

Decision Tree Algorithm



Agenda for Today's Session

- What is Classification?
- Types of Classification
- Classification Use case
- What is Decision Tree?
- Terminologies associated to a Decision Tree
- Visualizing a Decision Tree
- Writing a Decision Tree Classifier from Scratch in Python using CART Algorithm





What is Classification?

What is Classification?

“Classification is the process of dividing the data into different categories or groups by adding labels.”

- **Note:** It adds the data point to a particular labelled group on the basis of some condition”

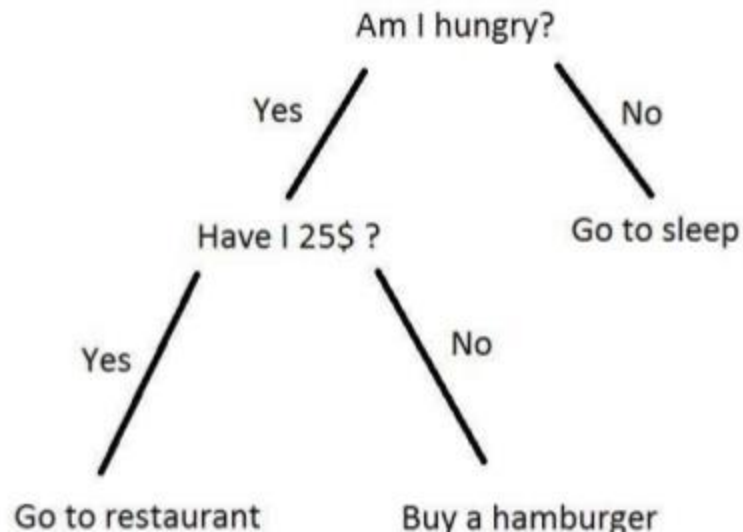


Types of Classification

- ☒ Decision Tree
- ☐ Random Forest
- ☐ Naïve Bayes
- ☐ KNN

Decision Tree

- Graphical representation of all the possible solutions to a decision
- Decisions are based on some conditions
- Decision made can be easily explained



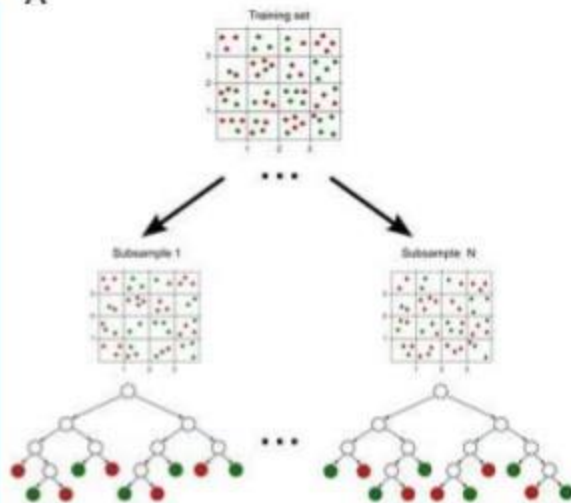
Types of Classification

- Decision Tree
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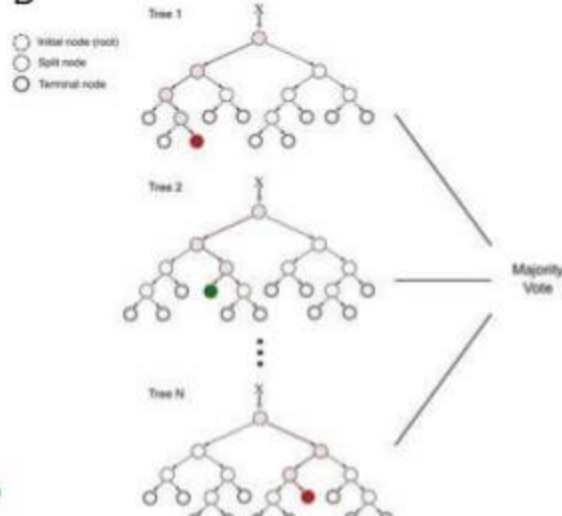
Random Forest

- Builds multiple decision trees and merges them together
- More accurate and stable prediction
- Random decision forests correct for decision trees' habit of overfitting to their training set
- Trained with the “bagging” method

A



B

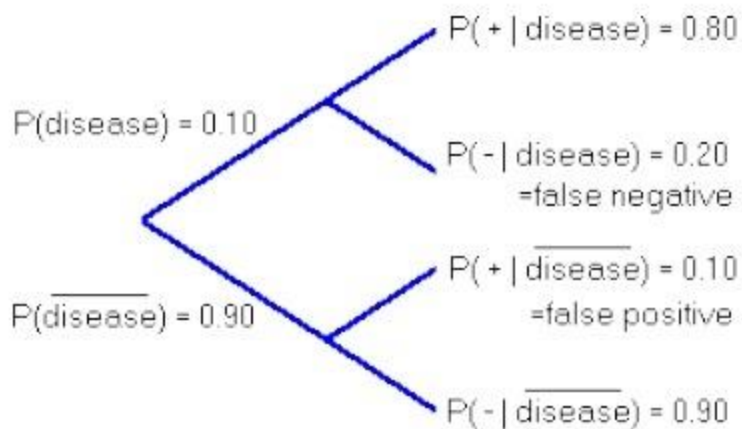


Types of Classification

- Decision Tree
- Random Forest
- Naïve Bayes**
- KNN

Naïve Bayes

- Classification technique based on Bayes' Theorem
- Assumes that the presence of a particular feature in a class is unrelated to the presence of any other feature



Types of Classification

- Decision Tree
- Random Forest
- Naïve Bayes
- KNN**

K-Nearest Neighbors

- Stores all the available cases and classifies new cases based on a similarity measure
- The “K” is KNN algorithm is the nearest neighbors we will take vote from.



K = 1



K = 3



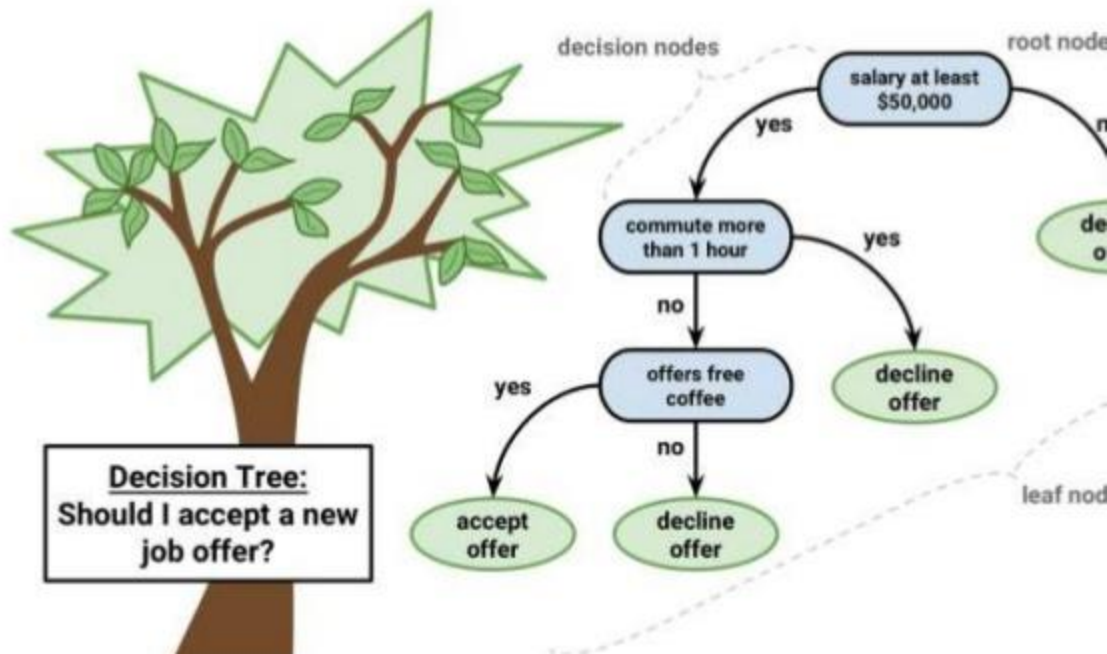
K = 5



What is Decision Tree?

"A decision tree is a graphical representation of the possible solutions to a decision based on certain conditions"

What is Decision Tree?



Understanding a Decision Tree

Dataset

This is how our dataset looks like!

Colour	Diameter	Label
Green	3	Mango
Yellow	3	Mango
Red	1	Grape
Red	1	Grape
Yellow	3	Lemon

Decision Tree

Gini Impurity = 0

Information Gain = 0.37

Gini Impurit

Info
Gain

100% Mango

```
is colour == Yellow
```

50% M
50% Le

What is Decision Tree?

Green	3	Mango
Yellow	3	Lemon
Yellow	3	Mango

Is the colour green?

Is the diameter ≥ 3

Is the colour yellow

TRUE

False

Decision Tree Terminologies

Decision Tree Terminology

Pruning

Opposite of Splitting, basically removing unwanted branches from the tree

Branch/SubTree

Formed by splitting the tree/node

Parent/Child Node

Root node is the parent node and all the other nodes branched from it is known as child node

Splitting

Splitting is dividing the root node/su node into different parts on the basis of some condition.

Root Node

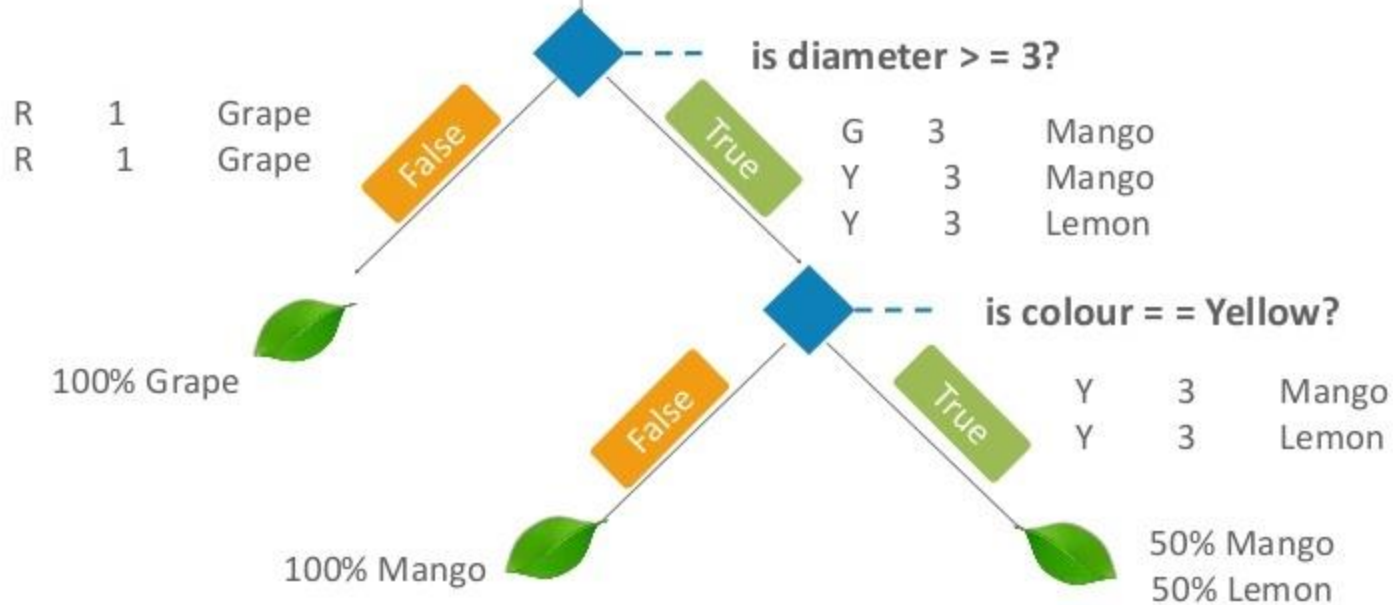
It represents the entire population or sample and this further gets divided into two or more homogenous sets.

Leaf Node

Node cannot be further segregated into further nodes



Color	Diam	Label
Green	3	Mango
Yellow	3	Lemon
Red	1	Grape
Yellow	3	Mango
Red	1	Grape



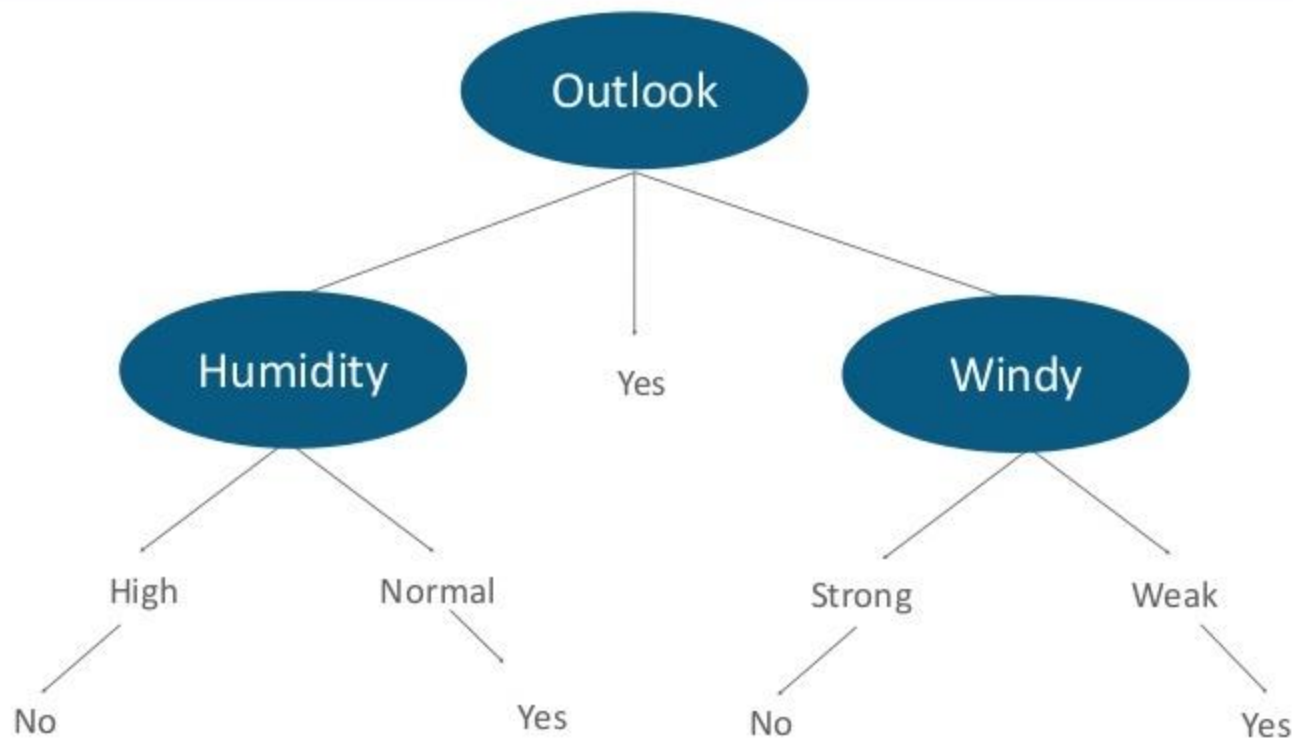
CART Algorithm

Let's First Visualize the Decision Tree

Which Question to ask and When?



Let's First Visualize the Decision Tree



Learn about Decision Tree

Which one among them
should you pick first?

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Learn about Decision Tree

Answer: Determine the attribute that best classifies the training data

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Learn about Decision Tree

But How do we choose
the best attribute?

Or

How does a tree decide
where to split?

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

How Does A Tree Decide Where To Split?

Gini Index

The measure of impurity (or purity) used in building decision tree in CART is Gini Index

Chi Square

It is an algorithm to find out the statistical significance between the differences between sub-nodes and parent node



Information Gain

The information gain is the decrease in entropy after a dataset is split on the basis of an attribute. Constructing a decision tree is all about finding attribute that returns the highest information gain

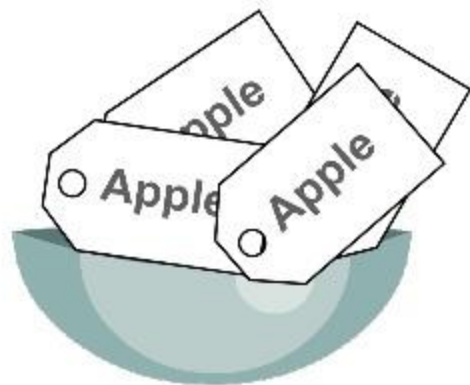
Reduction in Variance

Reduction in variance is an algorithm used for continuous target variables (regression problems). The split with lower variance is selected as the criteria to split the population

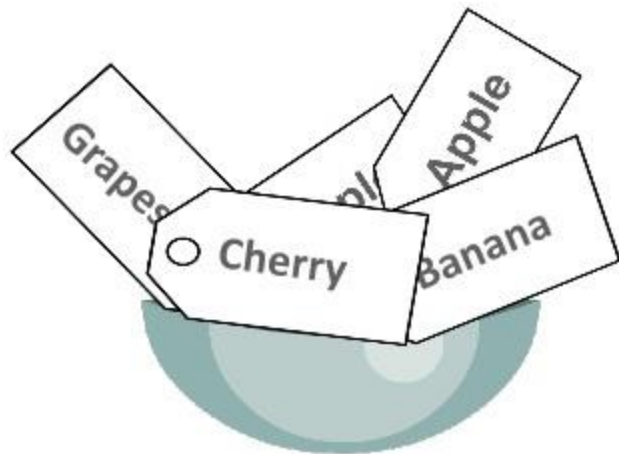
Let's First Understand What is Impurity



Impurity = 0



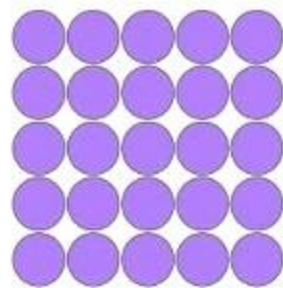
Let's First Understand What is Impurity



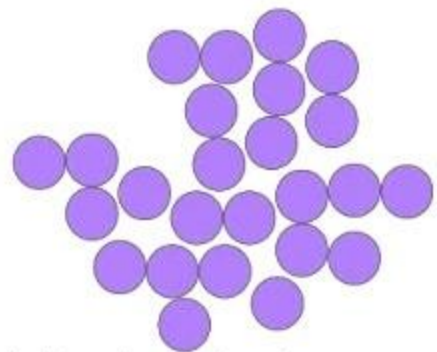
Impurity $\neq 0$

- Defines randomness in the data
- **Entropy** is just a metric which measures the impurity or
- The first step to solve the problem of a decision tree

What is Entropy?

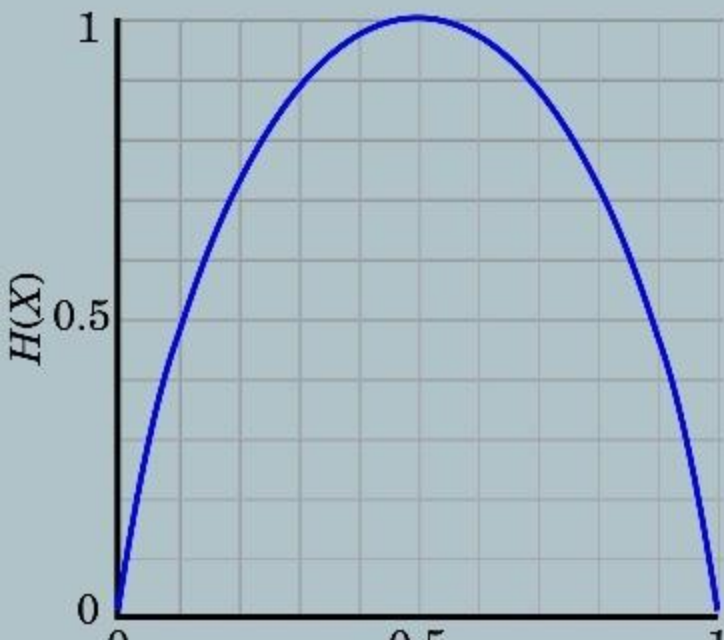


Low Entropy



High Entropy

What is Entropy?



$$\text{Entropy}(s) = -P(\text{yes}) \log_2 P(\text{yes}) - P(\text{no}) \log_2 P(\text{no})$$

Where,

- S is the total sample space,
- $P(\text{yes})$ is probability of yes

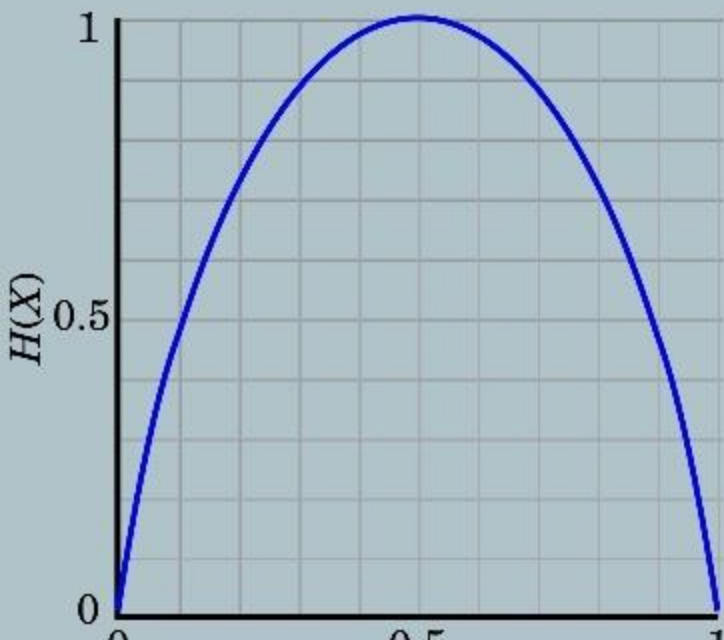
If number of yes = number of no ie $P(S) = 0.5$

$$\Rightarrow \text{Entropy}(s) = 1$$

If it contains all yes or all no ie $P(S) = 1$ or 0

$$\Rightarrow \text{Entropy}(s) = 0$$

What is Entropy?



$$E(S) = -P(\text{Yes}) \log_2 P(\text{Yes})$$

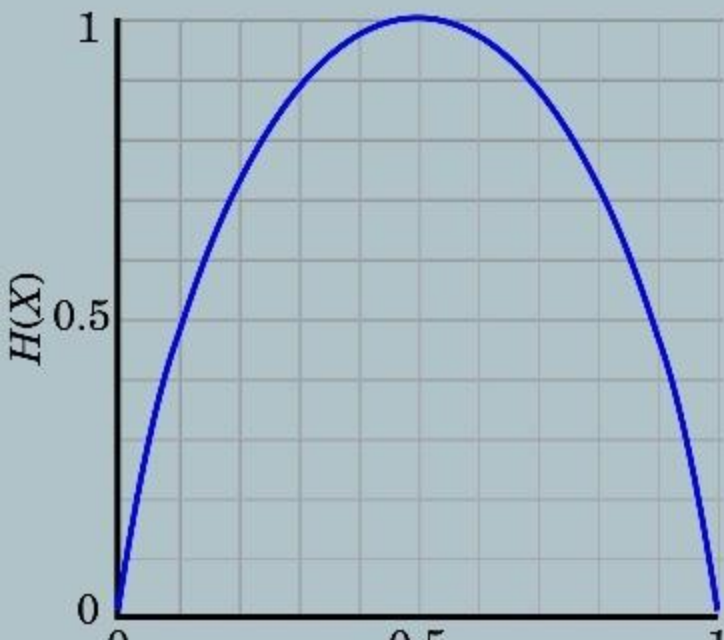
When $P(\text{Yes}) = P(\text{No}) = 0.5$ ie YES + NO = Total Sample(S)

$$E(S) = 0.5 \log_2 0.5 - 0.5 \log_2 0.5$$

$$E(S) = 0.5(\log_2 0.5 - \log_2 0.5)$$

$$E(S) = 1$$

What is Entropy?



$$E(S) = -P(\text{Yes}) \log_2 P(\text{Yes})$$

When $P(\text{Yes}) = 1$ ie YES = Total Sample(S)

$$E(S) = 1 \log_2 1$$

$$E(S) = 0$$

$$E(S) = -P(\text{No}) \log_2 P(\text{No})$$

When $P(\text{No}) = 1$ ie No = Total Sample(S)

$$E(S) = 1 \log_2 1$$

$$E(S) = 0$$

What is Information Gain?

- Measures the reduction in entropy
- Decides which attribute should be selected as the decision node

If S is our total collection,

Information Gain = Entropy(S) – [(Weighted Avg) x Entropy(each feature)]

Let's Build Our Decision Tree

Step 1: Compute the entropy for the Data set

Out of 14 instances we have 9 YES and 5 NO

So we have the formula,

$$E(S) = -P(\text{Yes}) \log_2 P(\text{Yes}) - P(\text{No}) \log_2 P(\text{No})$$

$$E(S) = - (9/14) * \log_2 9/14 - (5/14) * \log_2 5/14$$

$$E(S) = 0.41 + 0.53 = 0.94$$

	outlook	temp.	humidity	windy	play
D1	sunny	hot	high	false	no
D2	sunny	hot	high	true	no
D3	overcast	hot	high	false	yes
D4	rainy	mild	high	false	yes
D5	rainy	cool	normal	false	yes
D6	rainy	cool	normal	true	no
D7	overcast	cool	normal	true	yes
D8	sunny	mild	high	false	no
D9	sunny	cool	normal	false	yes
D10	rainy	mild	normal	false	yes
D11	sunny	mild	normal	true	yes
D12	overcast	mild	high	true	yes
D13	overcast	hot	normal	false	yes
D14	rainy	mild	high	true	no

Which Node To Select As Root Node?

Outlook?

Temperature?

Humidity?

Windy?

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Which Node To Select As Root Node: Outlook



outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Which Node To Select As Root Node: Outlook

$$E(\text{Outlook} = \text{Sunny}) = -2/5 \log_2 2/5 - 3/5 \log_2 3/5 = 0.971$$

$$E(\text{Outlook} = \text{Overcast}) = -1 \log_2 1 - 0 \log_2 0 = 0$$

$$E(\text{Outlook} = \text{Sunny}) = -3/5 \log_2 3/5 - 2/5 \log_2 2/5 = 0.971$$

Information from outlook,

$$I(\text{Outlook}) = 5/14 \times 0.971 + 4/14 \times 0 + 5/14 \times 0.971 = 0.693$$

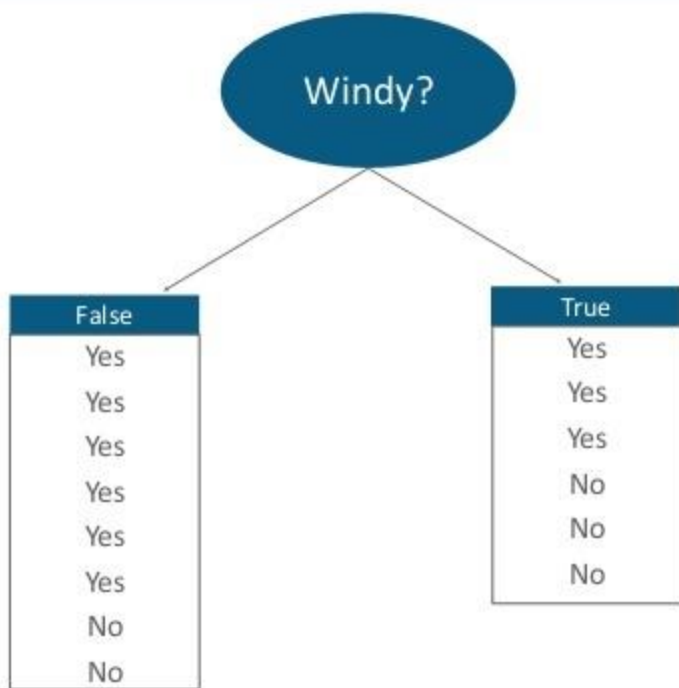
Information gained from outlook,

$$\text{Gain}(\text{Outlook}) = E(S) - I(\text{Outlook})$$

$$0.94 - 0.693 = 0.247$$

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Which Node To Select As Root Node: Outlook



outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Which Node To Select As Root Node: Windy

$$E(\text{Windy} = \text{True}) = 1$$

$$E(\text{Windy} = \text{False}) = 0.811$$

Information from windy,

$$I(\text{Windy}) = 8/14 \times 0.811 + 6/14 \times 1 = 0.892$$

Information gained from outlook,

$$\text{Gain}(\text{Windy}) = E(S) - I(\text{Windy})$$

$$0.94 - 0.892 = 0.048$$

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Similarly We Calculated For Rest Two

Which Node To Select As Root Node

Outlook:

Info

Gain: 0.940-0.693

0.693

0.247

Temperature:

Info

Gain: 0.940-0.911

0.911

0.029

Humidity:

Info

Gain: 0.940-0.788

0.788

0.152

Windy:

Info

Gain: 0.940-0.982

0.892

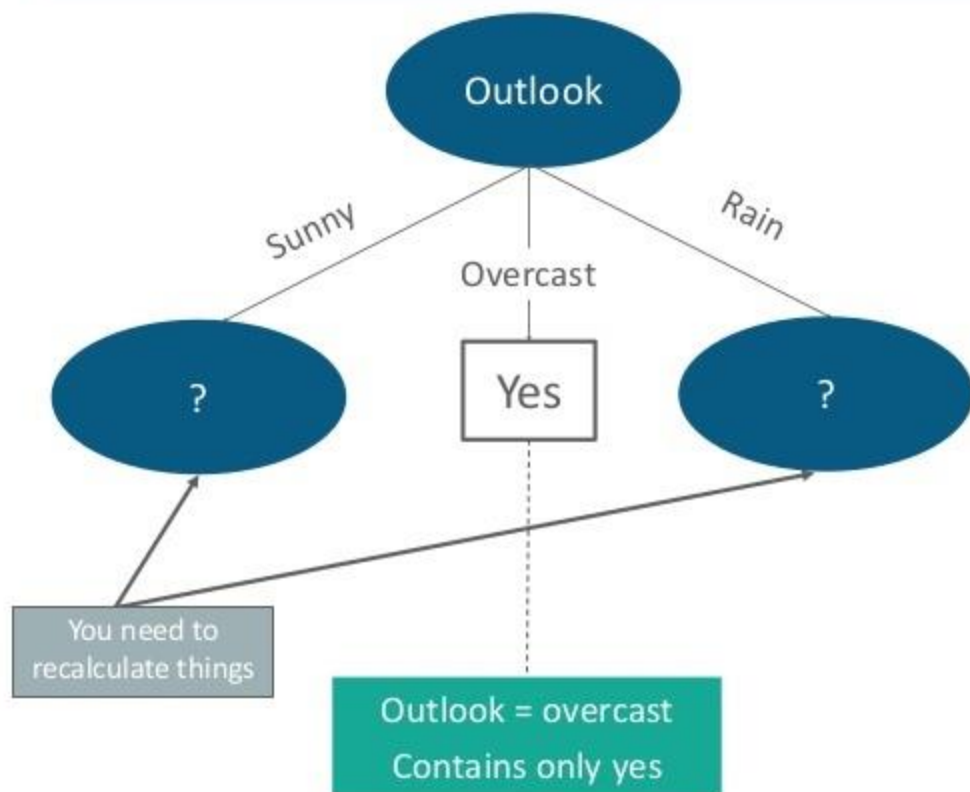
0.048

Since Max gain = 0.247,

Outlook is our ROOT Node

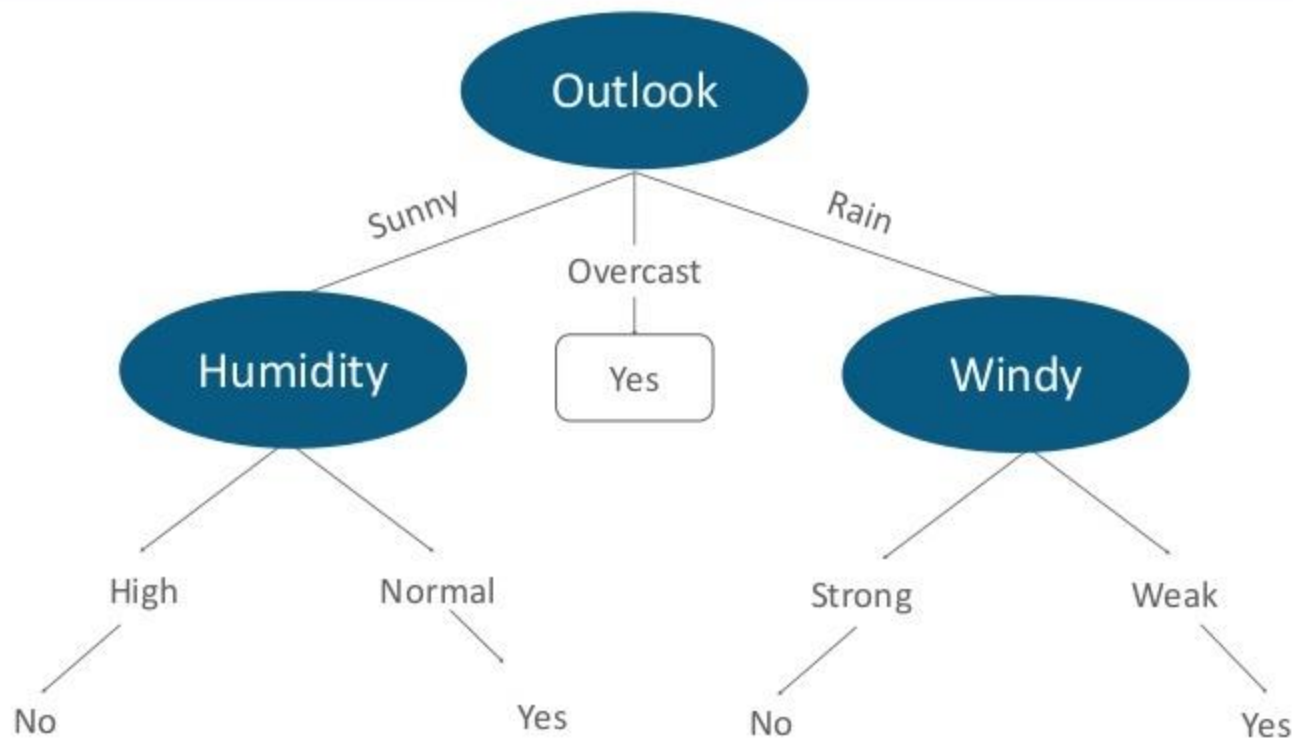
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sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

Which Node To Select Further?



outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

This Is How Your Complete Tree Will Look Like



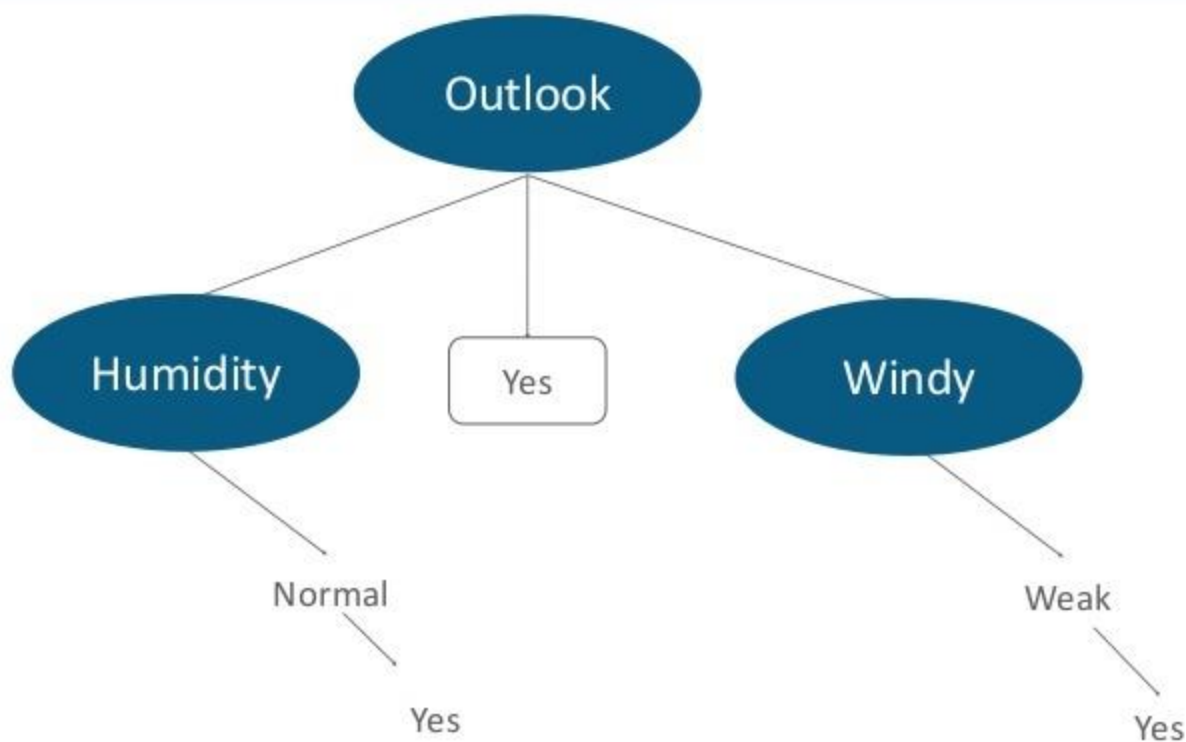
What Should I Do To Play - Pruning

“A decision tree is a graphical representation of the possible solutions to a decision based on certain conditions”

What is Pruning?



Pruning: Reducing The Complexity

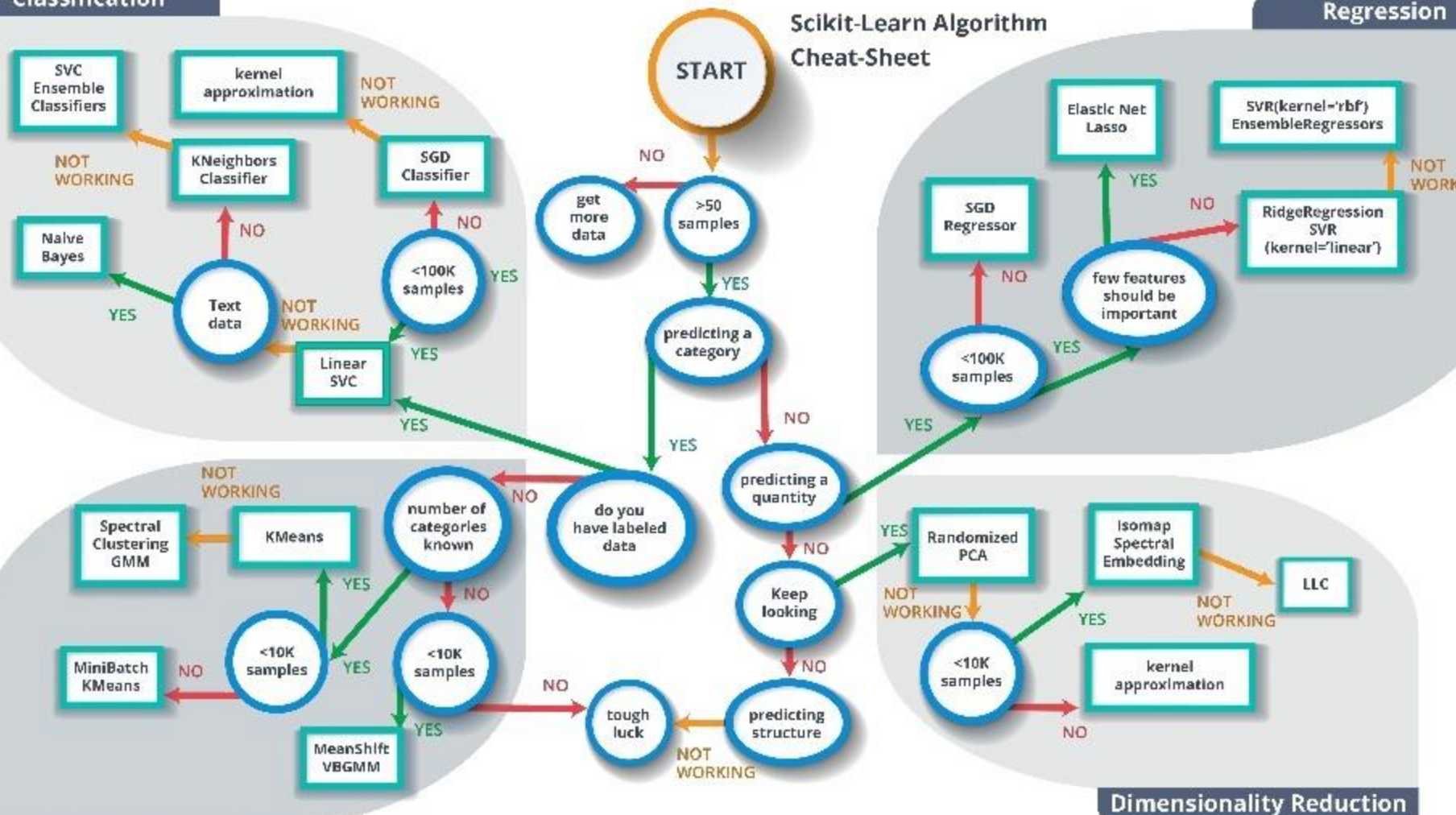


**Are tree based models better than
linear models?**

Classification

Scikit-Learn Algorithm Cheat-Sheet

Regression



edureka!