

>

Задание 1

> $syst := \{y1'(x) = -y1(x) + 2 y2(x), y2'(x) = 6 y1(x)\} :$

$dsolve(syst, \{y1(x), y2(x)\});$

$A := Matrix([[-1, 2], [6, 0]]);$

$LinearAlgebra[Eigenvectors](A);$

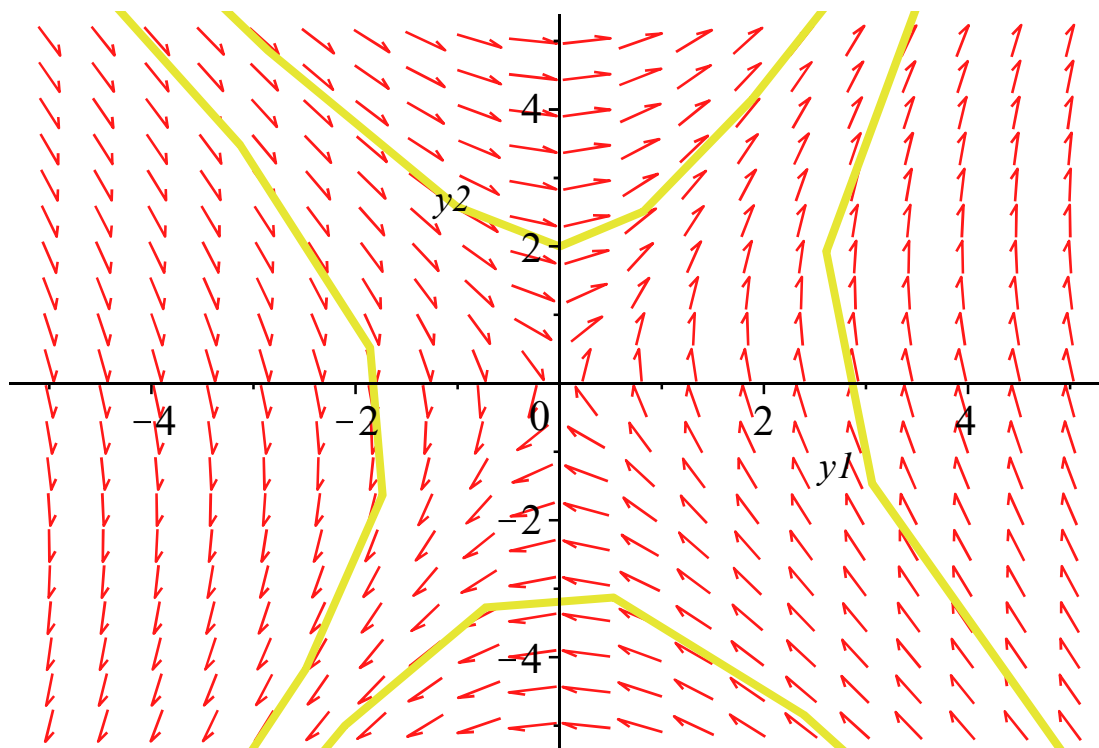
$$\left\{y1(x) = -\frac{2}{3} \frac{C1}{e^{-4x}} + \frac{C2}{2} e^{3x}, y2(x) = -C1 e^{-4x} + C2 e^{3x}\right\}$$

$$A := \begin{bmatrix} -1 & 2 \\ 6 & 0 \end{bmatrix}$$

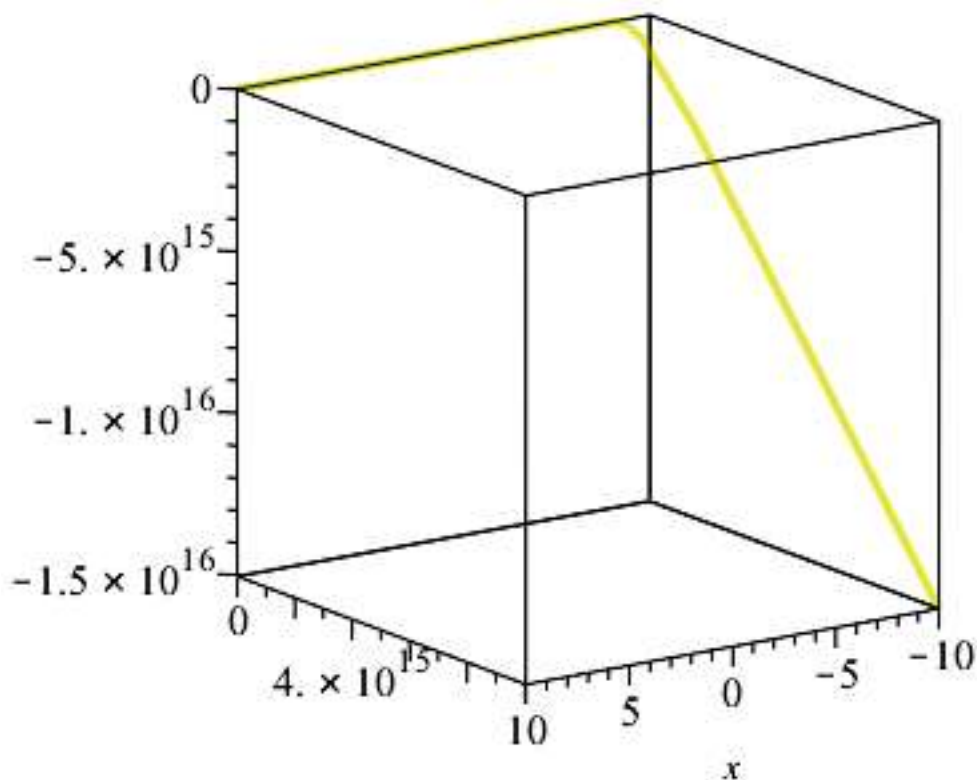
$$\begin{bmatrix} 3 \\ -4 \end{bmatrix}, \begin{bmatrix} \frac{1}{2} & -\frac{2}{3} \\ 1 & 1 \end{bmatrix}$$

(1)

> $DEtools[phaseportrait](syst, [y1(x), y2(x)], x = -5..5, [[0, 0, 2], [3, 0, -3], [1, -2, 1], [2, 3, 4]], y1 = -5..5, y2 = -5..5);$



> $DEtools[DEplot3d](syst, [y1(x), y2(x)], x = -10..10, [[0.1, 0.1, 0.1]]);$



Задание 2

> $\text{syst} := \{y1'(x) = 3 y1(x) + 12 y2(x), y2'(x) = y1(x) + 7 y2(x)\} :$
 $\text{dsolve}(\text{syst}, \{y1(x), y2(x)\});$

$$\left\{ y1(x) = _C1 e^{9x} + _C2 e^x, y2(x) = -\frac{C1 e^{9x}}{2} - \frac{C2 e^x}{6} \right\}$$

(2)

Задание 3

> $\text{syst} := x'(t) = x(t) - 2 y(t) + 1, y'(t) = -3 x(t) :$

$\text{cond} := x(0) = 0, y(0) = 1 :$

$s := \text{dsolve}(\{\text{syst}, \text{cond}\}, \{x(t), y(t)\});$

$\text{DEtools}[\text{DEplot3d}](\{\text{syst}\}, [x(t), y(t)], t = -2..2, [[0, 0, 1]]);$

$$s := \left\{ x(t) = \frac{e^{-2t}}{5} - \frac{e^{3t}}{5}, y(t) = \frac{3 e^{-2t}}{10} + \frac{e^{3t}}{5} + \frac{1}{2} \right\}$$

