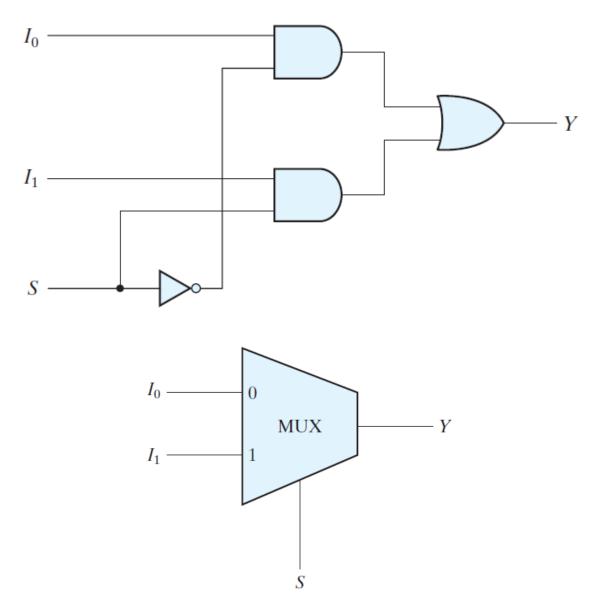


Lecture 12 — Combinational logic circuits

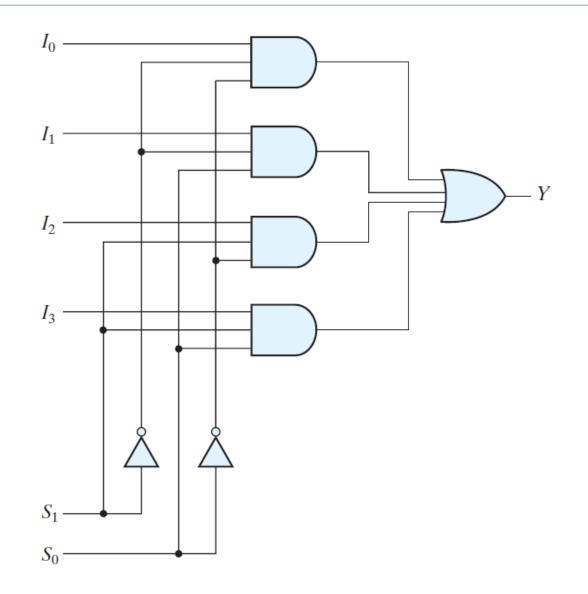
Dr. Aftab M. Hussain,

Assistant Professor, PATRIOT Lab, CVEST

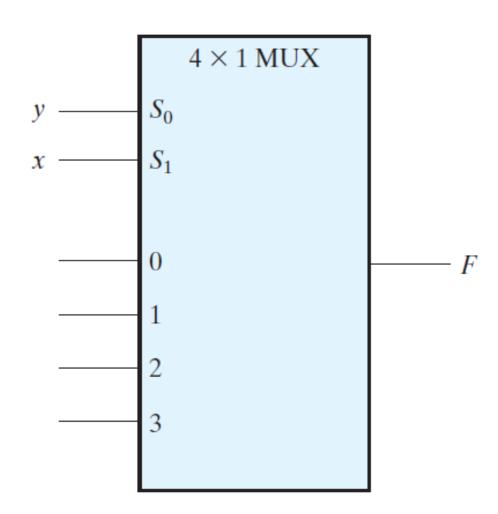
- A multiplexer is a combinational circuit that selects binary information from one of many input lines and directs it to a single output line
- The selection of a particular input line is controlled by a set of selection lines
- Normally, there are 2ⁿ input lines and n selection lines whose bit combinations determine which input is selected
- A two-to-one-line multiplexer connects one of two 1-bit sources to a common destination
- The multiplexer acts like an electronic switch that selects one of two sources
- The block diagram of a multiplexer (also called MUX) is sometimes depicted by a wedge-shaped symbol



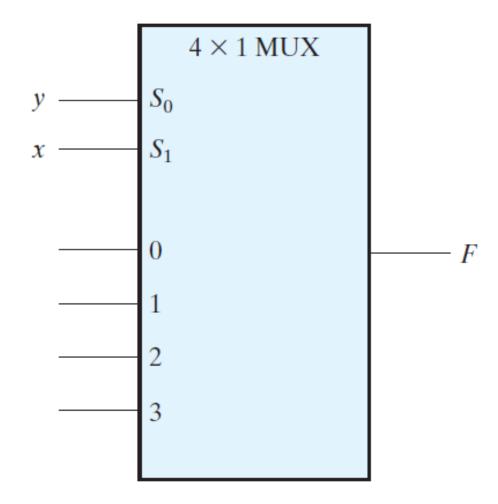
- Similarly, we can make a four-to-one-line multiplexer
- Each of the four inputs, I_0 through I_3 , is applied to one input of an AND gate
- The outputs of the AND gates are applied to a single OR gate that provides the oneline output
- A multiplexer is also called a data selector, since it selects one of many inputs and steers the binary information to the output line
- In general, a 2ⁿ-to-1-line multiplexer is constructed ANDing each input line with 2ⁿ minterms
- The outputs of the AND gates are applied to a single OR gate



- We can use MUXes to implement Boolean functions
- The minterms of a function are generated in a multiplexer by the circuit associated with the selection inputs
- The individual minterms can be selected by the data inputs, thereby providing a method of implementing a Boolean function of *n* variables with a multiplexer that has *n* selection inputs and 2ⁿ data inputs, one for each minterm
- Example: implement EXOR



- There is a neat trick to obtain a more efficient method for implementing a Boolean function of n variables with a multiplexer that has n - 1 selection inputs
- The first *n* 1 variables of the function are connected to the selection inputs of the multiplexer
- The remaining single variable of the function is used for the data inputs
- Say we have a three variable function F(x,y,z)
- We take a 4to1 MUX (with two input select lines) and each data input of the multiplexer will be z, z', 1, or 0

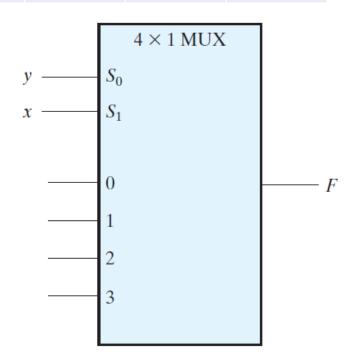


• Consider the function:

$$F(x, y, z) = \sum (1,4,5,6)$$

- This function of three variables can be implemented with a four-to-one-line multiplexer
- The two variables x and y are applied to the selection lines in that order; x is connected to the S₁ input and y to the S₀ input
- The values for the data input lines are determined from the truth table of the function
- When xy = 00, output F is equal to z because F = 0 when z = 0 and F = 1 when z = 1
- This requires that variable z be applied to data input 0
- In a similar fashion, we can determine the required input to data lines 1, 2, and 3 from the value of *F* when *xy* = 01, 10, and 11, respectively

X	Υ	Z	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	0



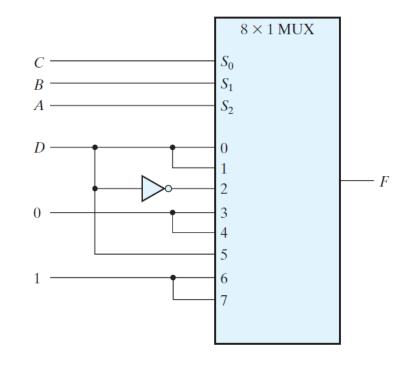
- The general procedure for implementing any Boolean function of n variables with a multiplexer with n 1 selection inputs and 2^{n-1} data inputs follows from the previous example
- 1. To begin with, Boolean function is listed in a truth table
- 2. Then the most significant *n* 1 variables in the table are applied to the selection inputs of the multiplexer
- 3. For each combination of the selection variables, we evaluate the output as a function of the last variable
- 4. This function can be 0, 1, the variable, or the complement of the variable
- 5. These values are then applied to the data inputs in the proper order

$$F(A, B, C, D) = \sum (1, 3, 4, 11, 12, 13, 14, 15)$$

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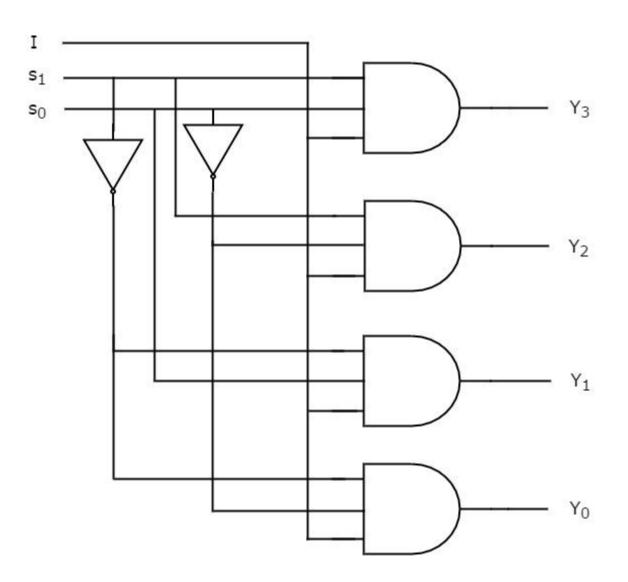
$$F(A, B, C, D) = \sum (1, 3, 4, 11, 12, 13, 14, 15)$$

A	B	C	D	F	
0	0	0	0 1	0 1	F = D
0	0	1 1	0 1	0 1	F = D
0	1 1	0	0 1	1 0	F = D'
0	1 1	1 1	0 1	0	F = 0
1 1	0	0	0 1	0	F = 0
1 1	0	1 1	0 1	0 1	F = D
1 1	1 1	0	0 1	1 1	F = 1
1 1	1 1	1 1	0 1	1 1	F = 1



Demultiplexer

- Demultiplexers do the exact opposite of MUX operation – take a single line input and direct it to an output line depending on the select line input
- 1to2ⁿ Demux will have n select lines
- We again make minterms from the available inputs and AND it with the single data line
- Based on the input signals the particular output is connected to the data line and all other outputs are zero

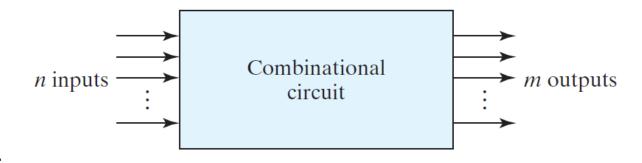


Combinational circuits

- Logic circuits for digital systems may be combinational or sequential
- A combinational circuit consists of logic gates whose outputs at any time are determined from only the present combination of inputs
- A combinational circuit performs an operation that can be specified logically by a set of Boolean functions
- In contrast, sequential circuits employ storage elements in addition to logic gates
- Their outputs are a function of the inputs and the state of the storage elements
- Because the state of the storage elements is a function of previous inputs, the
 outputs of a sequential circuit depend not only on present values of inputs, but
 also on past inputs, and the circuit behavior must be specified by a time sequence
 of inputs and internal states

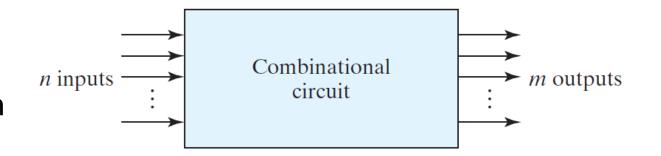
Combinational circuits

- A combinational circuit consists of an interconnection of logic gates
- Combinational logic gates react to the values of the signals at their inputs and produce the value of the output signal, transforming binary information from the given input data to a required output data
- Each input and output variable exists physically as an analog signal whose values are interpreted to be a binary signal that represents logic 1 and logic 0



Combinational circuits

- For *n* input variables, there are 2ⁿ possible combinations of the binary inputs
- For each possible input combination, there is one possible value for each output variable
- Thus, a combinational circuit can be specified with a truth table that lists the output values for each combination of input variables
- A combinational circuit also can be described by m Boolean functions, one for each output variable
- Each output function is expressed in terms of the *n* input variables



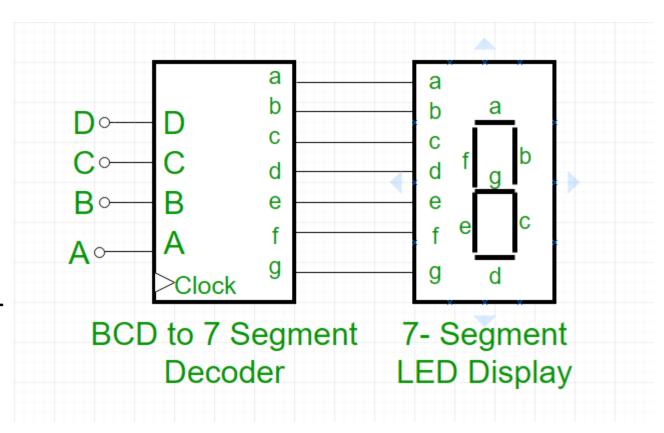
Circuit design

- The design of combinational circuits starts from the specification of the design objective and culminates in a logic circuit diagram or a set of Boolean functions from which the logic diagram can be obtained
- The procedure involves the following steps:
- 1. From the specifications of the circuit, determine the required number of inputs and outputs and assign a symbol to each
- 2. Derive the truth table that defines the required relationship between inputs and outputs
- 3. Make the K-map, if necessary
- Obtain the simplified Boolean functions for each output as a function of the input variables
- Draw the logic diagram and verify the correctness of the design (manually or by simulation)

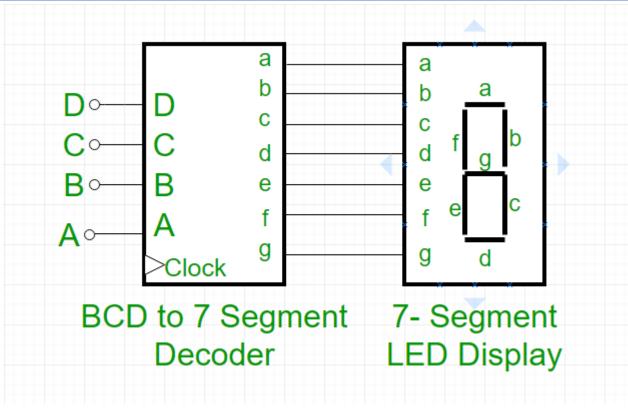
Here. We. Go.

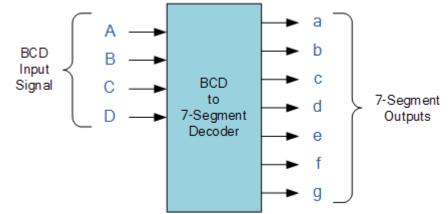
The 7-Degment Decoden

- We discussed many ways of representing symbols using binary variables – signed magnitude, 2's complement, BCD, ASCII etc.
- Going from one representation may be considered as an encoding/decoding operation
- Consider the practical problem of displaying binary numbers using a 7segment LED display
- For this, we need to "decode" the binary information into the display inputs



- First, we realize that there are 4 inputs and 7 outputs!
- Thus, the truth-table will be a 16 row table with 7 different columns for 7 outputs
- Hence, there will be 7 different functions we will be implementing to make this decoder
- The other thing we need to realize is whether a particular output should be HIGH or LOW for the LED to glow?



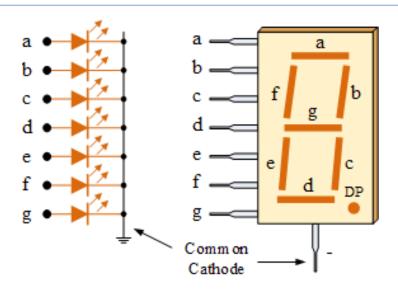


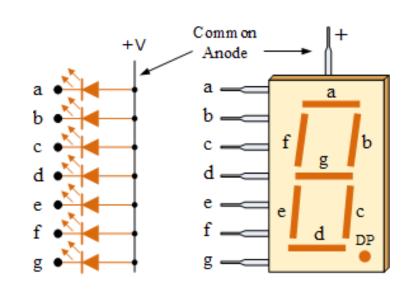
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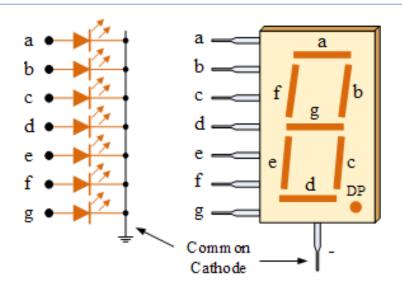
Lecture 11

- The other thing we need to realize is whether a particular output should be HIGH or LOW for the LED to glow?
- To know the answer to this, we see that there are two types of 7-segment LED displays – common anode and common cathode
- The common cathode connects all LED cathodes to a common ground, thus, when input is high LED glows
- Conversely, the common anode connects all LED anodes to +V_{cc}, thus, when input is low, LED glows





- Let us choose common cathode LED display to make the function
- Thus, we can make the truth-table
- Obviously, the BCD system only goes from 0 to 9, while we have 16 rows for 4 inputs
- What about the other rows?
- In the other rows, we fill all the outputs as don't care, because we are sure that these are not going to be input anyway (trust the engineer before you)
- Thus, we have six don't care conditions



Α	В	С	D	а	b	С	d	е	f	g
0	0	0	0	1	1	1	1	1	1	0
0	0	0	1	0	1	1	0	0	0	0
0	0	1	0	1	1	0	1	1	0	1
0	0	1	1	1	1	1	1	0	0	1
0	1	0	1	0	1	1	0	0	1	1
0	1	0	1	1	0	1	1	0	1	1
0	1	1	0	1	0	1	1	1	1	1
0	1	1	1	1	1	1	0	0	0	0
1	0	0	0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1	0	1	1