

Friday : Contest 2

{ Bit Manipulation, sorting, modular arithmetic, string }

Sorting : Arranging data in increasing or decreasing order based on a parameter

Cricketers

Salary

Runs

MSD

1L (3)

7000

Virat

5L (4)

10000

SKY

0.5L (1)

3000

Jadeja

1L (2)

2500

Inc

Dec

{ 3 5 7 9 10 }

Inc

based on value

{ 1, 13, 9, 6, 12 }

Inc

factors: 1 2 3 4 6

based on factors

## Algorithms

- |    |    |                |
|----|----|----------------|
| 1) | A1 | Merge sort     |
| 2) | A2 | Quick sort     |
|    | :  | Selection sort |
|    |    | :              |

Advanced

## Problem solving based on sorting

How to sort an array in your language?

	Python	C++	Java
$l =$	$l.sort()$	$sort(l, l+n)$	$Collection.sort(l)$
	↓ Inc		
	<div>TC: <math>O(N \log N)</math> SC: <math>O(1)</math></div>		

Q1) Given an array of  $N$  elements. Remove all elements from array one by one.

Cost of removing any element:

Sum of all array elements at that time (before deletion)

Return **minimum cost** of deleting all elements.

	0	1	2		0	1	2
A:	<del>2</del>	<del>1</del>	4	A:	2	1	4
Deleted 1:	$2+1+4 = 7$						
Delete 2:	$2+4 = 6$						
Delete 4:	$4 = 4$						

Total cost: 17

$\{ \cancel{2}, \cancel{1}, 1 \}$

$$\text{Del } 6: \quad 6+4+1 = 11$$

$$\text{Del } 4: \quad 4+1 = 5$$

$$\text{Del } 1: \quad 1 = 1$$

TC: 17

Remove the max element.

↓  
2<sup>nd</sup> largest  $\rightarrow$  3<sup>rd</sup> largest  $\rightarrow$  Smallest

Why?

70

$$\{ \cancel{a_0} \quad a_1 \quad a_2 \quad \cancel{a_3} \} \quad 4$$

Del  $a_0$ :  $a_0 + a_1 + a_2 + a_3$

Del  $a_1$ :  $a_1 + a_2 + a_3$

Del  $a_3$ :  $a_2 + a_3$

Del  $a_2$ :  $a_2$

$$a_0 + 2a_1 + 4a_2 + 3a_3$$

Minimize

Highest coefficient needs to be multiplied by least value

$$a_2 < a_3 < a_1 < a_0$$

Obs: Del elements in decreasing order

1<sup>st</sup> lowest element  $\times N$

2<sup>nd</sup> lowest  $\times N-1$

$\vdots$

largest  $\times 1$

l.sort() // asc order

mincost = 0

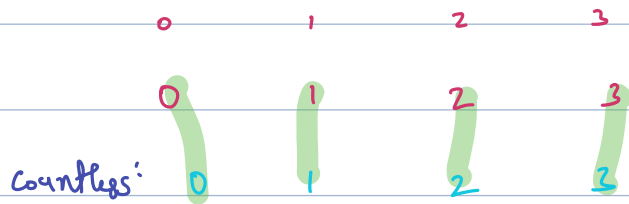
TC:  $O(N \log N + N)$

temp = N

SC:  $O(1)$

```
for (i=0; i<N; i++) {  
    mincost += temp * A[i]  
    temp --  
}
```

return mincost



Q2) Nobel integer

Given an array of size  $N$  having <sup>unique elements</sup> distinct elements. Count number of nobel integers.

Nobel integer: Any element  $A[i]$  for which  
count of elements less than it =  $A[i]$

A:	0	1	2	3	4	5
	-1	-5	3	5	-10	4
Countless	2	1	3	5	0	4

Nobel : 3

A:	0	1	2	3	4	5	6	7
	4	8	3	2	-1	1	7	6

$\{ -3, 0, 2, 5 \}$   
 countless 0 1 2 3

$\boxed{\text{nobel} = 1}$

Brute force: For every index  $i$

TC:  $O(N^2)$

count no. of  $\text{eles} < A[i]$

count ==  $A[i]$

# nobel

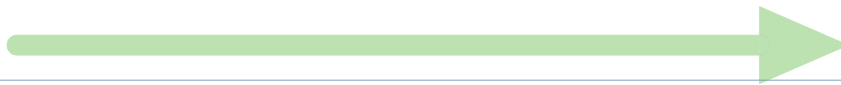
Optimised approach:

0 1 2 3 4 5 6 7  
 4 8 3 2 -1 1 7 6

sort 0 1 2 3 4 5 6 7

-1 1 2 3 4 6 7 8

countless: 0 1 2 3 4 5 6 7



$\boxed{\text{countless} = i}$

$\text{A.sort()}$  nobel = 0

TC:  $O(N \log N)$

for ( $i = 0; i < N; i++$ ) {

if ( $A[i] == i$ ) {

nobel++

}

}

Data can Repeat { ~~Nobel integers~~ }

0 1 2 3 4 5  
Ex { 0 2 2 3 3 6 }

0 1 2 3 4 5 6 7 8  
Ex: { -10 1 1 1 4 4 4 7 10 } -

	0	1	2	3	4	5	6	7	8
Ex: { -10	1	1		2	4	4	4	8	10 }
countless:	0	1	1	3	4	4	4	7	8

Ans: 5



countless:

0	1	2	3	4
-10	1	1	3	100
0	1	1	3	4

output: 3

countless:

0	1	2	3	4	5	6	7	8	9	10	11	12	13
-3	0	2	2	5	5	5	5	8	8	10	10	10	14
0	1	2	2	4	4	4	4	8	8	10	10	10	13

Ans: 7

1) Brute force remains same

2)

countless = i

✗

✓

obs 1) countless remains same for equal values

✓

2) First occurrence countless = i

A[i] is repeating or first occurrence?

→ check previous value

l.sort()

nobel = 0 , countless = 0

```
for (i = 0; i < N; i++) {  
    if (A[i] != A[i-1]) {  
        |  
        } countless = i  
        if (countless == A[i]) {  
            |  
            } nobel++  
        }  
    }  
}
```

TODO: fix this  
code

10:39 - 10:50

Q Given an array, sort the array based on number of factors?

0	1	2	3	4	5	6
9	3	4	8	16	37	63