

(1)

Задание 1

$$> f := (x, n) \rightarrow \frac{2n-5}{n+7} \cdot \frac{1}{(3x^2-4x+2)^n} :$$

$$\text{Limit}\left(\frac{f(x, n+1)}{f(x, n)}, n = \text{infinity}\right) = \text{limit}\left(\frac{f(x, n+1)}{f(x, n)}, n = \text{infinity}\right);$$

$$\lim_{n \rightarrow \infty} \frac{(2n-3)(n+7)(3x^2-4x+2)^n}{(n+8)(3x^2-4x+2)^{n+1}(2n-5)} = \frac{1}{3x^2-4x+2}$$

(2)

$$> \text{solve}\left(\left|\frac{1}{3x^2-4x+2}\right| < 1\right);$$

$$\left(-\infty, \frac{1}{3}\right), (1, \infty)$$

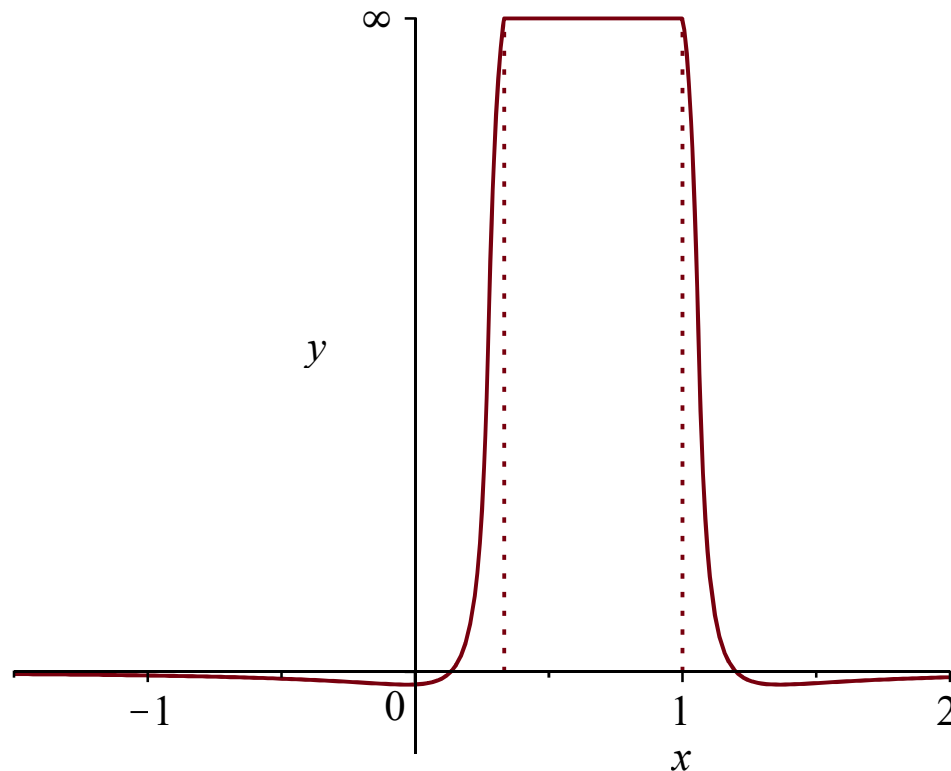
(3)

$$> y1 := \text{plot}(\text{sum}(f(x, n), n = 1..10000), x = -1.5..2, y = -1..\text{infinity}) :$$

$$y2 := \text{plot}\left(\left[\frac{1}{3}, t, t = 0..\text{infinity}\right], x = -1.5..2, y = -1..\text{infinity}, \text{linestyle} = 2\right) :$$

$$y3 := \text{plot}([1, t, t = 0..\text{infinity}], x = -1.5..2, y = -1..\text{infinity}, \text{linestyle} = 2) :$$

$$\text{plots}[\text{display}]([y1, y2, y3]);$$



Задание 2.

$$> f := (x, n) \rightarrow \frac{x^n}{7n-10} :$$

$$\text{Limit}(f(x, n), n = \text{infinity}) = \text{limit}(f(x, n), n = \text{infinity}) \text{ assuming } 0 \leq x \leq 1;$$

$$\text{Limit}\left(\frac{f(x, n+1)}{f(x, n)}, n = \text{infinity}\right) = \text{limit}(f(x, n), n = \text{infinity}) \text{ assuming } 0 \leq x \leq 1;$$

$$\lim_{n \rightarrow \infty} \frac{x^n}{7n-10} = 0$$

$$\lim_{n \rightarrow \infty} \frac{x^{n+1}(7n-10)}{(7n-3)x^n} = 0$$

(4)

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> solve(1/(7*n-3) < 0.1, n);
n_min = 2;
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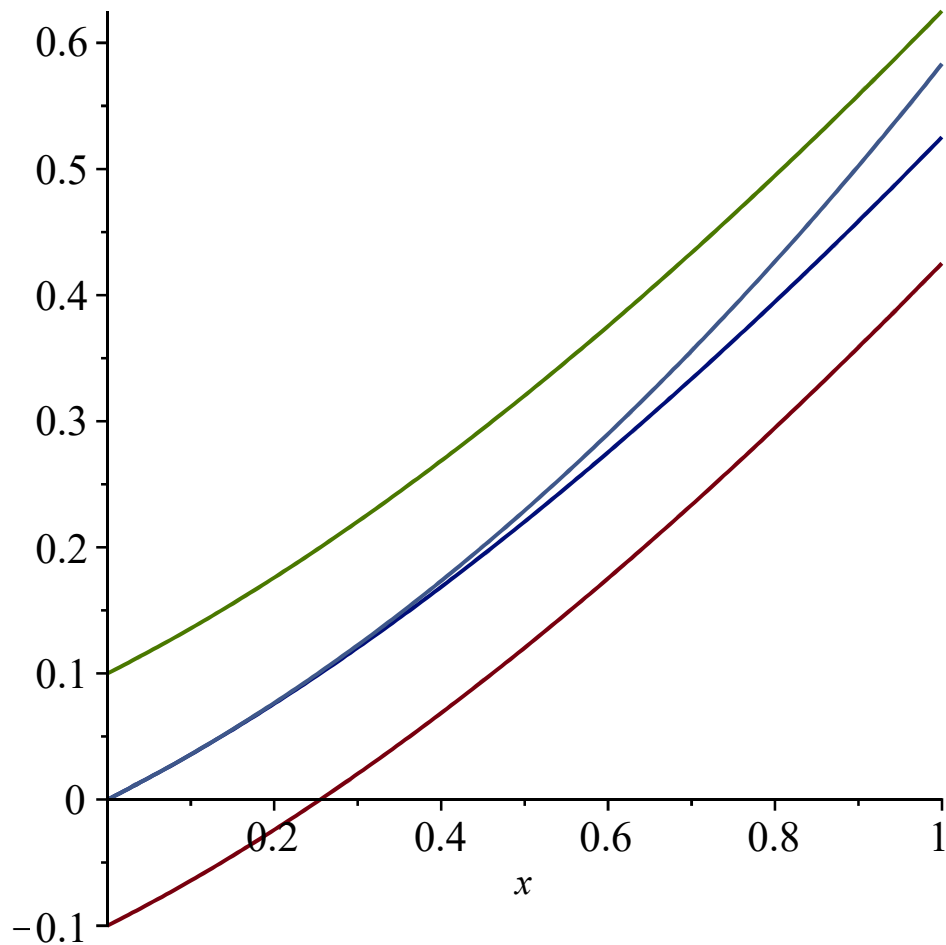
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y1 := sum((-1)^n * x^n / (7*n-10), n=1..infinity):
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y2 := sum((-1)^n * x^n / (7*n-10), n=1..2):
```

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plot([y1-0.1, y1, y1+0.1, y2], x=0..1);
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$(-\infty, 0.4285714286), (1.857142857, \infty)$

$n_{\min} = 2$



Задание 3.

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> f := x -> cos(4*x^2):
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f(x) = taylor(f(x), x=0, 20);
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Int(f(x), x=0..0.5) = evalf(int(f(x), x=0..0.5), 3);
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$$\cos(4x^2) = 1 - 8x^4 + \frac{32}{3}x^8 - \frac{256}{45}x^{12} + \frac{512}{315}x^{16} + O(x^{20})$$

$$\int_0^{0.5} \cos(4x^2) \, dx = 0.452$$

(5)

$$\text{> } f := n \rightarrow \frac{(-1)^n}{2 \cdot (2n)!(4n+1)} :$$

$$f(n+1) := f(n+1);$$

$$n > fsolve\left(\left|\frac{(-1)^{n+1}}{2(2n+2)!(4n+5)}\right| = 0.001, n\right);$$

$$Sum(f(n), n=0..2) = evalf(sum(f(n), n=0..2), 3);$$

$$f(n+1) := \frac{(-1)^{n+1}}{2(2n+2)!(4n+5)}$$

$$1.237344088 < n$$

$$\sum_{n=0}^2 \frac{(-1)^n}{2(2n)!(4n+1)} = 0.452$$

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