

# Digital IC Design

EE5311

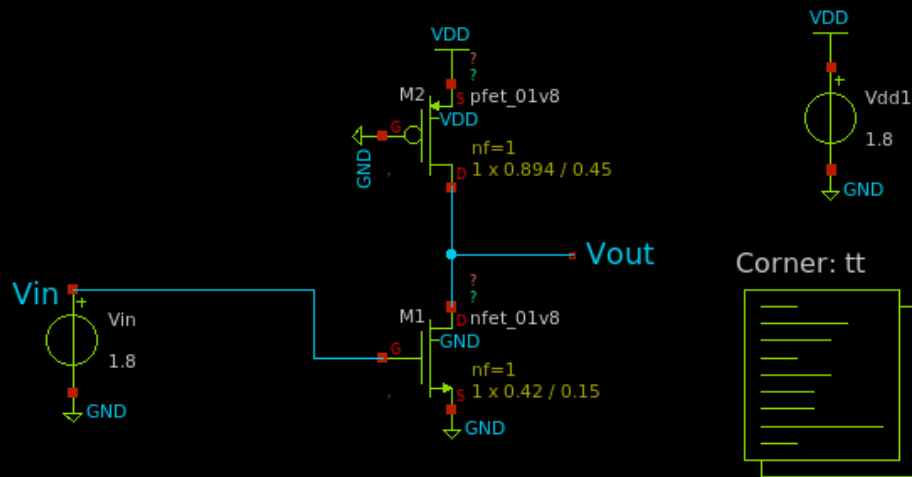
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EE22B045

Tutorial - 2  
Report

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# Experiment - 1

## Schematic:



```
s2
.control
  dc Vin 0 1.8 0.1
  plot v(Vout) vs v(Vin)

  let derivout = deriv(v(Vout))
  plot derivout
  meas dc Vil when derivout=-1 cross=1
  meas dc vih when derivout=-1 cross=2
  meas dc Vth when v(Vout)=0.9
  meas dc idd find i(Vdd1) when v(Vin)=1.8

  let NML = Vil
  let NMh = 1.8 - Vih
  echo NML: $&NML NMH: $&NMh Idd: $&idd

.endc
```

## NgSpice response:

```

Experiment_1.spice" -a || sh
** Copyright 1985-1994, Regents of the University of California.
** Copyright 2001-2024, The ngspice team.
** Please get your ngspice manual from https://ngspice.sourceforge.io/docs.html
** Please file your bug-reports at http://ngspice.sourceforge.net/bugrep.html
** Creation Date: Wed Jan 22 06:35:27 UTC 2025
*****

Note: No compatibility mode selected!

Circuit: ** sch_path: /home/ee22b045/ee5311/tutorial_2/experiment_1.sch

Doing analysis at TEMP = 27.000000 and TNOM = 27.000000

Using SPARSE 1.3 as Direct Linear Solver
Reference value : 0.00000e+00
No. of Data Rows : 19
vil      = 8.166412e-01
vih      = 1.296677e+00
vth      = 1.124175e+00
idd      = -4.497300e-05
NML: 0.816641 NMH: 0.503323 Idd: -4.4973E-05
ngspice 1 -> #
ngspice 2 -> █
  
```

## Calculation:

Tutorial 2 DIC:

①  $\hookrightarrow V_{OL} = 0.1V$  ; ie when  $v_{in} = v_{DD}$   
 $\therefore V_{out} = V_{OL} = 0.1V$

$$\left(\frac{W}{L}\right)_n = \frac{0.142}{0.15}$$

$I_{Dsp} = -I_{Dsn}$

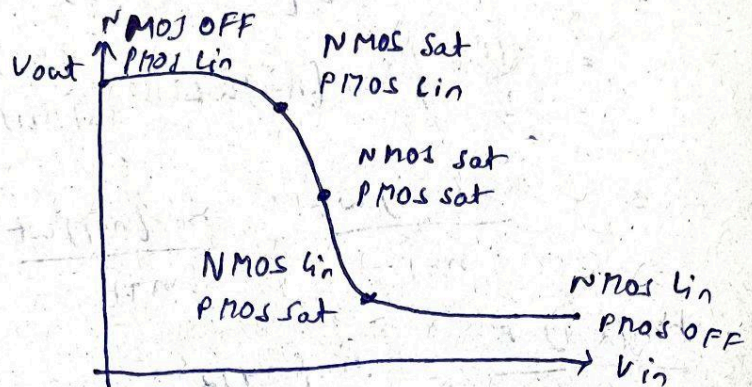
$V_{Gsn} = v_{in} ; V_{Gsp} = v_{in} - v_{DD}$

$V_{DSn} = V_{out} ; V_{Dsp} = V_{out} - v_{DD}$



@  $V_{OL}$  region NMOS is in Linear region  
and PMOS is in Saturation region

$I_{D,P}$  @

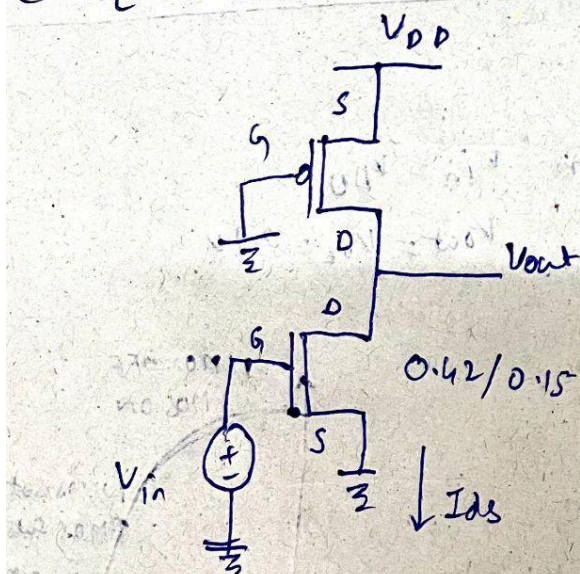


$I_{D,P}$  @ Saturation =  $I_{D,n}$  @ Linear region.

$$I_{D,P} @ \text{Saturation} = \frac{\mu_0 C_{ox}}{2} \left(\frac{W}{L}\right)_p \left[ (V_{GS,p} - V_{T,p})^2 \right] \left[ 1 + \lambda_p V_{DS,p} \right]$$

$$I_{D,n} @ \text{Linear} = \frac{\mu_0 C_{ox}}{2} \left(\frac{W}{L}\right)_n \left[ (V_{GS,n} - V_{T,n}) V_{DS,n} - \frac{V_{DS,n}^2}{2} \right]$$

@  $V_{OL} \approx 0.1 = V_{out}$



$$V_{GS,p} = -1.8V$$

$$|V_{TP}| = 0.7$$

$$V_{DS,p} = V_{out} = V_{DD} = 0.1 - 1.82 = -1.72V$$

$$V_{GS,n} = V_{in}$$

$$V_{TN} = 0.7$$

$$V_{DS,n} = V_{out} = 0.1V$$



$$I_{D,P} = \frac{(0.009)(0.00816)}{2} \left(\frac{W}{L}\right)_P \left[(-1.8+0.7)^2\right] \left[1 + (0.12)(-1.7)\right]$$

$$= (3.672 \times 10^{-5}) \times \left(\frac{W}{L}\right)_P [1.21] [0.694]$$

$$I_{D,P} = 3.083 \times 10^{-5} \times \left(\frac{W}{L}\right)_P$$

$$I_{D,n} = (0.025)(0.00835) \left(\frac{0.52}{0.15}\right) \left[ (V_{in} - 0.7)0.1 - \frac{1}{2}(0.1)^2 \right]$$

$$I_{D,n} = (5.838 \times 10^{-5}) [0.1V_{in} - 0.025]$$

if  $V_{in} = V_{DD} = 1.8V$  :  $I_{D,n} = 6.1299 \times 10^{-5} A$

$$I_{D,P} = I_{D,n}$$

$$\Rightarrow \left(\frac{W}{L}\right)_P = 1.988$$

$\omega_p = 0.298$   
 $L_P = 0.15$   $\left| \begin{array}{l} 0.894 \\ L = 0.45 \end{array} \right.$

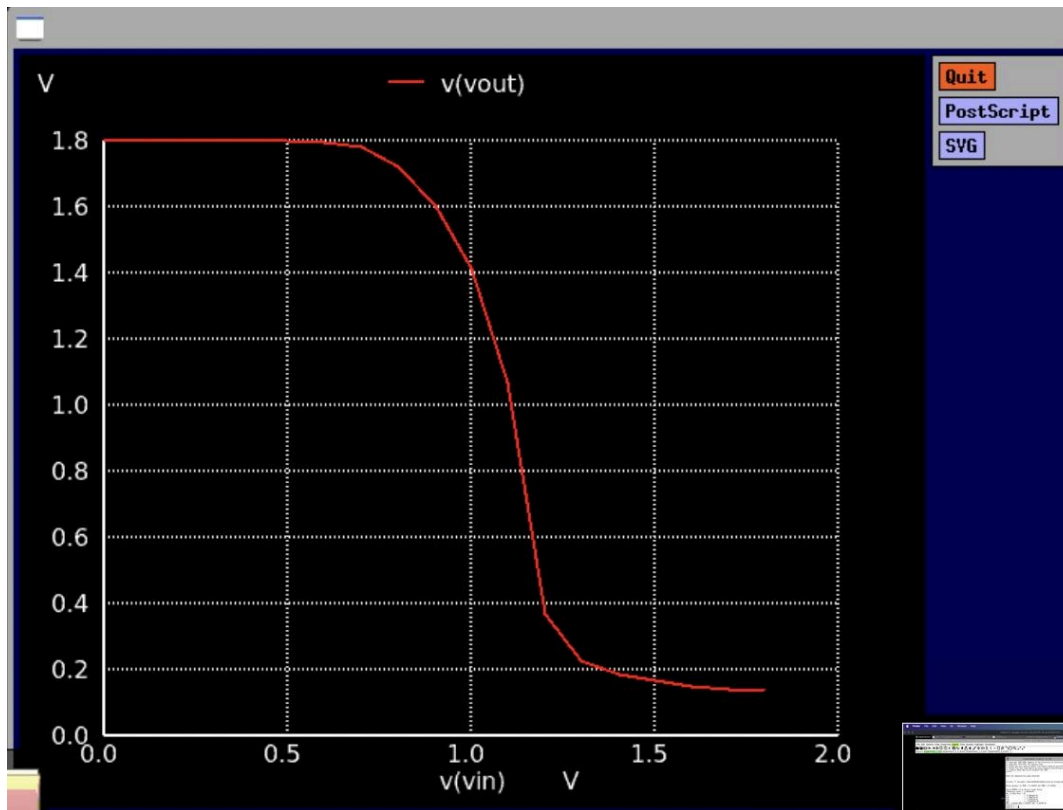
→ inverter threshold voltage from the graph @  $0.9V = \frac{V_{DD}}{2} = V_{out}$

$V_{in} = V_{TH} = 1.12V$

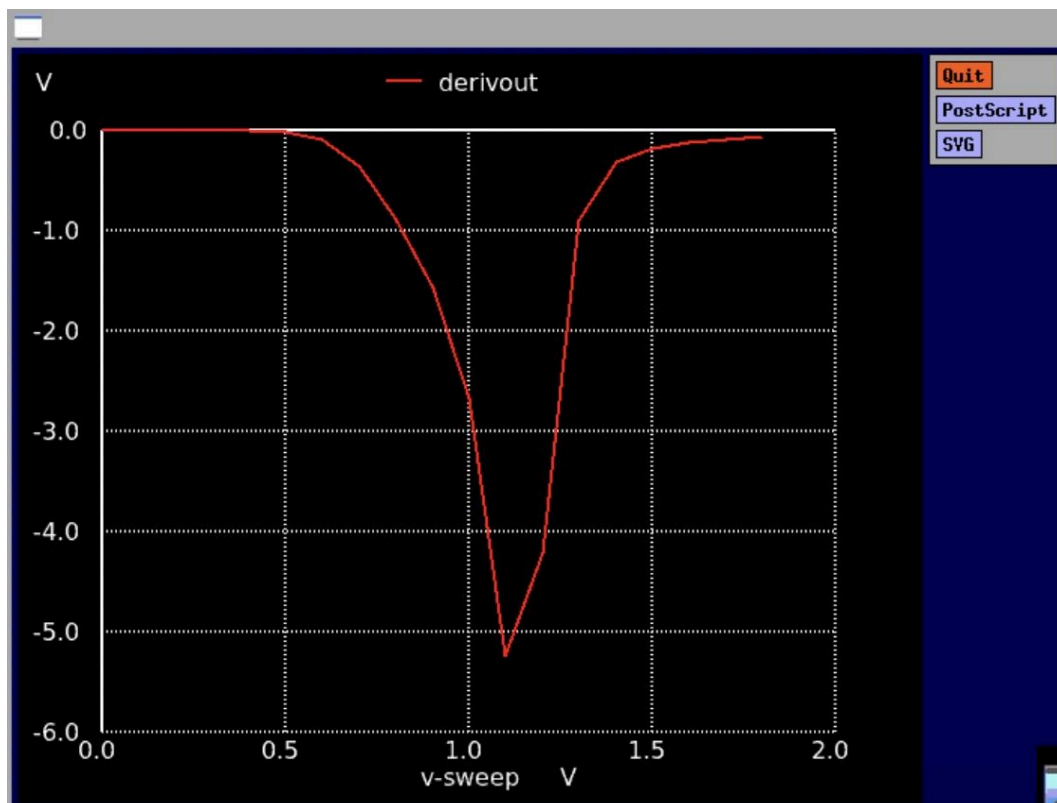
$$V_{IL} = 8.166 \times 10^{-1} = 0.816V$$

$$V_{IH} = 1.296 \times 10^0 = 1.296V$$

$$V_{TH} = 1.12V$$



Above figure shows DC characteristics graph for  $(W/L)_p = 1.988$   
 $W_p = 0.894$  ||  $L_p = 0.45$



Above Figure shows the Derivative Graph, and The Points hitting "-1" Derivates are noted through the code.

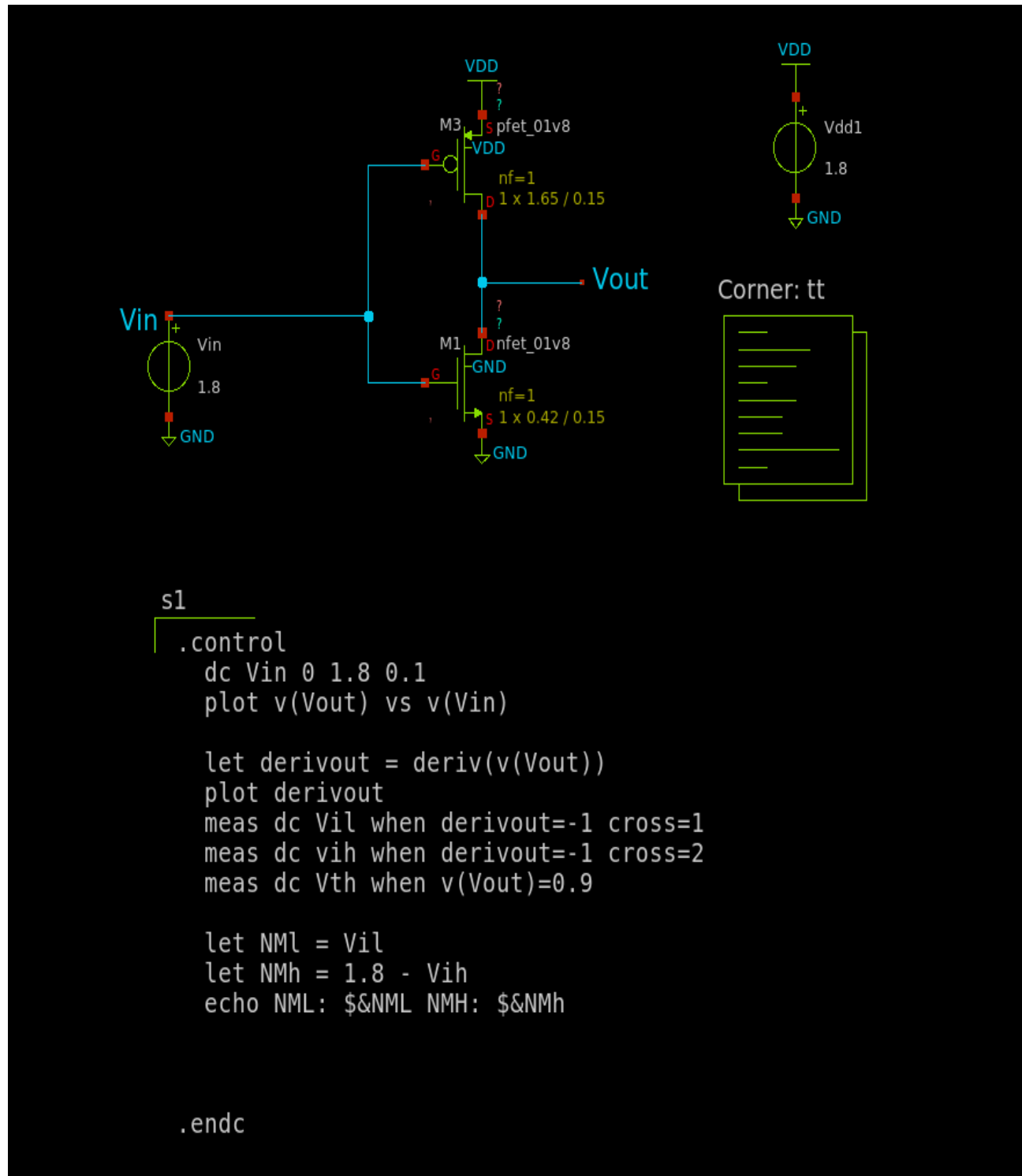
**Inverter Threshold Voltage**  $V_{th} = 1.12V$

**Average Power** =  $I_{dd} \times V_{dd}$   
=  $44.976\mu A \times 1.8V = 80\mu Watt$

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# Experiment - 2

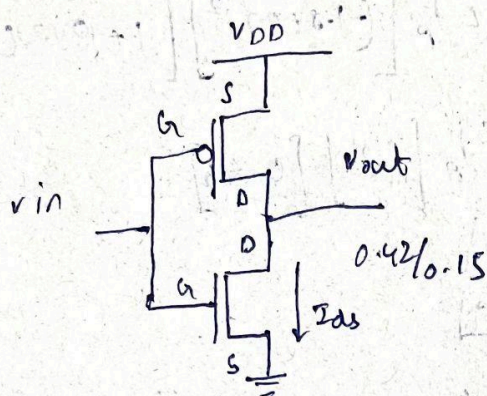
## Schematic for (A) & (B):





## Calculations:

(2)



$$V_{GS,P} = V_{in} - V_{DD} = 2 - 0.1 = 1.9$$

$$V_{TP} = 0.7$$

$$V_{DS,P} = V_{out} - V_{DD} = V_{out} - 2 = -0.9$$

$$V_{GS,N} = V_{in} = 0.9$$

$$V_{TN} = 0.7$$

$$V_{DS,N} = V_{out} = 0.9$$

$$I_{D,P} @ \text{saturation} = \frac{\mu_0 C_{ox}}{2} \left( \frac{W}{L} \right)_P \left[ (V_{GS,P} - V_{TP})^2 \right] \left[ 1 + \lambda_P V_{DS,P} \right]$$

$$I_{D,N} @ \text{saturation} = \frac{\mu_0 C_{ox}}{2} \left( \frac{W}{L} \right)_N \left[ (V_{GS,N} - V_{TN})^2 \right] \left[ 1 + \lambda_N V_{DS,N} \right]$$

Condition  $V_{in} = V_{DD}/2$  i.e. when  $V_{out} = \frac{V_{DD}}{2}$

$$V_{TH} = V_{in} = \frac{V_{DD}}{2}$$

So,  $V_{out} = 0.9 = V_{in}$

$$I_{D,P} = \frac{(0.009)(0.00816)}{2} \left( \frac{W}{L} \right)_P \left[ (0.2)^2 \right] \left[ 1 + (0.18)(-0.9) \right]$$

$$I_{D,P} = 1.23 \times 10^{-6} A \left( \frac{W}{L} \right)_P$$

$$I_{D,N} = \frac{(0.025)(0.00834)}{2} \left( \frac{0.42}{0.15} \right) \left[ (0.2)^2 \right] \left[ 1 + (0.18)(0.9) \right]$$

$$I_{D,N} = 1.356 \times 10^{-5} A$$



$$I_{D,p} \approx I_{D,N}$$

$$\Rightarrow \left( \frac{W}{L} \right)_p = 11.03 \quad \left| \quad \begin{array}{l} W_p = 1.6 \mu \\ L_p = 0.15 \mu \end{array} \right.$$

→ When  $\left( \frac{W}{L} \right)_p$  is decreased by a factor of 10 =

$$\hookrightarrow V_{TH} = 0.66V \approx 0.66V$$

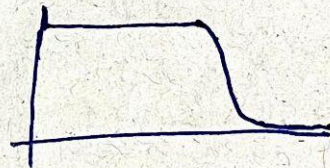
ie ; it decents faster



→ When  $\left( \frac{W}{L} \right)_p$  is increased by a factor of 10 =

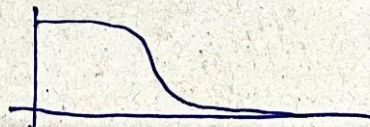
$$\hookrightarrow V_{TH} = 1.04V$$

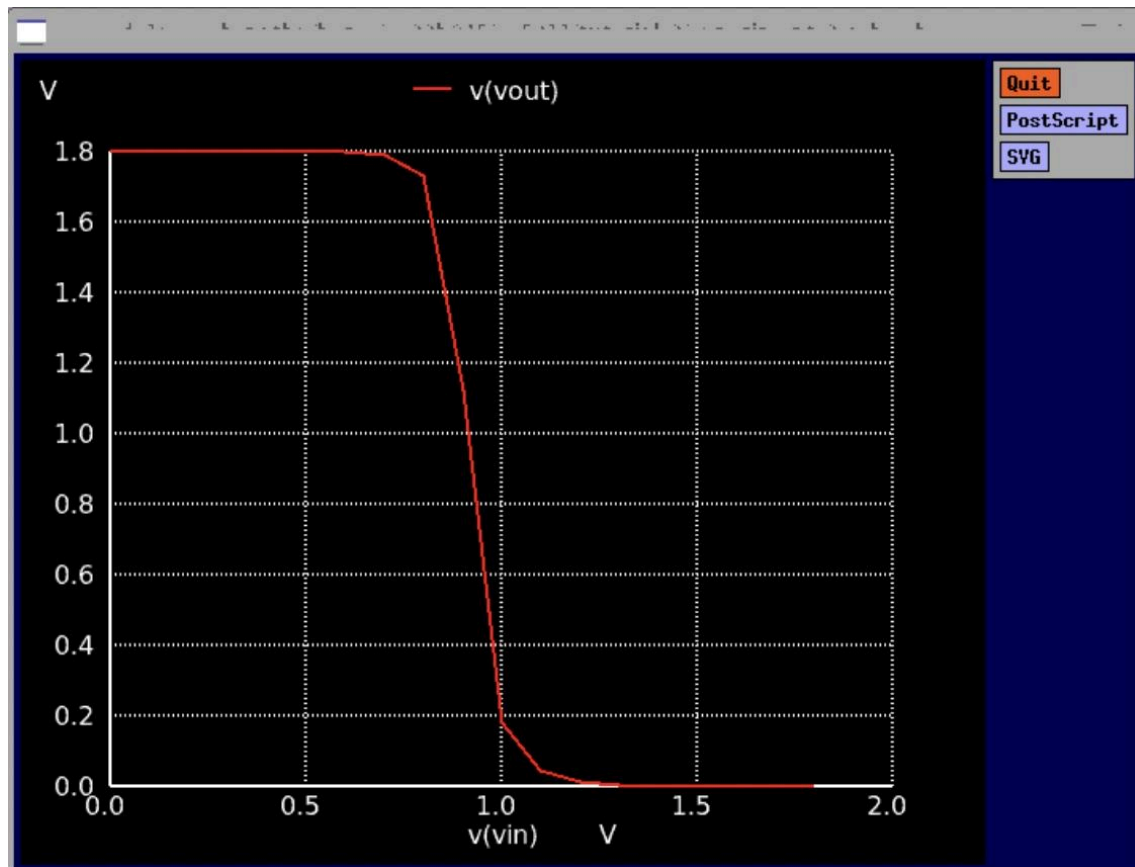
ie ; it decents later



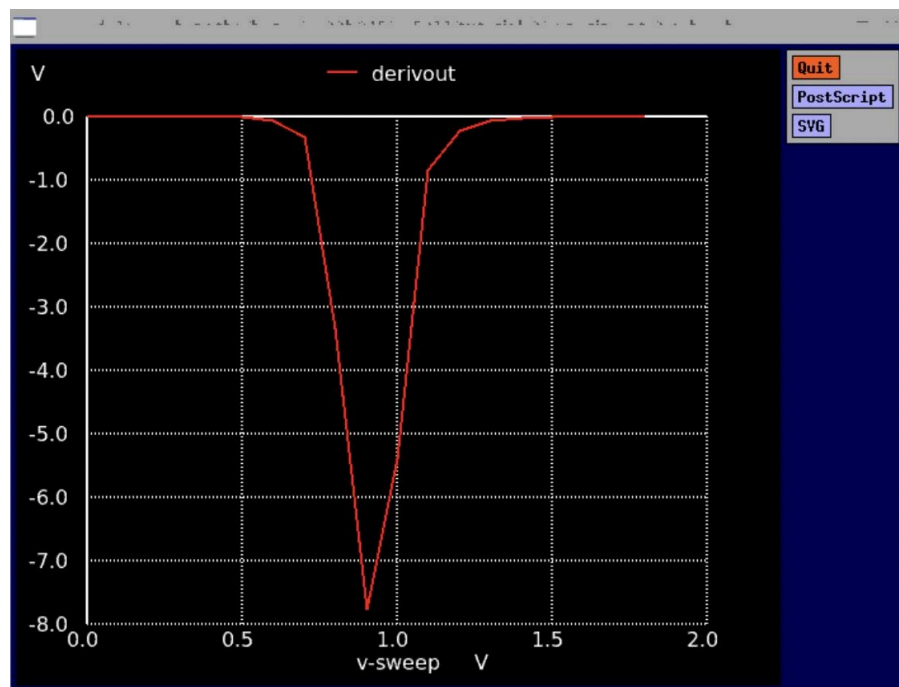
→ ideally when  $\left( \frac{W}{L} \right)_p$

$$V_{TH} = 0.92V$$





Above figure shows DC characteristics graph for  $(W/L)_p = 11.03$   
 $W_p = 1.65$  ||  $L_p = 0.15$



Above Figure shows the Derivative Graph, and The Points hitting "-1" Derivates are noted through the code.



## NgSPice Response:

```
Experiment_2_A_B.spice" -a || sh
** Compiled with KLU Direct Linear Solver
** The U. C. Berkeley CAD Group
** Copyright 1985-1994, Regents of the University of California.
** Copyright 2001-2024, The ngspice team.
** Please get your ngspice manual from https://ngspice.sourceforge.io/docs.html
** Please file your bug-reports at http://ngspice.sourceforge.net/bugrep.html
** Creation Date: Wed Jan 22 06:35:27 UTC 2025
*****

Note: No compatibility mode selected!

Circuit: ** sch_path: /home/ee22b045/ee5311/tutorial_2/experiment_2_a_b.sch

Doing analysis at TEMP = 27.000000 and TNOM = 27.000000

Using SPARSE 1.3 as Direct Linear Solver
Reference value : 0.00000e+00
No. of Data Rows : 19
vil          = 7.223556e-01
vih          = 1.096542e+00
vth          = 9.236806e-01
NML: 0.722356 NMH: 0.703458
ngspice 1 -> █
```

### **Noise Margines:**

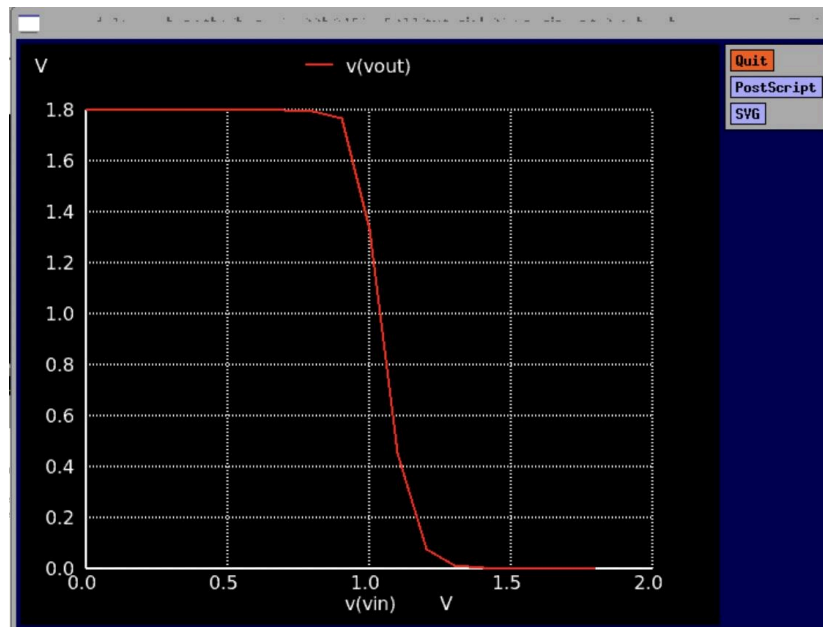
NML = 0.722V

NMH = 0.734V

DC Characteristics when W/L ratio is **Increased by 10** times:

NHL: 0.839V

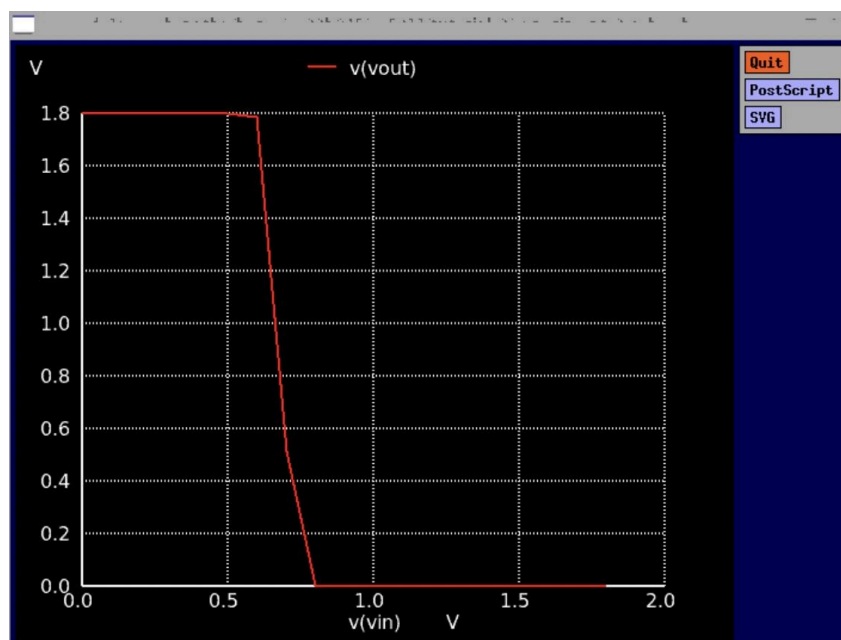
NHM: 0.534V



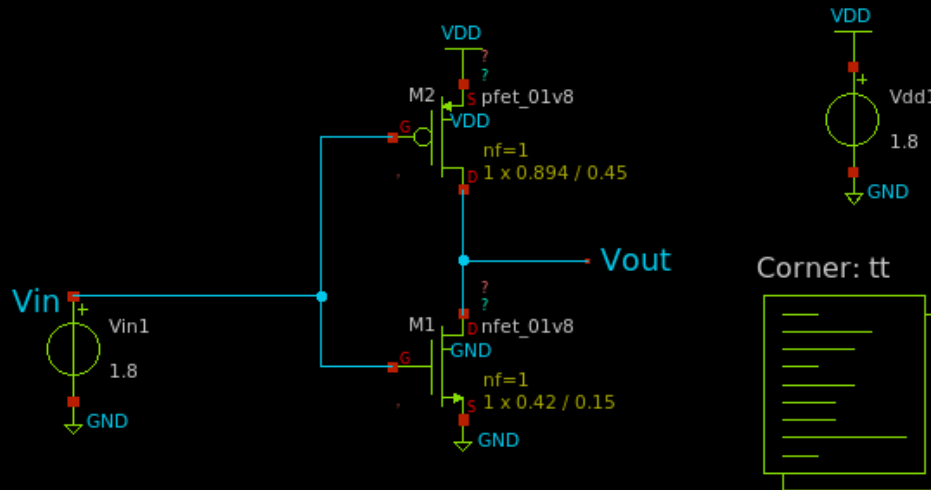
DC Characteristics when W/L ratio is **Decreased by 10** times:

NHL: 0.514V

NHM: 0.938V



## Schematic for (C):



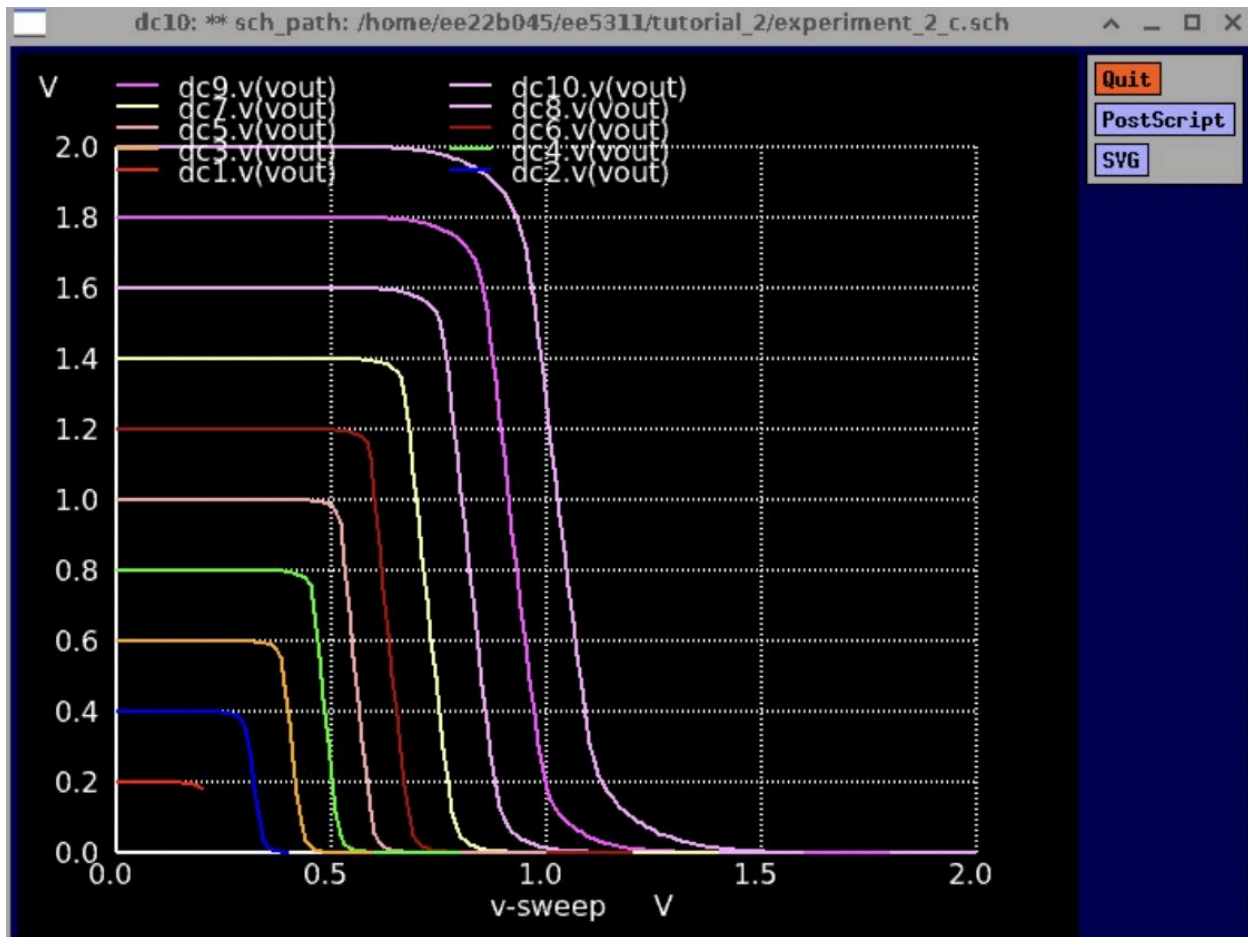
```

s1
.control
let vds = 0.2
set cache = ''
let index = 1
let N = 10
let imax = vector(N)
while index le N
    alter Vdd1 $&vds
    dc Vin1 0 $&vds 0.01
    set cache = ( $cache dc{$&index}.v(Vout) )
    let imax[index - 1] = abs(vecmin(dc{$&index}.i(Vdd1)))
    let vds = vds + 0.2
    let index = index + 1
end
plot $cache

.endc

```





For low VDD (e.g., 0.2V, 0.4V):

- The inverter does not work effectively because the MOSFETs are in the subthreshold region, leading to weak drive currents.
- $V_{thV_{th}}$  deviates from  $VDD/2$ .
- The gain (slope of the transition) is low, causing poor noise margins.

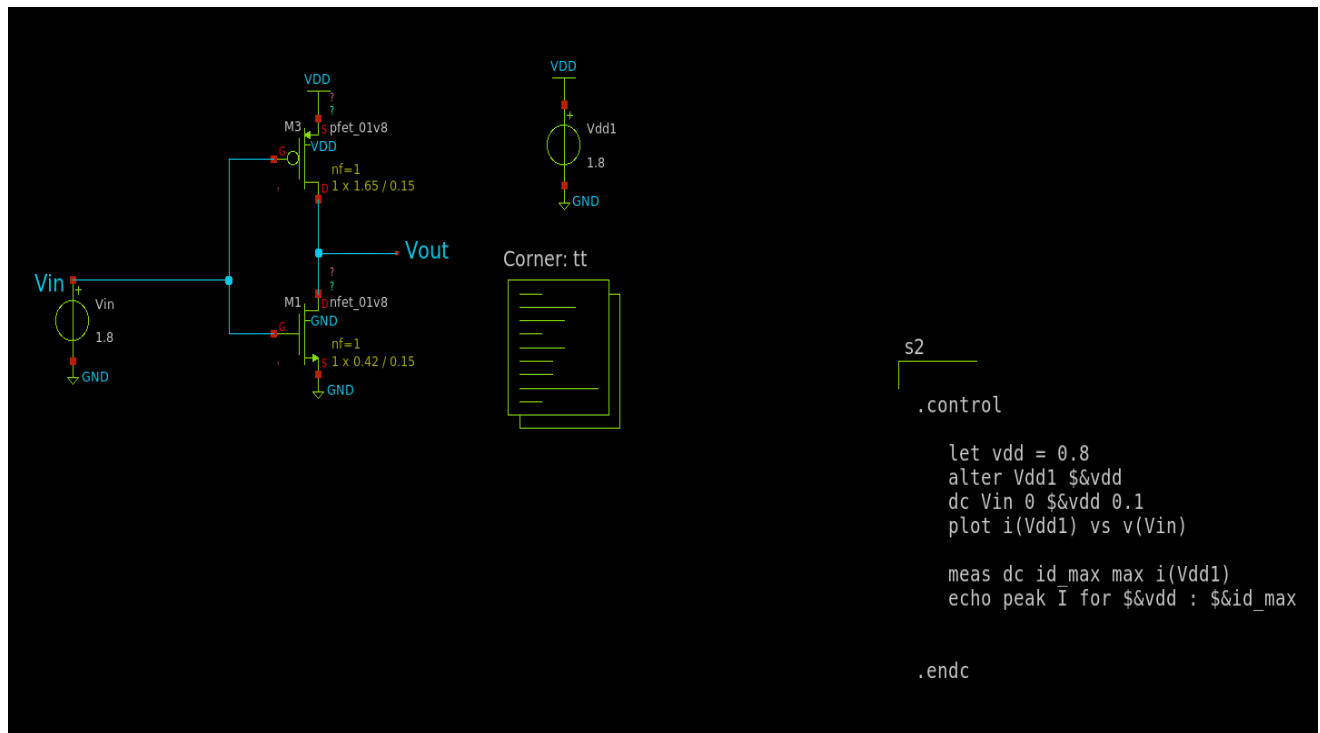
For mid-range VDD (e.g., 0.8V, 1.0V):

- The inverter functions normally.
- $V_{th} \approx VDD/2$  if  $(W/L)_p$  is properly sized.
- Noise margins are sufficient for digital logic.

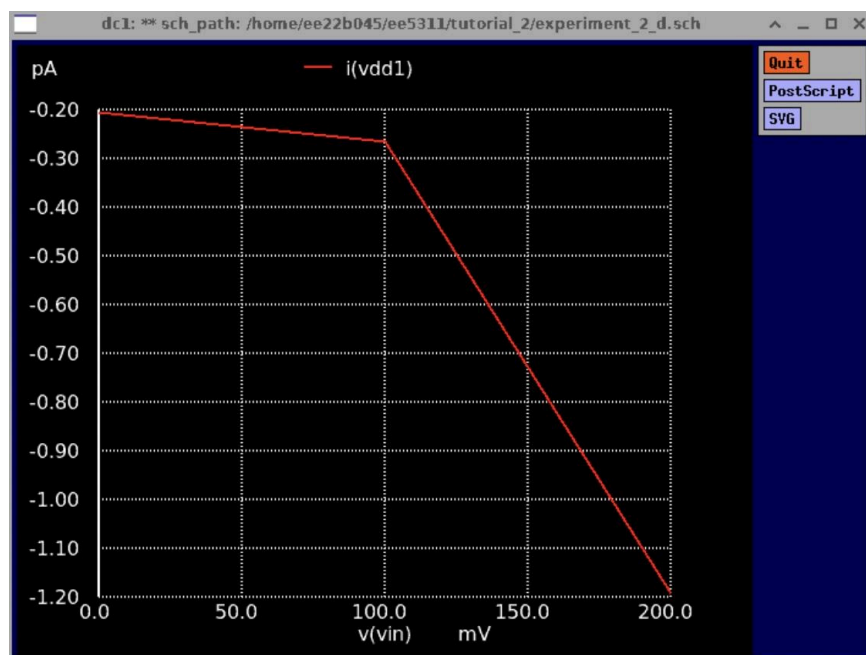
For high VDD (e.g., 1.8V):

- The transition is sharper.
- Strong drive currents improve switching speed.
- Increased noise margins.

## Schematic for (D):

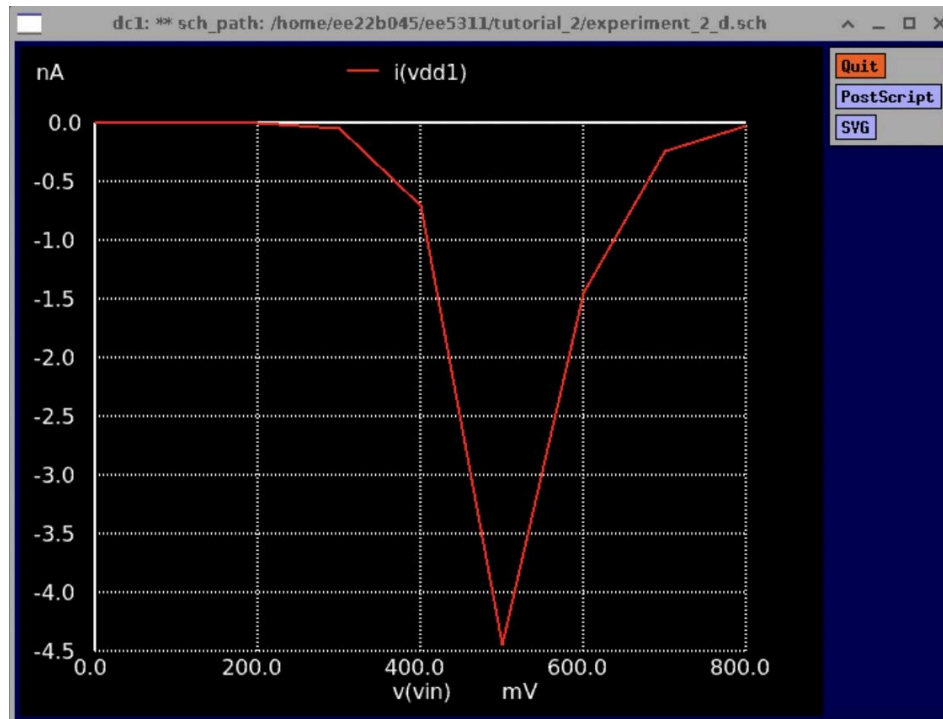


- 1)  $I_{ds}$  vs  $V_{in}$  @  $V_{dd} = 0.2V$   
 $I_{max} = -0.204pA$  (pico Amps)



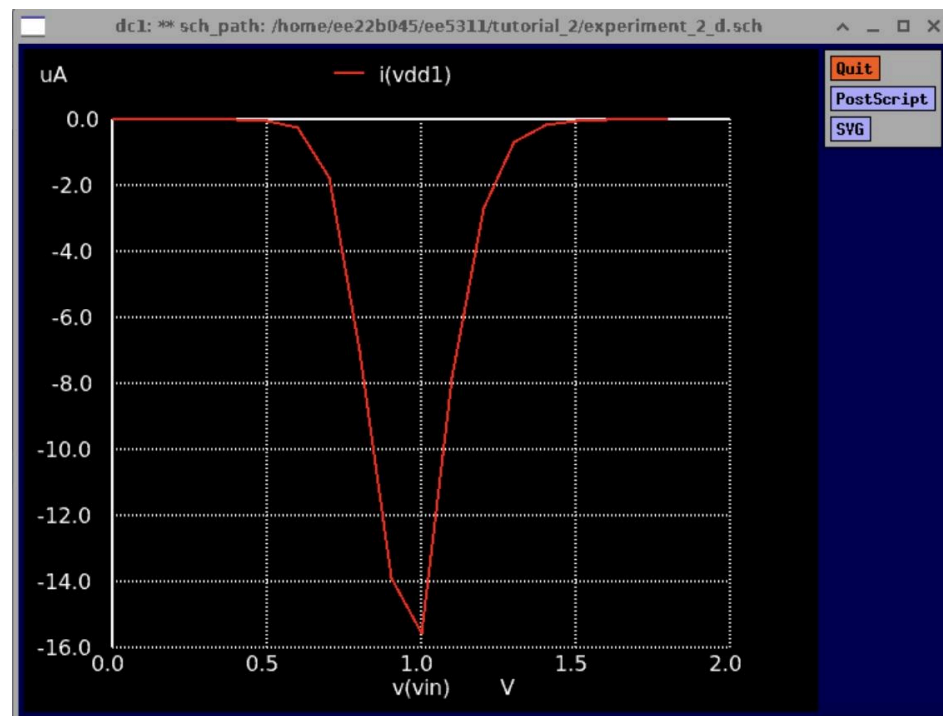
2)  $I_{ds}$  vs  $V_{in}$  @  $V_{dd} = 0.8V$

$I_{max} = -0.812nA$  (nano Amps)



3)  $I_{ds}$  vs  $V_{in}$  @  $V_{dd} = 1.8V$

$I_{max} = -1.835\mu A$  (micro Amps)





- Peak  $I_{ds}$  increases as  $V_{DD}$  increases.
- For small  $V_{DD}$ , transistors operate in the **weak inversion** region, reducing  $I_{ds}$ .
- For high  $V_{DD}$ ,  $I_{ds}$  reaches larger values, leading to **faster switching**.

- The End -

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