

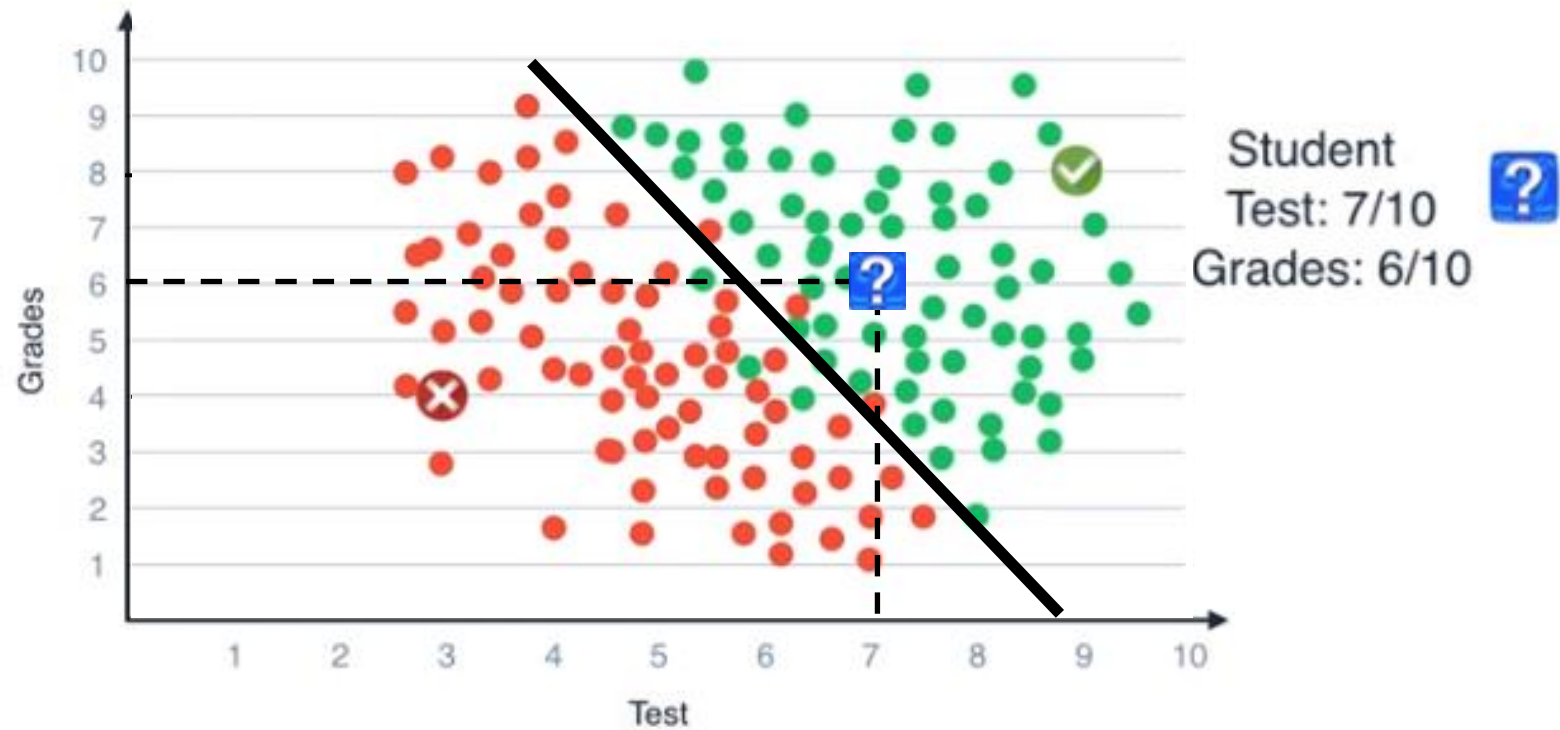
# Classification



Test



Grades





BOUNDARY: A LINE  $2x_1 + x_2 - 18 = 0$

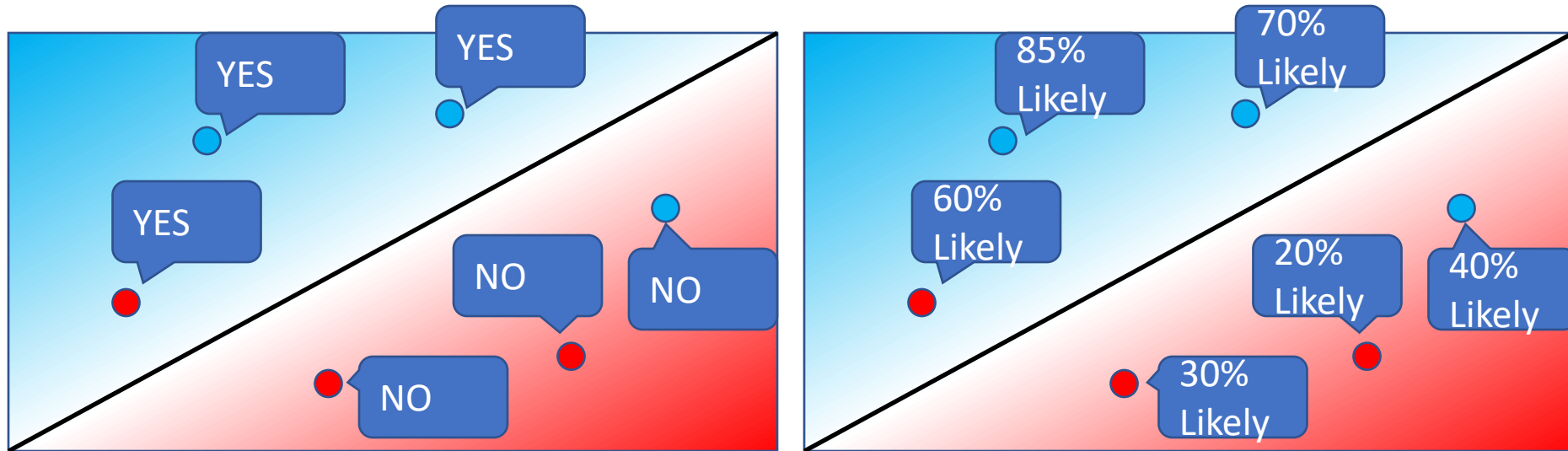
Score =  $2 * \text{Test} + \text{Grades} - 18$

PREDICTION:  $\left\{ \begin{array}{l} \text{score} \geq 0 \text{ ACCEPT} \\ \text{score} < 0 \text{ REJECT} \end{array} \right\}$

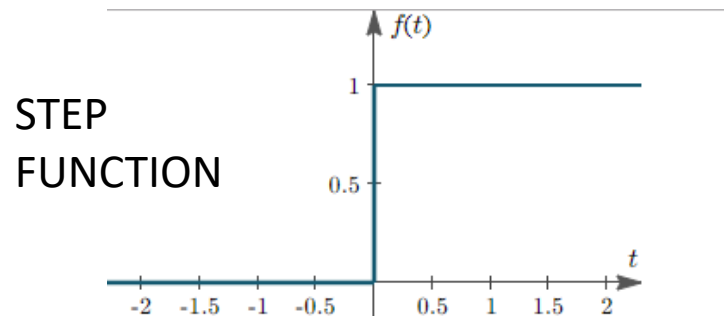
Now that you know the equation for the line ( $2x_1 + x_2 - 18 = 0$ ), and similarly the “score” ( $2x_1 + x_2 - 18$ ), what is the score of the student who got 7 in the test and 6 for grades?



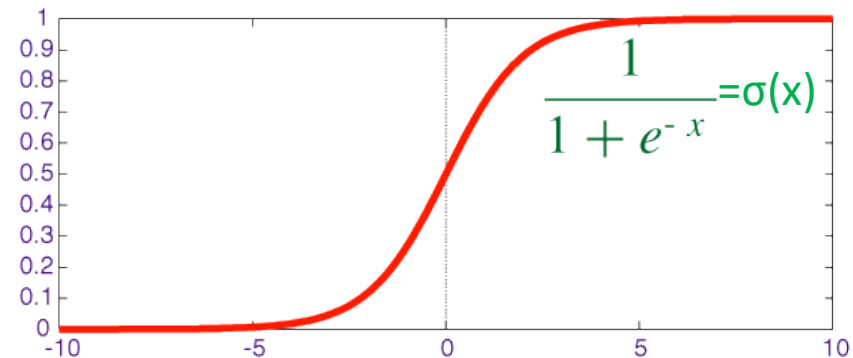
# Discrete vs Continuous



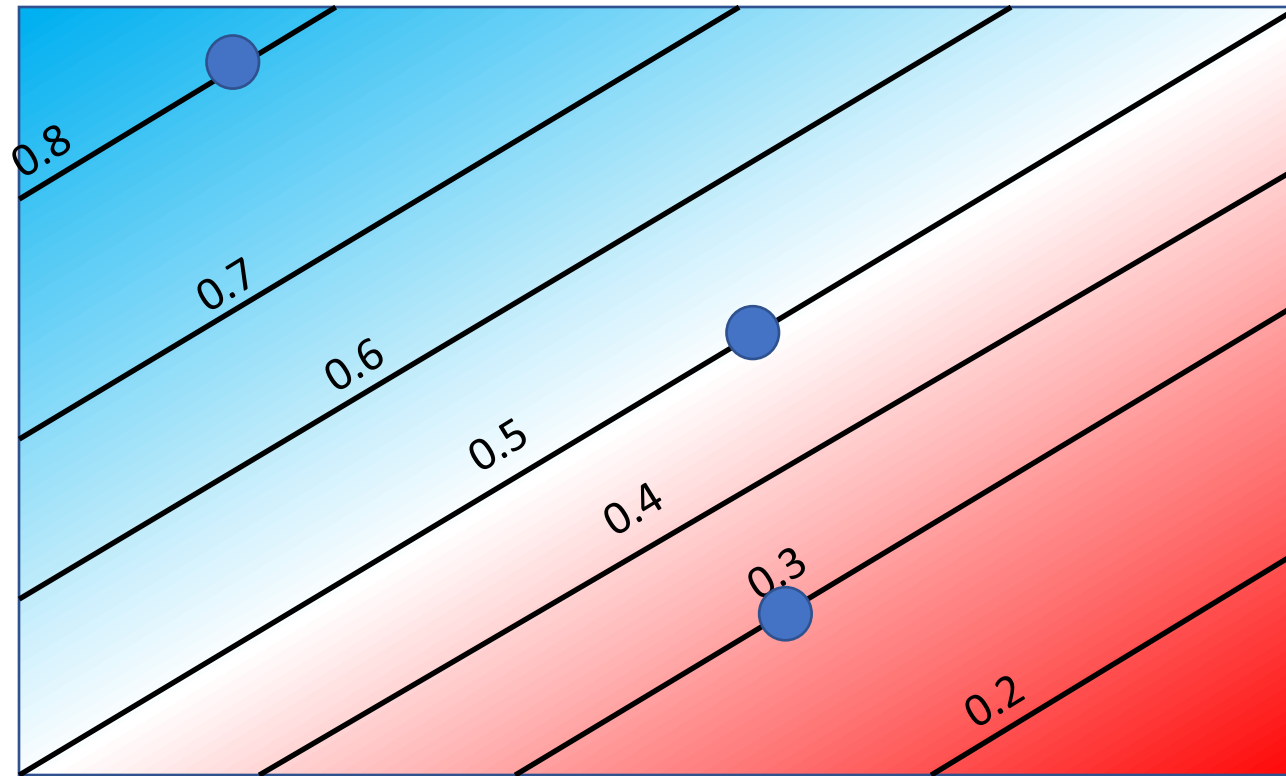
PREDICTION:  $\left. \begin{array}{l} \text{score} \geq 0 \text{ YES} \\ \text{score} < 0 \text{ NO} \end{array} \right\}$



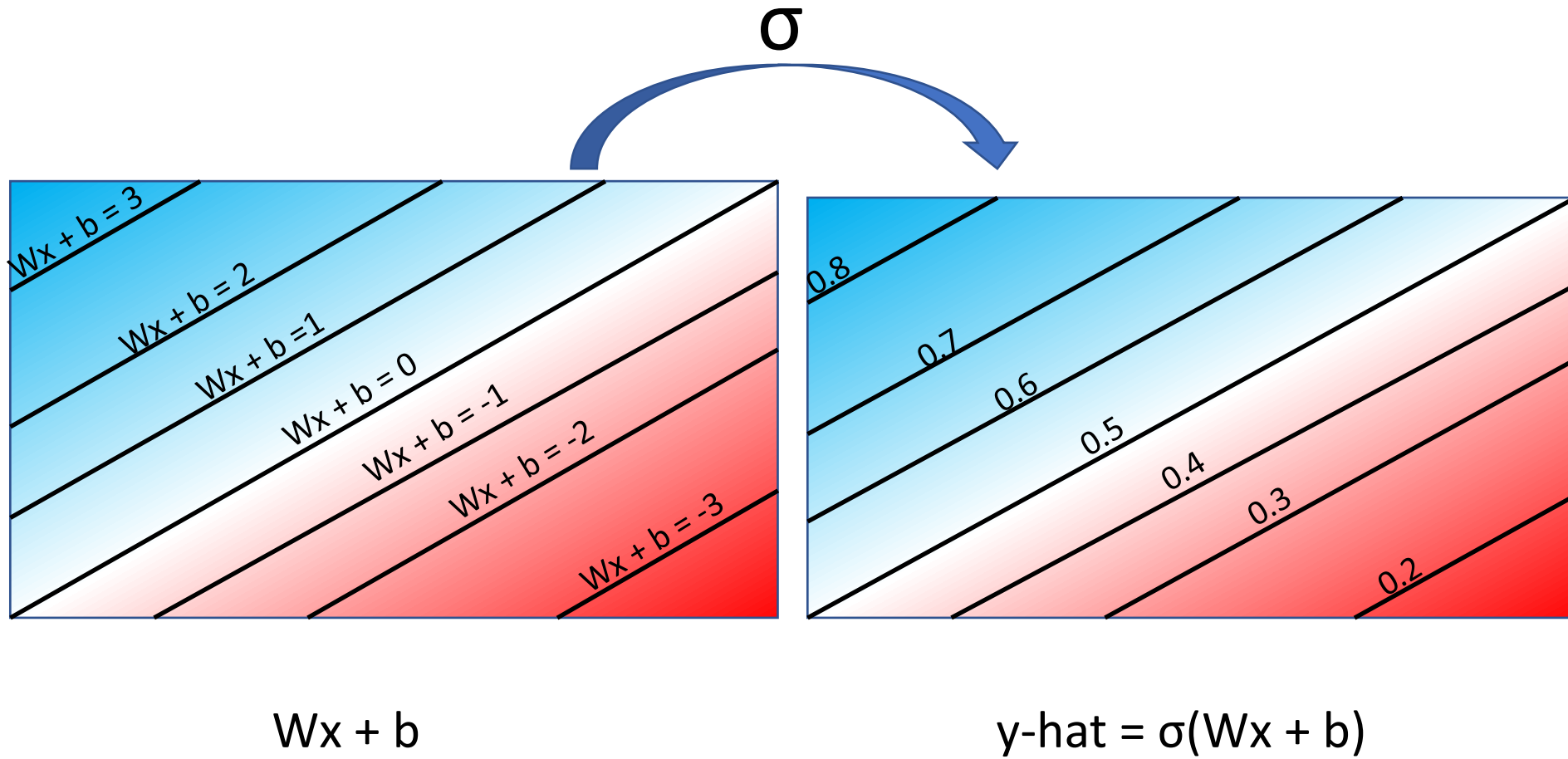
SIGMOID FUNCTION



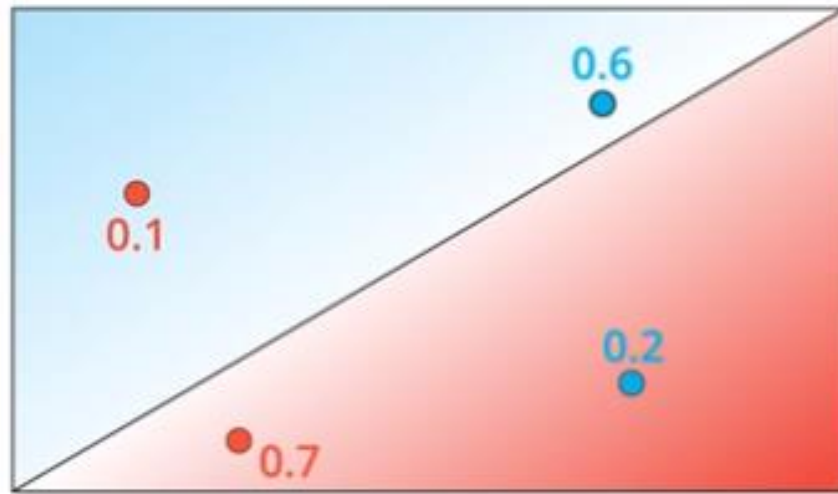
# Predictions



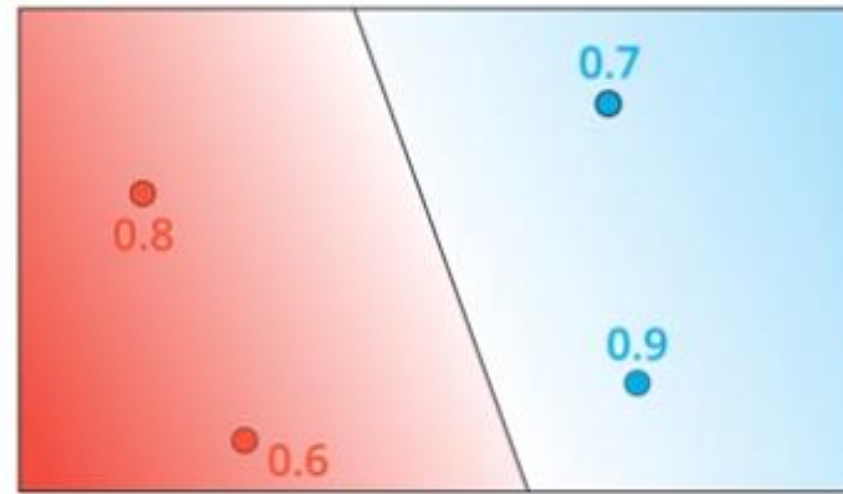
# Predictions



# Maximum Likelihood



$$0.6 * 0.2 * 0.1 * 0.7 = 0.0084$$



$$0.7 * 0.9 * 0.8 * 0.6 = 0.3024$$





# Products of Probabilities

$$0.6 * 0.2 * 0.1 * 0.7 = 0.0084$$

$$0.7 * 0.9 * 0.8 * 0.6 = 0.3024$$



Quiz:

What function to use?

- sin ☐
- cos ☐
- log ☐
- exp ☐

# Cross Entropy

$$0.6 * 0.2 * 0.1 * 0.7 = 0.0084$$

$$0.7 * 0.9 * 0.8 * 0.6 = 0.3024$$

$$\begin{aligned} \ln(0.6) + \ln(0.2) + \ln(0.1) + \ln(0.7) \\ -0.51 \quad -1.61 \quad -2.3 \quad -0.36 \end{aligned}$$

$$\begin{aligned} \ln(0.7) + \ln(0.9) + \ln(0.8) + \ln(0.6) \\ -0.36 \quad -0.1 \quad -0.22 \quad -0.51 \end{aligned}$$

$$\begin{aligned} -\ln(0.6) - \ln(0.2) - \ln(0.1) - \ln(0.7) \\ 0.51 \quad 1.61 \quad 2.3 \quad 0.36 \end{aligned}$$

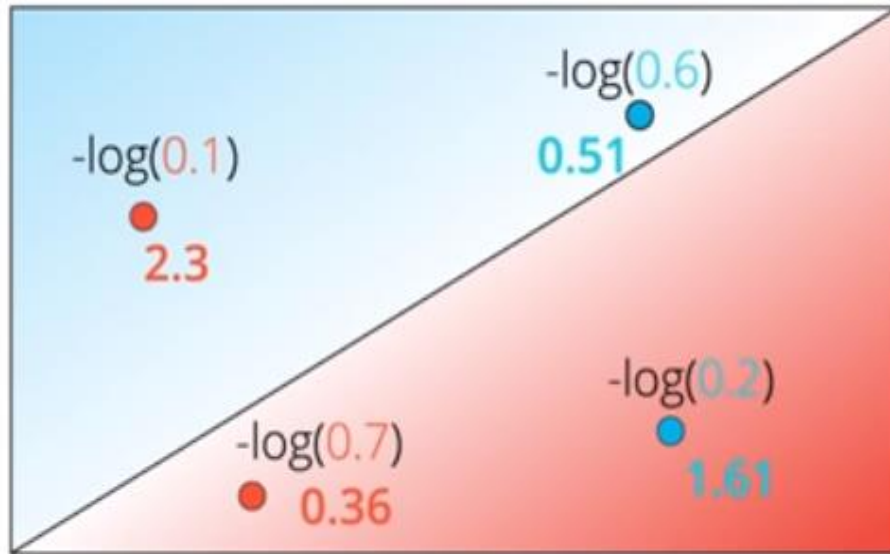
$$\begin{aligned} -\ln(0.7) - \ln(0.9) - \ln(0.8) - \ln(0.6) \\ 0.36 \quad 0.1 \quad 0.22 \quad 0.51 \end{aligned}$$

4.8

1.2

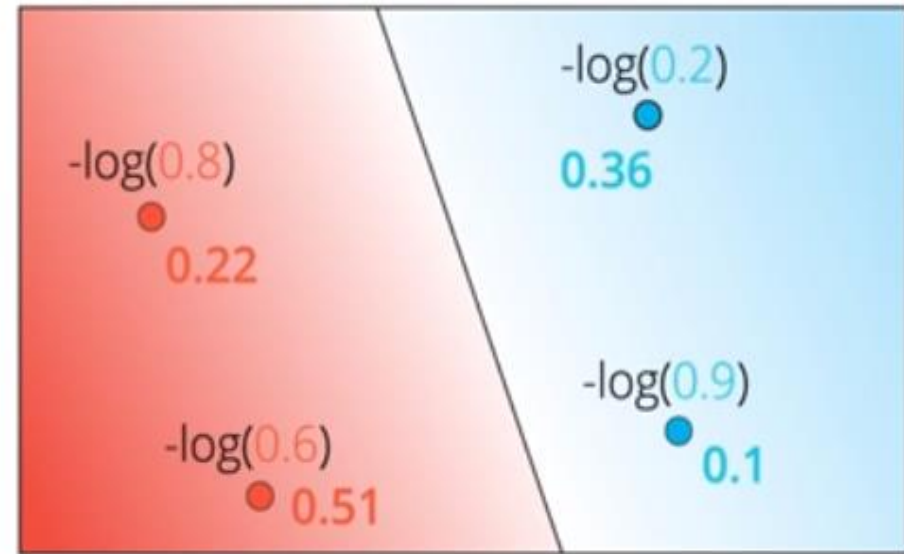
CROSS ENTROPY

# Cross Entropy



$$0.6 * 0.2 * 0.1 * 0.7 = 0.0084$$

$$-\log(0.6) - \log(0.2) - \log(0.1) - \log(0.7) = 4.8$$

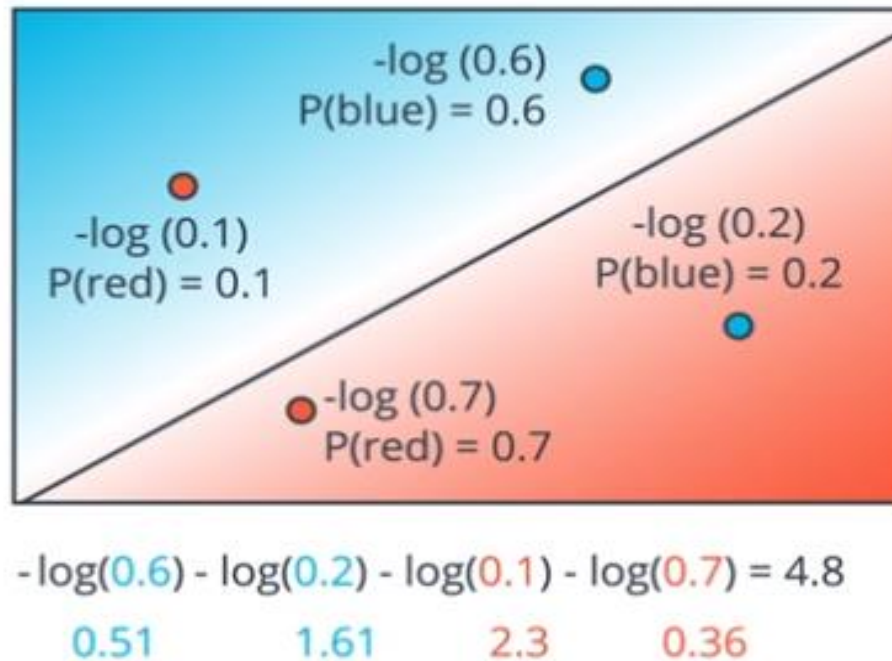


$$0.7 * 0.9 * 0.8 * 0.6 = 0.3024$$

$$-\log(0.7) - \log(0.9) - \log(0.8) - \log(0.6) = 1.2$$



# Error Function



If  $y = 1$

$$P(\text{blue}) = \hat{y}$$

$$\text{Error} = -\ln(\hat{y})$$

If  $y = 0$

$$P(\text{red}) = 1 - P(\text{blue}) = 1 - \hat{y}$$

$$\text{Error} = -\ln(1 - \hat{y})$$

$$\text{Error} = -(1-y)(\ln(1-\hat{y})) - y\ln(\hat{y})$$

$$\text{Error Function} = -\frac{1}{m} \sum_{i=1}^m (1-y_i)(\ln(1-\hat{y}_i)) + y_i \ln(\hat{y}_i)$$

$$E(W,b) = -\frac{1}{m} \sum_{i=1}^m (1-y_i)(\ln(1-\sigma(Wx^{(i)}+b))) + y_i \ln(\sigma(Wx^{(i)}+b))$$



MOUNT  
ERRORIST