

ASEN 5070 HW # 10

1. Program the Givens square root free algorithm (Eq. 5.4.70).

Given the problem of HW # 8 i. e.,

$$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \end{bmatrix} = \begin{bmatrix} 1 & \delta \\ 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} \varepsilon_1 \\ \varepsilon_2 \end{bmatrix}, \bar{X} = \begin{bmatrix} \bar{x}_1 \\ \bar{x}_2 \end{bmatrix} = \begin{bmatrix} 4 \\ 7 \end{bmatrix}, P_0 = \begin{bmatrix} 1/\delta^2 & 0 \\ 0 & 1/\delta^2 \end{bmatrix}$$

$$R = I, \delta = 1 \times 10^{-2}, 1 \times 10^{-4}, 1 \times 10^{-6}, \dots, 1 \times 10^{-16}$$

- a. For each value of δ solve for \hat{X} and P_2 . Compare your results for P_2 to the exact solution (Eq (4.7.24)) by plotting the trace difference as you did in HW # 8.
- b. For $\delta = 1 \times 10^{-2}$, amaze your friends by demonstrating that $\sum_{i=1}^2 e_i^2$ from your solution** agrees with the results obtained from Eq (5.4.33). See also Eq(5.6.21).

**Note $\sum_{i=1}^2 e_i^2 = 6.51300624 \times 10^{-3}$ for this problem