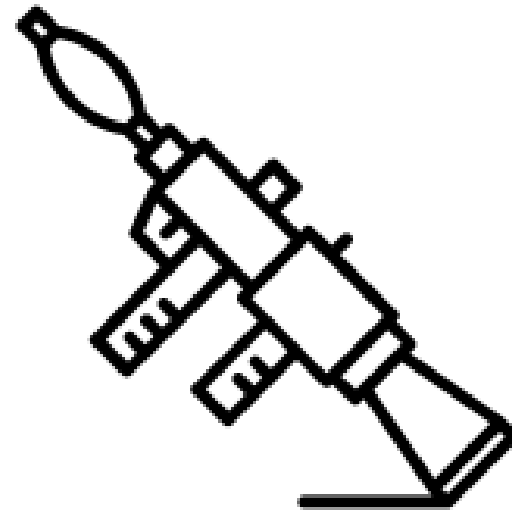
Polynomial Regression



Model Selection



Simple Problem



Complex Solution

Model Selection

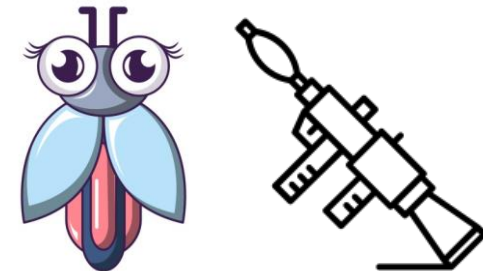
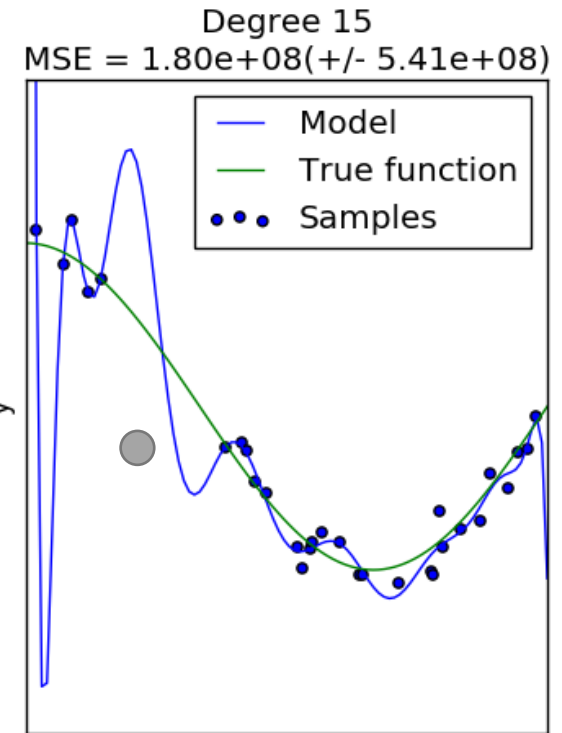
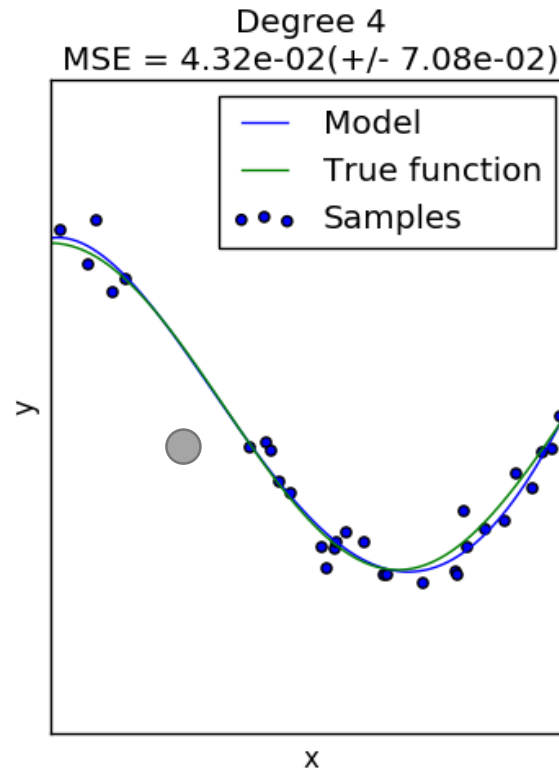
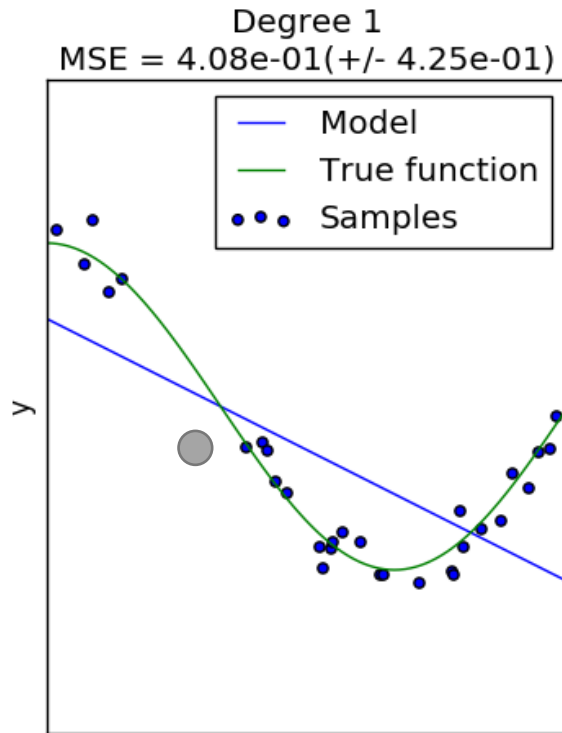


Complex Problem

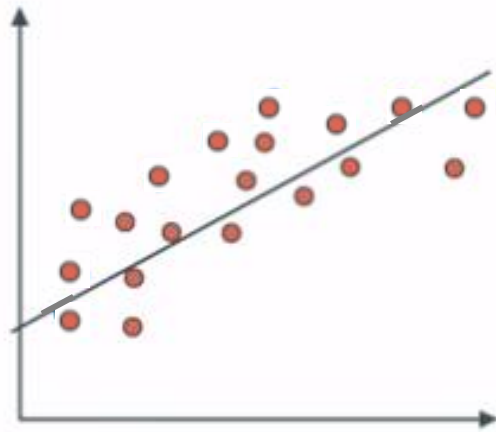


Simple Solution

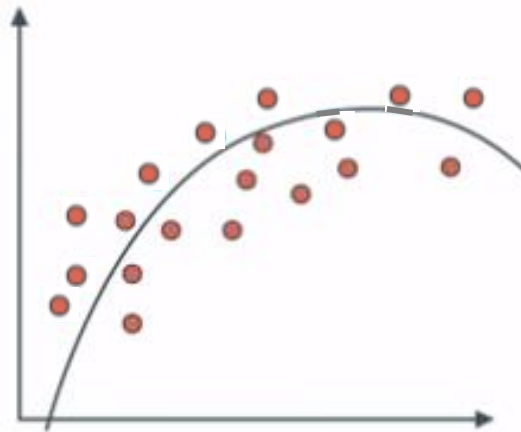
Under-fitting & Over-fitting



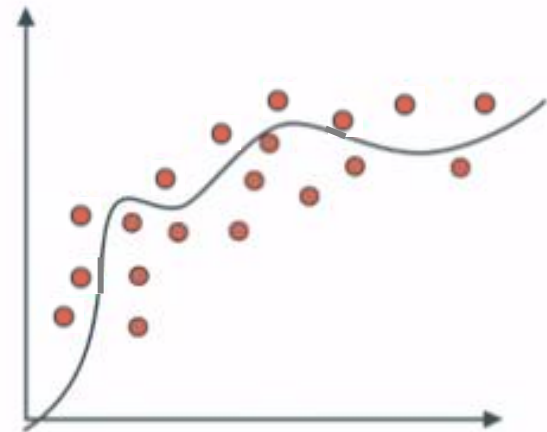
Model Complexity



HIGH BIAS
Degree = 1

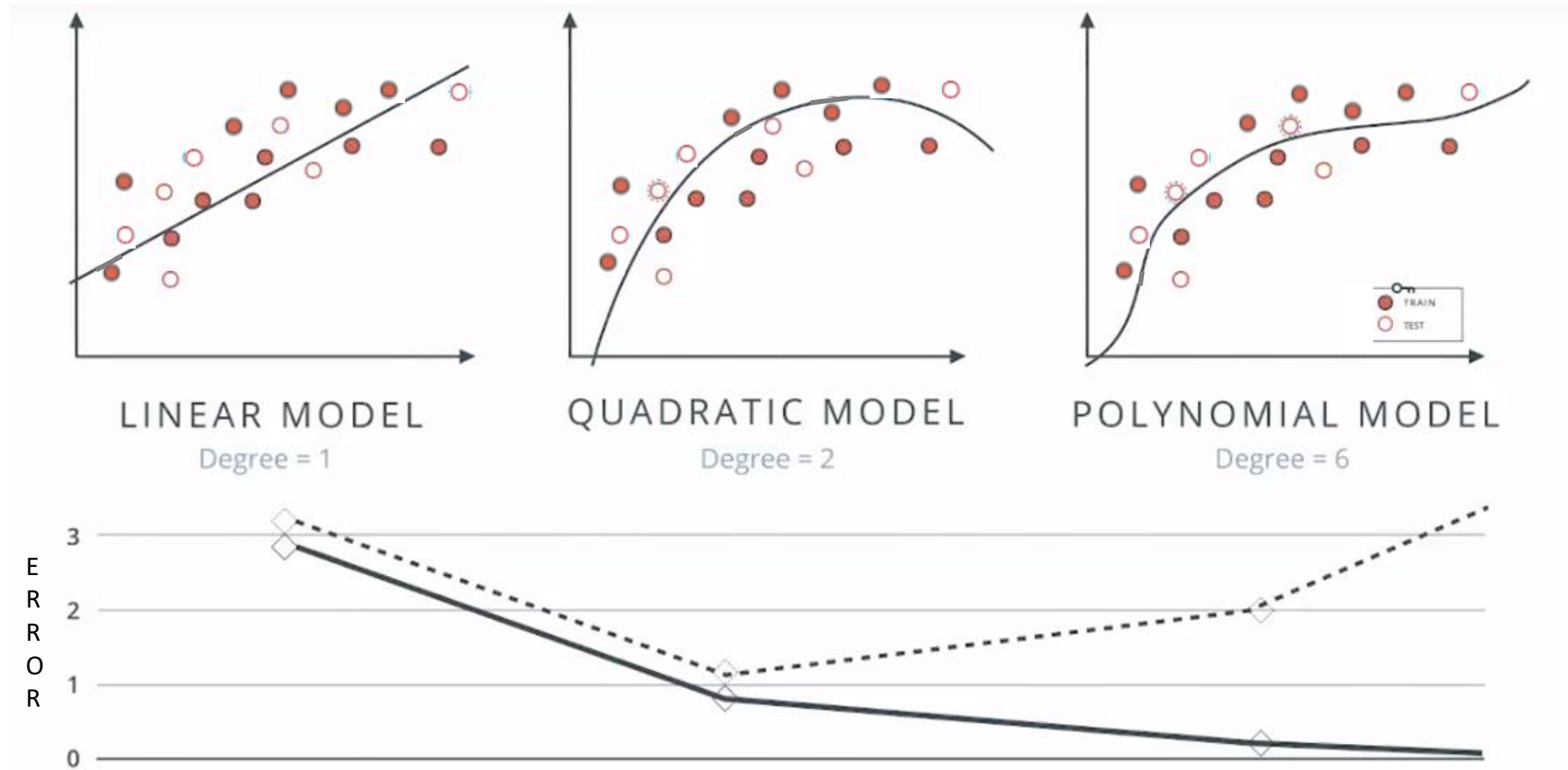


POLYNOMIAL
Degree = 2

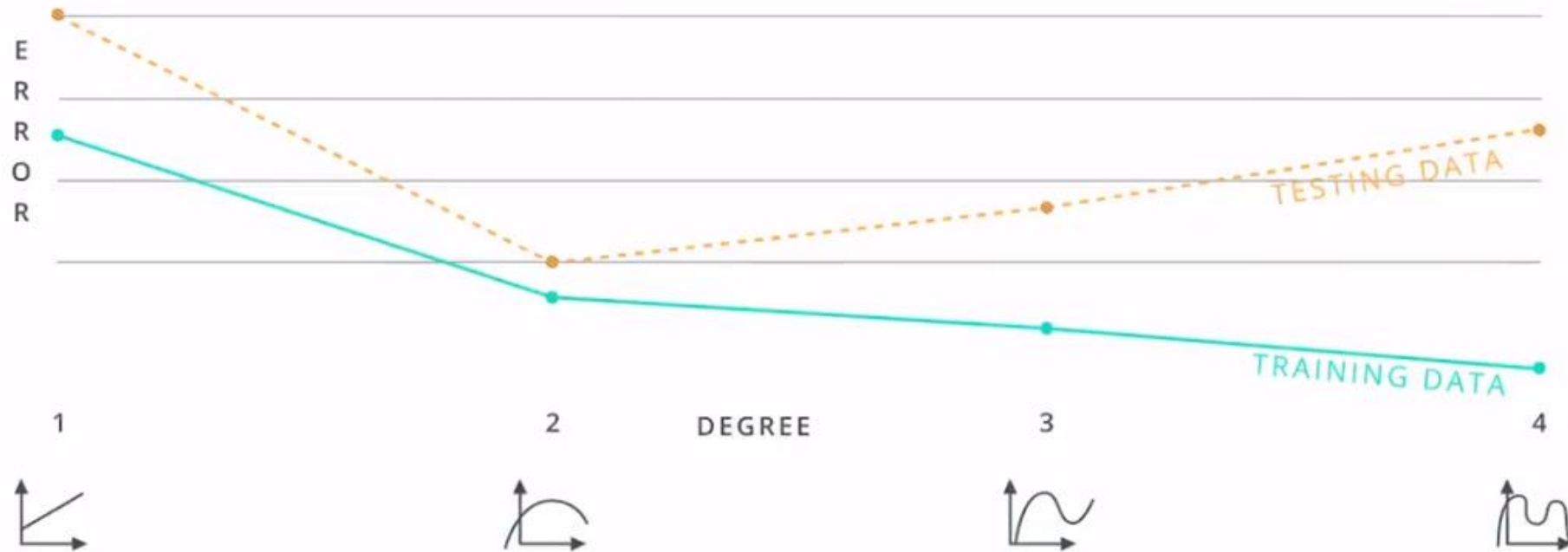


HIGH VARIANCE
Degree = 6

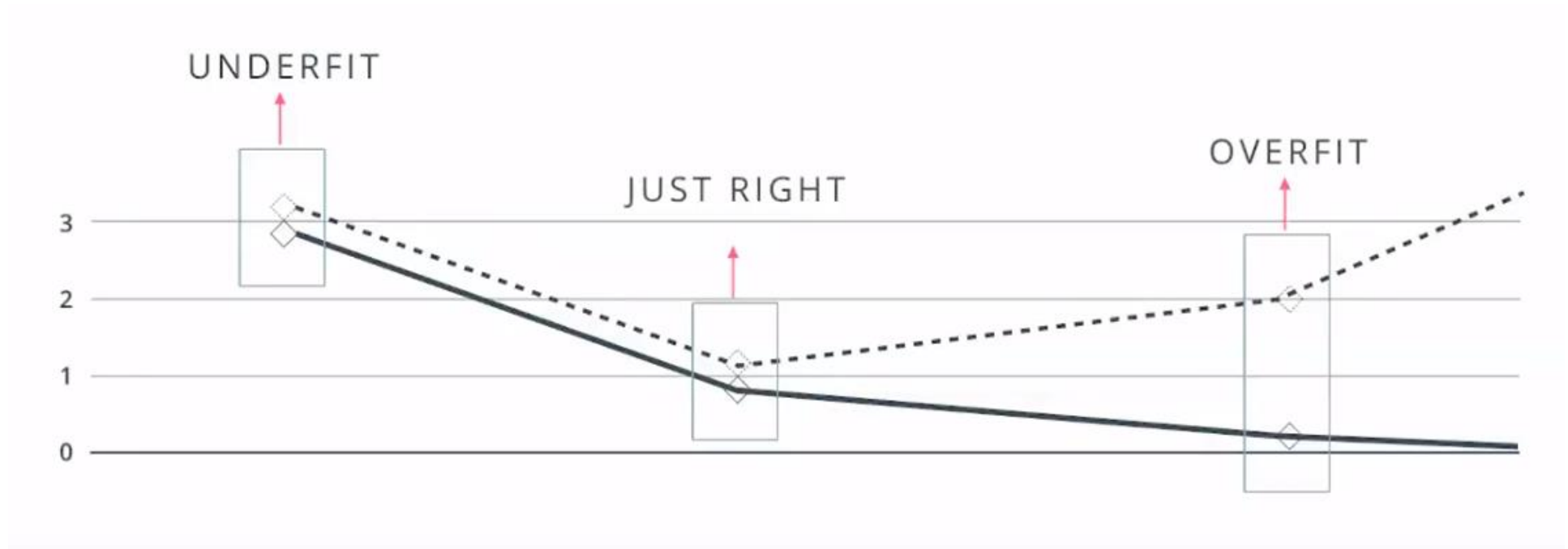
Model Complexity



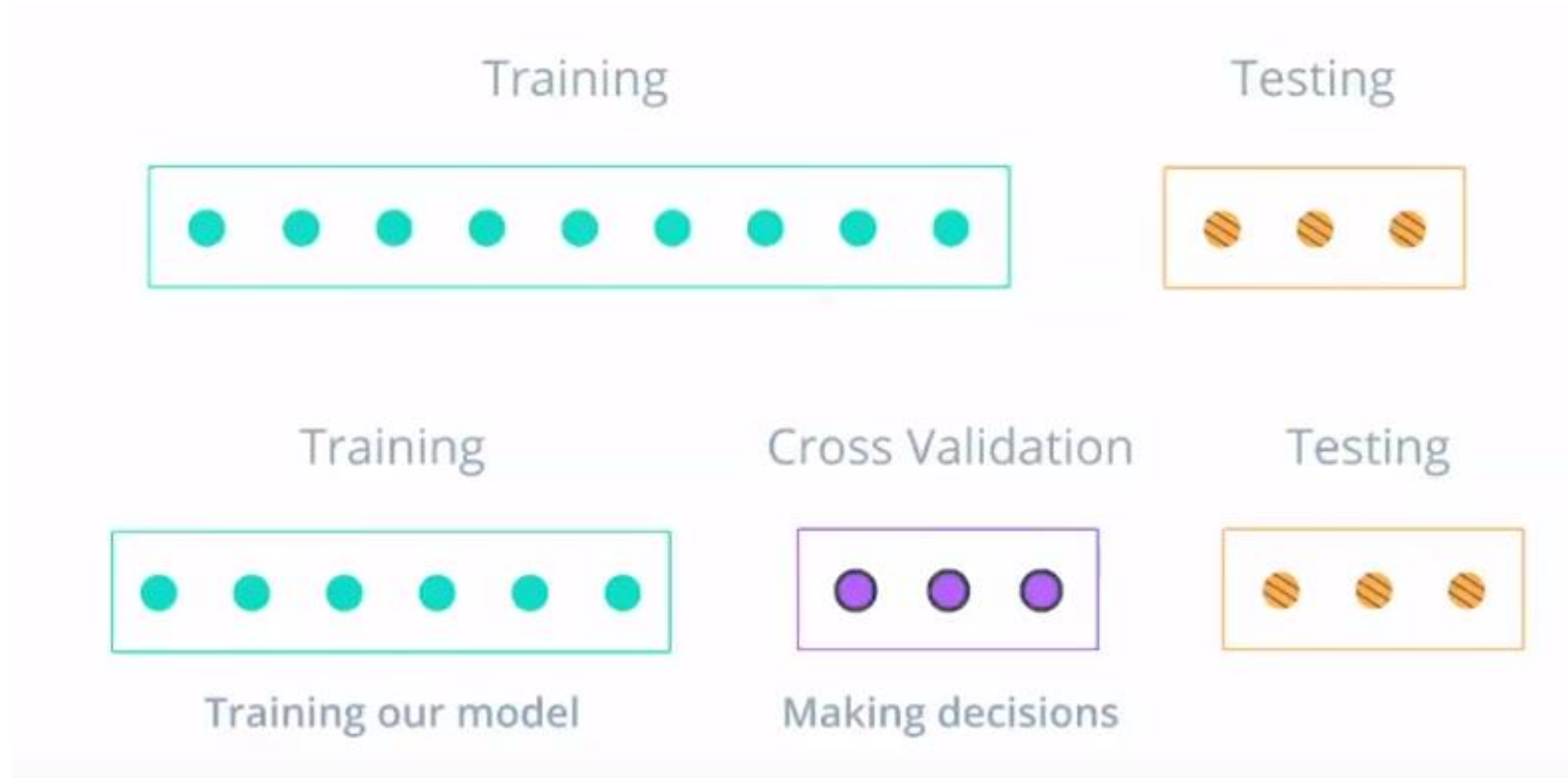
Model Complexity



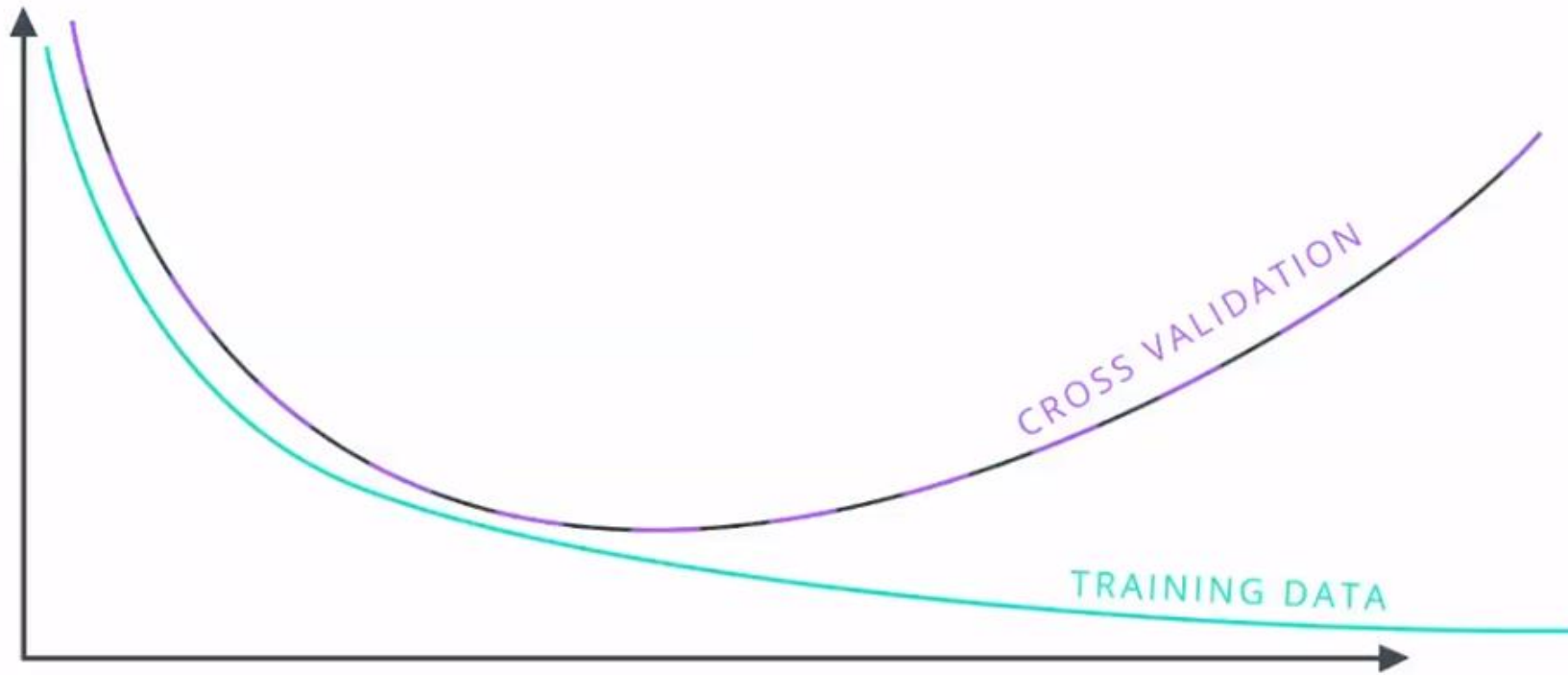
Model Complexity



Model Complexity



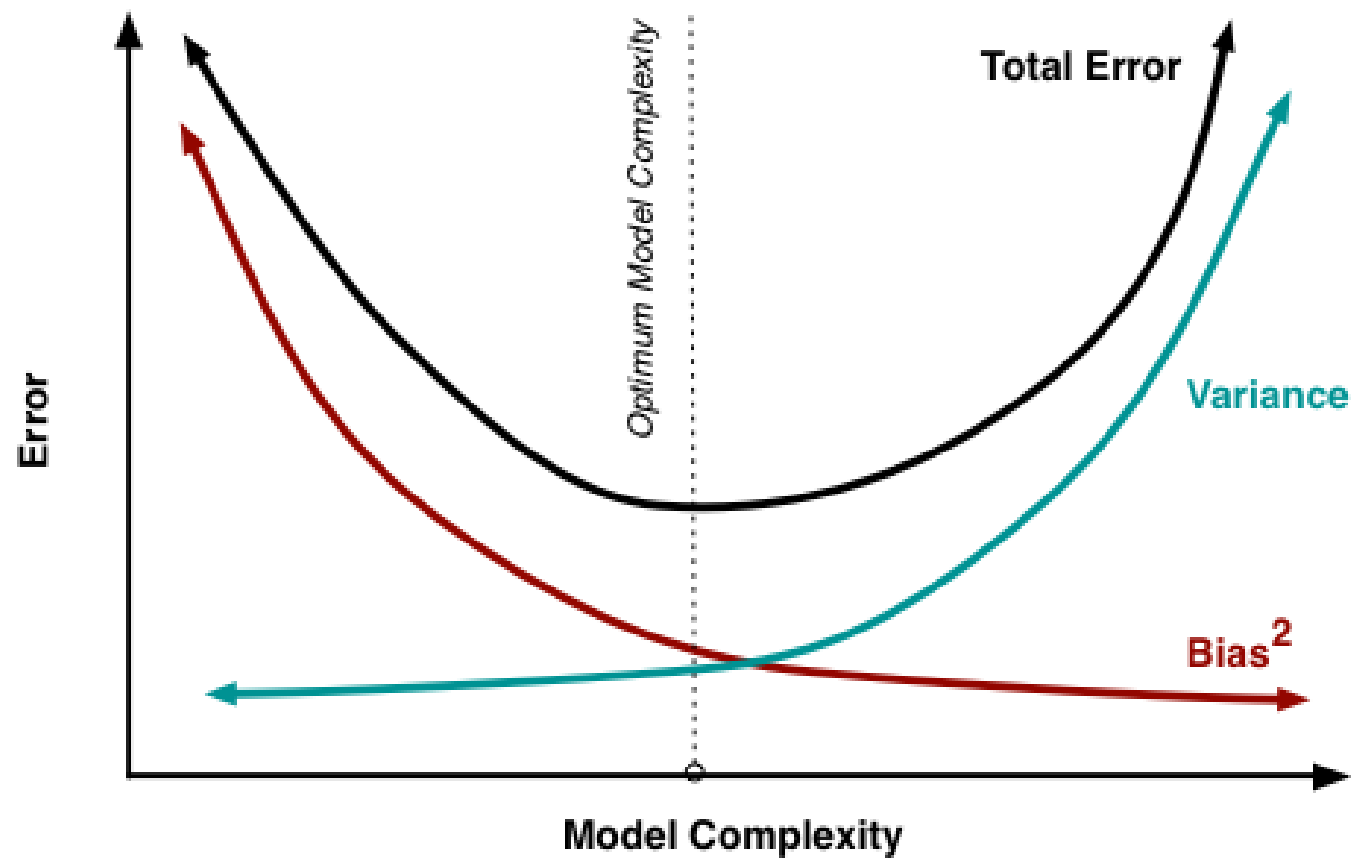
Model Complexity



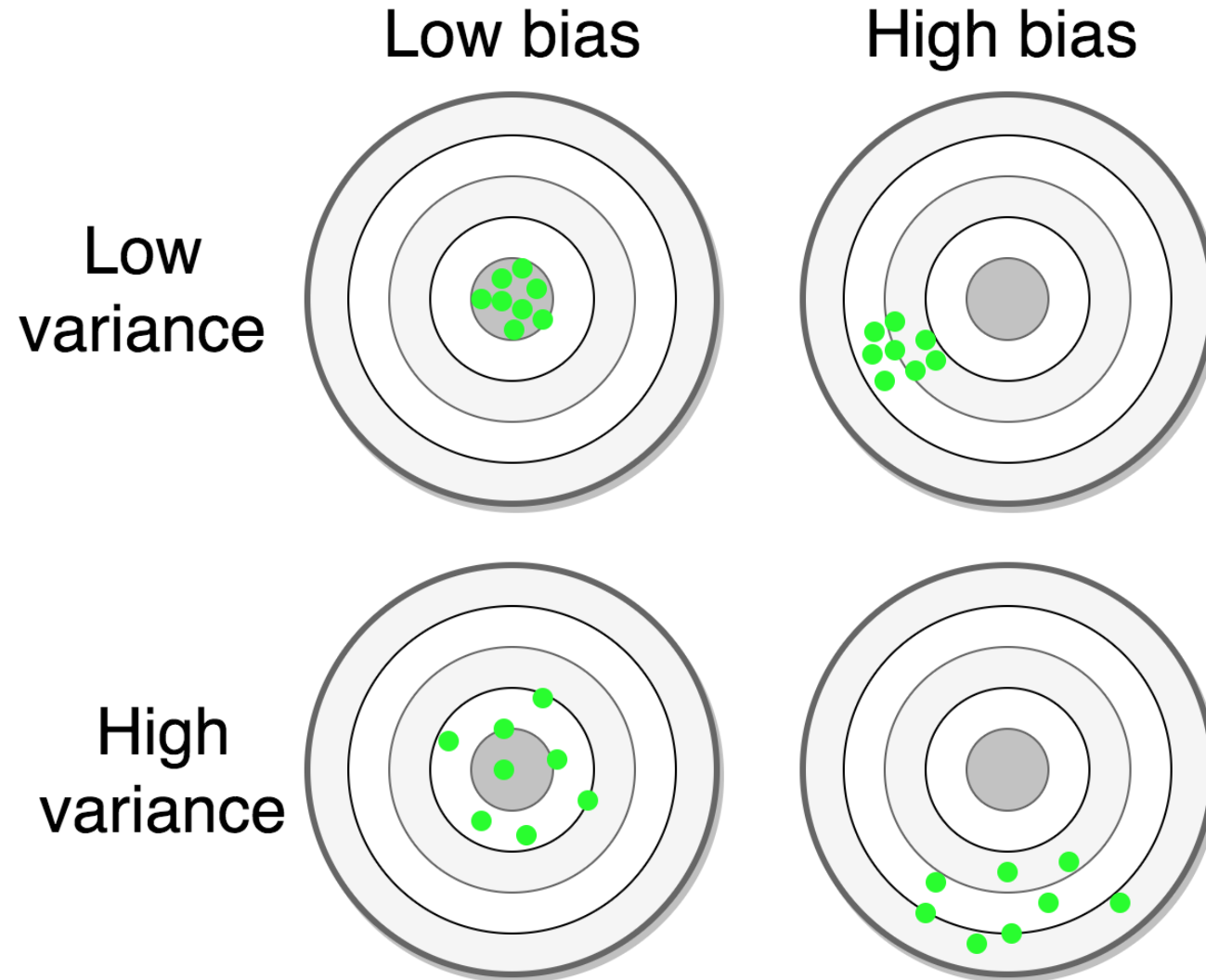
Impact of training points



Bias Variance Trade-off



Bias Variance Trade-off



Regularization / Shrinkage

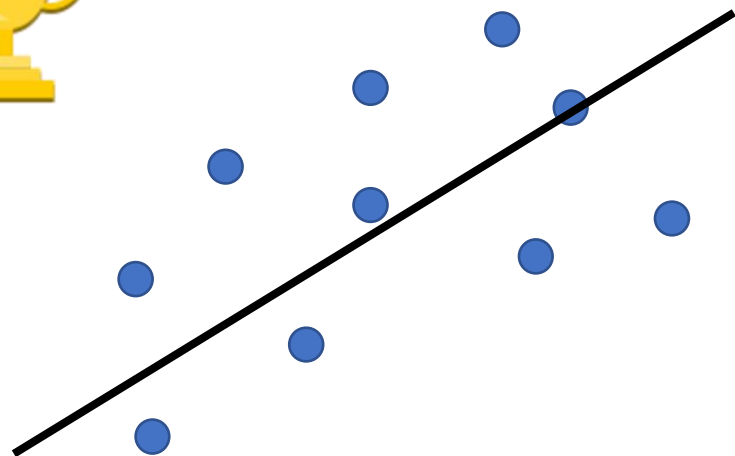
Ridge / L2

$$\sum_{i=1}^n \left(y_i - \beta_0 - \sum_{j=1}^p \beta_j x_{ij} \right)^2 + \lambda \sum_{j=1}^p \beta_j^2 = \text{RSS} + \lambda \sum_{j=1}^p \beta_j^2$$

Lasso / L1

$$\sum_{i=1}^n \left(y_i - \beta_0 - \sum_{j=1}^p \beta_j x_{ij} \right)^2 + \lambda \sum_{j=1}^p |\beta_j| = \text{RSS} + \lambda \sum_{j=1}^p |\beta_j|$$

SIMPLE MODEL



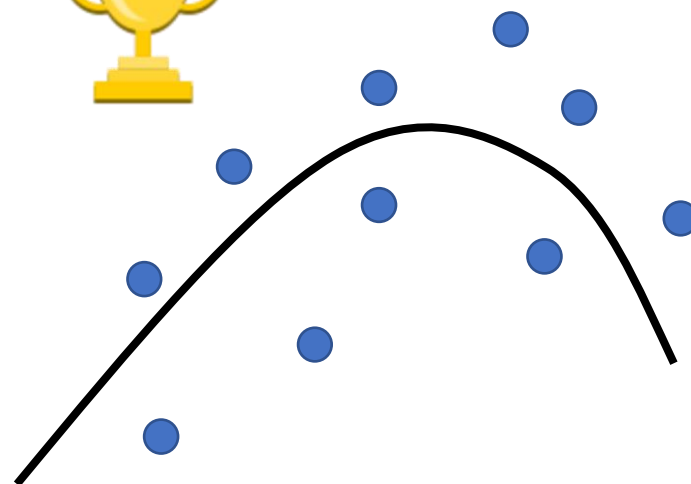
ERROR:



$$3x_1 + 4x_2 + 5$$



COMPLEX MODEL



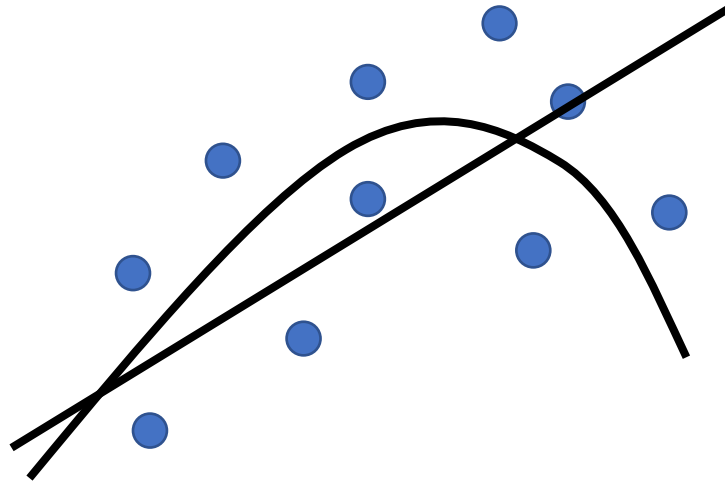
ERROR:



$$2x_1^3 - 2x_1^2x_2 - 4x_2^3 + 3x_1^2 + 6x_1x_2 + 4x_2^2 + 5$$



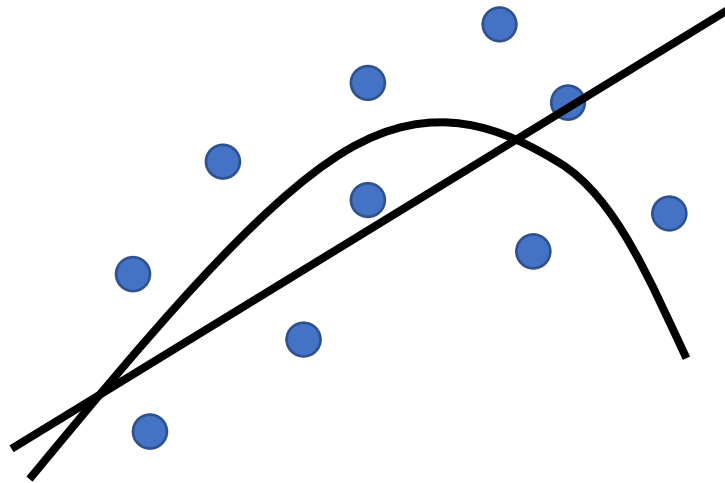
L1 (Lasso) Regularization



$$2x_1^3 - 2x_1^2x_2 - 34x_1^3 + 43x_1^2x_2 + 6x_1x_2 + 4x_2^2 + 5$$

$$|2| + |-2| + |-34| + |43| + |6| + |4| = 76$$

L2 (Ridge) Regularization



$$2x_1^3 - 2x_1^2x_2 - 3x_1x_2^2 + 4x_2^3 + 5 + 6x_1x_2 + 4x_2^2 + 5$$

$$2^2 + (-2)^2 + (-3)^2 + 4^2 + 5^2 + 6^2 + 4^2 = 85$$

Simple vs Complex Models



Requires LOW ERROR
OK if it's COMPLEX

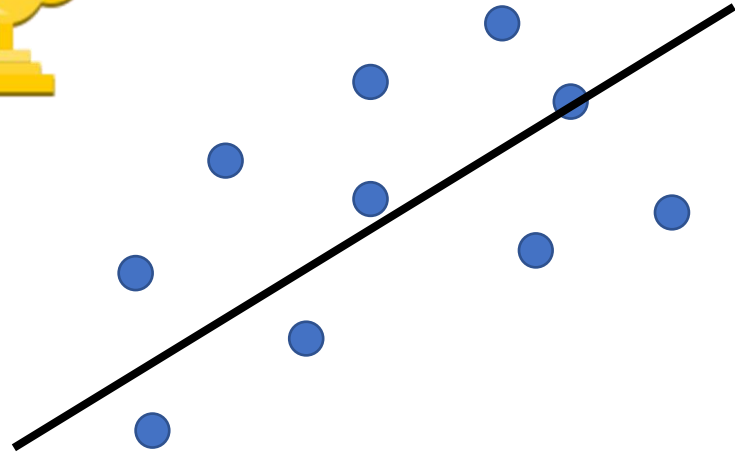
PUNISHMENT on COMPLEXITY should be
SMALL



Requires SIMPLICITY
OK with ERRORS

PUNISHMENT on COMPLEXITY should be
BIG

The λ Parameter

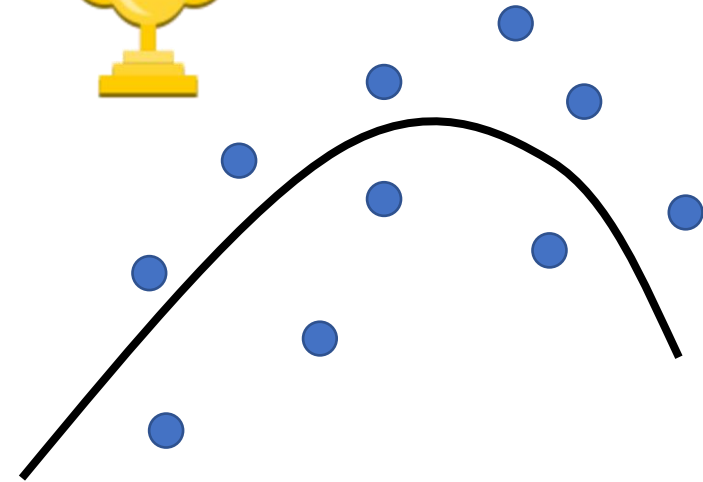


λ

ERROR:



$$3x_1 + 4x_2 + 5$$



λ

ERROR:



$$2x_1^3 - 2x_1^2x_2 - 4x_2^3 + 3x_1^2 + 6x_1x_2 + 4x_2^2 + 5$$

SAMPLE λ