

Tutorial - 3

```

1. Int LinearSearch(int Arr[], int n, int key)
   for (int i=0; i<n; i++)
   {
       if (Arr[i] == key)
           return i;
   }
   return -1;

```

2. Iterative insertion sort

```

Void Insertionsort(int Arr[], int n)
{
    int i, j, t=0;
    for (i=1; i<n; i++) {
        t = Arr[i];
        j = i-1;
        while (j >= 0 && t < Arr[j])
        {
            Arr[j+1] = Arr[j];
            j--;
        }
        Arr[j+1] = t;
    }
}

```

Recursive insertion Sort.

```

Void Insertionsort(int Arr[], int n)
{
    if (n <= 1)
        return;

```

```

    Insertionsort(Arr, n-1);

```

```

    int last = Arr[n-1];

```

```

    j = n-2;

```

```

    while (j >= 0 && Arr[j] > last) {

```

```

        Arr[j+1] = Arr[j];

```

```

        j--; }
    Arr[j+1] = last;
}

```

Insertion Sort is called online Sorting because it does not need to know anything about what value it will sort and the information is requested while the algorithm is running.

3 (i) Bubble Sort:-

Time Complexity:- Best Case = $O(n^2)$
Worst Case = $O(n^2)$

Space Complexity = $O(1)$

(ii) Selection Sort:-

Time Complexity:- Best Case = $O(n^2)$
Worst Case = $O(n^2)$

Space Complexity = $O(1)$

(iii) Merge Sort:-

Time Complexity:- Best Case = $O(n \log n)$
Worst Case = $O(n \log n)$

Space Complexity = $O(n)$

(iv) Insertion Sort:-

Time Complexity:- Best Case = $O(n)$
Worst Case = $O(n^2)$

Space Complexity = $O(1)$

(v) Quick Sort:-

Time Complexity:- Best Case = $O(n \log n)$
Worst Case = $O(n^2)$

Space Complexity = $O(n)$

③ ① $\text{key} \leftarrow 3$

5	1	3	2	6
0	1	2	3	4

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(vi) Heap Sort:-

Time Complexity: Best Case = $O(n \log n)$

Worst Case = $O(n \log n)$

Space Complexity = $O(1)$

(4) Sorting Algo	inplace	Stable	Online
Selection	✓		
Insertion	✓	✓	✓
Merge		✓	
Quick	✓		
Heap	✓		
Bubble	✓	✓	

(5). Iterative Binary Search:-

```

int Binary Search (int Arr[], int l, int r, int key)
{
    while (l <= r)
    {
        (m) → int m = (l+r) / 2;
        if (Arr[m] == key)
            return m;
        if (Arr[m] < key) // Right side search
            l = m+1;
        else
            r = m-1;
    }
    return -1; // Not found case.
}

```

Note: Time Complexity: ① Best Case = $O(1)$
 ② Avg. Case = $O(\log n)$
 ③ Worst Case = $O(\log n)$

Recursive Binary Search:-

```

int BinarySearch (int Arr[], int l, int r, int key)
{
    if (r >= l)
    {
        int m = (l+r) / 2;
        if (Arr[m] == key)
            return m;
        else if (Arr[m] > key)
            return BinarySearch (Arr, l, mid-1, key);
        else
            return BinarySearch (Arr, mid+1, r, key);
    }
    return -1;
}

```

T.C :- Best Case = $O(1)$
 Worst Case = $O(\log n)$
 Avg. Case = $O(\log n)$

Linear Search T.C :-

Best Case = $O(1)$
 Avg. Case = $O(n)$
 Worst Case = $O(n)$

(16) Recurrence relation for binary recursive search:-

$$T(n) = T(n/2) + 1$$

7. $A[i] \neq A[j] = K$

(8). Quick Sort is the fastest general purpose sort. In most practical situations, quick sort is the method of choice. If stability is important & space is available, merge sort might be best.

9. Inversion Count for an array indicates - how far (or close) the array is from being sorted. If the array is already sorted, then the inversion count is 0, but if the array is sorted in the reverse order, the inversion count is the maximum.

Arr[] = { 7, 21, 31, 8, 10, 1, 20, 6, 4, 5 }

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
int mergeSort(int Arr[], int temp[], int left, int right)
```

```
{ int merge(int Arr[], int temp[], int left, int mid, int right)
```

```
{ int mergeSort(int Arr[], int ArrSize)
```

```
{ int temp [ ArrSize];
```

```
return mergeSort(Arr, temp, 0, ArrSize - 1);
```

```
} int mergeSort(int Arr[], int temp[], int left, int right)
```

```
{ int mid, invCount = 0;
```

```
if (right > left) {
```

```
mid = left + (right - left) / 2;
```

```
invCount += mergeSort(Arr, temp, left, mid);
```

```
invCount += mergeSort(Arr, temp, mid + 1, right);
```

```
invCount += merge(Arr, temp, left, mid + 1, right);
```

```
} return invCount;
```

```

int merge (int Arr[], int temp[], int left, int mid,
           int right)
{
    int i, j, k, invCount = 0;
    i = left;
    j = mid;
    k = left;
    while ( (i <= mid-1) && (j <= right) ) {
        if ( Arr[i] <= Arr[j] )
            temp[k++] = Arr[i++];
        else {
            temp[k++] = Arr[j++];
            invCount = invCount + (mid - i);
        }
    }
    while ( i <= mid-1 )
        temp[k++] = Arr[i++];
    while ( j <= right )
        temp[k++] = Arr[j++];
    for ( i = left; j <= right; i++)
        Arr[i] = temp[i];
    return invCount;
}

```

```

int main() {
    int Arr[] = {7, 21, 57, 8, 10, 1, 20, 6, 4, 5};
    int n = sizeof(Arr) / sizeof(Arr[0]);
    int ans = mergesort(Arr, n);
    cout << "no of inversion arr" << ans;
    return 0;
}

```


10. The worst case time complexity of quick sort is $O(n^2)$. The worst case occurs when the picked pivot is always an extreme (smallest or largest) element. This happens when input array is sorted or reverse sorted and either first or last element is picked as pivot. The best case of quick sort is when we will select pivot as a mean element.

11. Recurrence relation of:

(a) Merge Sort: $T(n) \Rightarrow 2T(n/2) + n$

(b) Quick Sort: $T(n) \Rightarrow 2T(n/2) + n$

Merge sort is more efficient & works faster than quick sort in case of larger array size or dataset.

Worst Case complexity for quick sort is $O(n^2)$ whereas $O(n \log n)$ for merge sort.

(12) Stable Selection Sort \rightarrow

```

Void StableSelectionSort(int Arr[], int n)
{
    for (int i = 0; i < n-1; i++) {
        int min = i;
        for (int j = i+1; j < n; j++) {
            if (Arr[min] > Arr[j])
                min = j;
        }
        int key = Arr[min];
        while (min > i) {
            Arr[min] = Arr[min-1];
            min--;
        }
        Arr[i] = key;
    }
}
    
```

```

int main()
{
    int Arr[] = {4, 5, 3, 2, 4, 1};
    int n = sizeof(Arr) / sizeof(Arr[0]);
    StableSelectionSort(Arr, n);
    for (int i = 0; i < n; i++)
        cout << Arr[i] << " ";
    cout << endl;
    return 0;
}

```

13. The easiest way to do this is to use external sorting. We divide our source file into temporary files of size equal to the size of the RAM & first sort these files.

External Sorting: - If the input data is such that it cannot be adjusted in the memory entirely at once it ^{needs to be} sorted in a hard disk, floppy disk or any other storage device. This is called external sorting.

Internal Sorting: - If the input data is such that it can be adjusted in the main memory at once it is called internal sorting.