

# ASEN 5007-Homework 2

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## Problem 1

### Initializer Modules

Cell 1: module to form element stiffness of two-dimensional two-node bar element in global coordinates.

In[29]:=

```
ElemStiff2DTwoNodeBar[{x1_, y1_}, {x2_, y2_}], {Em_, A_}] := Module[
  {c, s, dx = x2 - x1, dy = y2 - y1, L, Ke},
  L = Sqrt[dx^2 + dy^2]; c = dx / L; s = dy / L;
  Ke = (Em * A / L) * {{ c^2, c * s, -c^2, -c * s},
    { c * s, s^2, -s * c, -s^2},
    {-c^2, -s * c, c^2, s * c},
    {-s * c, -s^2, s * c, s^2}};
  Return[Ke]
];
```

Cell 2 : module to merge two - node bar element stiffness into the master stiffness matrix.

In[30]:=

```
MergeElemIntoMasterStiff[Ke_, eftab_, Kin_] := Module[{i, j, ii, jj, K = Kin},
  For[i = 1, i <= 4, i++, ii = eftab[[i]];
    For[j = i, j <= 4, j++, jj = eftab[[j]];
      K[[jj, ii]] = K[[ii, jj]] += Ke[[i, j]]
    ]
  ]; Return[K]
];
```

Cell 3 : module to assemble master stiffness matrix of example truss.

In[31]:=

```

AssembleMasterStiffOfExampleTruss[] :=
  Module[{Ke, K = Table[0, {6}, {6}], s1 = 8, h = 3, Em = 1000, A1 = 2, A2 = 4},
    Ke = ElemStiff2DTwoNodeBar[{{0, 0}, {s1 / 2, h}}, {Em, A1}];
    K = MergeElemIntoMasterStiff[Ke, {1, 2, 3, 4}, K];
    Ke = ElemStiff2DTwoNodeBar[{{s1 / 2, h}, {s1, 0}}, {Em, A2}];
    K = MergeElemIntoMasterStiff[Ke, {3, 4, 5, 6}, K];
    (*Ke=ElemStiff2DTwoNodeBar[{{0,0},{10,10}}, {100, 2*Sqrt[2]}];
    K= MergeElemIntoMasterStiff[Ke, {1,2,5,6}, K]; *)
    Return[K]
  ];

```

Cell 4 : modules to apply homogeneous, single - freedom displacement BCs on master stiffness and forces.

In[32]:=

```

ModifiedMasterStiffForDBC[pdof_, K_] := Module[
  {i, j, k, nk = Length[K], np = Length[pdof], Kmod = K},
    For[k = 1, k <= np, k++, i = pdof[[k]];
      For[j = 1, j <= nk, j++, Kmod[[i, j]] = Kmod[[j, i]] = 0];
      Kmod[[i, i]] = 1];
    Return[Kmod]
];
ModifiedMasterForcesForDBC[pdof_, f_] := Module[
  {i, k, np = Length[pdof], fmod = f},
    For[k = 1, k <= np, k++, i = pdof[[k]]; fmod[[i]] = 0];
    Return[fmod]
];

```

Cell 5 : module to compute the internal force in a two - dimensional two - node bar element.

In[34]:=

```

IntForce2DTwoNodeBar[{{x1_, y1_}, {x2_, y2_}}, {Em_, A_}, eftab_, u_] :=
  Module[{c, s, dx = x2 - x1, dy = y2 - y1, L, ix, iy, jx, jy, ubar, e},
    L = Sqrt[dx^2 + dy^2]; c = dx / L; s = dy / L; {ix, iy, jx, jy} = eftab;
    ubar = {c * u[[ix]] + s * u[[iy]], -s * u[[ix]] + c * u[[iy]],
      c * u[[jx]] + s * u[[jy]], -s * u[[jx]] + c * u[[jy]]};
    e = (ubar[[3]] - ubar[[1]]) / L; Return[Em * A * e]
  ];

```

Cell 6 : module to get internal forces in members of example truss.

In[109]:=

```

IntForcesOfExampleTruss[u_] :=
  Module[{f = Table[0, {2}], s1 = 8, h = 3, Em = 1000, A1 = 2, A2 = 4},
    f[[1]] = IntForce2DTwoNodeBar[{{0, 0}, {s1 / 2, h}}, {Em, A1}, {1, 2, 3, 4}, u];
    f[[2]] = IntForce2DTwoNodeBar[{{s1 / 2, h}, {s1, 0}}, {Em, A2}, {3, 4, 5, 6}, u];
    (* f[[3]] = IntForce2DTwoNodeBar[{{0, 0}, {10, 10}}, {100, 2*Sqrt[2]},
      {1, 2, 5, 6}, u]; *)
    Return[f]
  ];

```

Cell 7: Simple function to print output for solutions in a stylized way

```
In[36]:= PrintWithStyle[x_] :=
  Module[{color = LightGreen}, Framed[Style[x, 18, Bold, Background → color],
    Background → color]
  ]
```

## Problem 1 Driver Script

```
In[110]:=
```

```
f = {0, 0, 12, 0, 0, 0};
K = AssembleMasterStiffOfExampleTruss[];
Print["Master Stiffness Matrix: "]; Print[K // MatrixForm];

(*Nodes 1,2,5, and 6 are fixed in position. No movement can occur*)
Kmod = ModifiedMasterStiffForDBC[{1, 2, 5, 6}, K];
fmod = ModifiedMasterForcesForDBC[{1, 2, 5, 6}, f];
u = Simplify[Inverse[Kmod].fmod];
Print["Computed nodal displacements:"];
PrintWithStyle[u]
f = Simplify[K.u];
Print["External node forces including reactions:"];
PrintWithStyle[f]
p = Simplify[IntForcesOfExampleTruss[u]];
Print["Internal member forces:"]
PrintWithStyle[p]
```

Master Stiffness Matrix:

$$\begin{pmatrix} 256 & 192 & -256 & -192 & 0 & 0 \\ 192 & 144 & -192 & -144 & 0 & 0 \\ -256 & -192 & 768 & -192 & -512 & 384 \\ -192 & -144 & -192 & 432 & 384 & -288 \\ 0 & 0 & -512 & 384 & 512 & -384 \\ 0 & 0 & 384 & -288 & -384 & 288 \end{pmatrix}$$

Computed nodal displacements:

```
Out[117]=
```

$$\left\{0, 0, \frac{9}{512}, \frac{1}{128}, 0, 0\right\}$$

External node forces including reactions:

```
Out[120]=
```

$$\left\{-6, -\frac{9}{2}, 12, 0, -6, \frac{9}{2}\right\}$$

Internal member forces:

```
Out[123]=
```

$$\left\{\frac{15}{2}, -\frac{15}{2}\right\}$$