PRINCIPAL COMPONENT ANALYSIS

PCA is one of the old and most important dimensionality reduction technique which is based on idea called variance maximisation based Reduction ¶

As a part of our Journey,I did my second task as Dimensionality Reduction of 784d data into 2d by using PCA on an interesting data set called SIGNED ALPHABETS MNIST and LINK for data set is

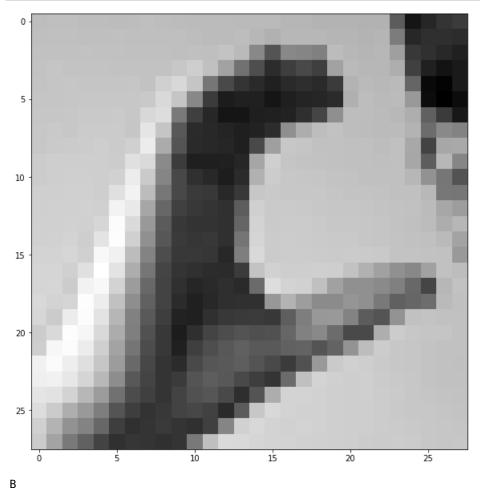
https://www.kaggle.com/datamunge/sign-language-mnist (https://www.kaggle.com/datamunge/sign-language-mnist)

```
In [0]:
            import pandas as pd
            import numpy as np
            import matplotlib.pyplot as plt
            import seaborn as sns
            import warnings
            warnings.filterwarnings("ignore")
In [53]:
           data = pd.read_csv("/content/drive/My Drive/Data_Scientist/pca-tsne/sign_mnist_train.csv")
            data.head()
Out[53]:
                label
                     pixel1
                             pixel2
                                    pixel3
                                           pixel4
                                                  pixel5
                                                         pixel6
                                                                 pixel7
                                                                        pixel8
                                                                               pixel9
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                                                                                              pixel11
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            5 rows × 785 columns
In [54]: data.shape
Out[54]: (27455, 785)
In [55]:
            labels = data['label']
            data = data.drop('label',axis= 1)
            data.head()
Out[55]:
                pixel1
                       pixel2
                              pixel3
                                     pixel4
                                            pixel5
                                                   pixel6
                                                           pixel7
                                                                  pixel8
                                                                         pixel9
                                                                                pixel10
                                                                                        pixel11
                                                                                                pixel12
                                                                                                        pixel13
                                                                                                                pixel14
                                                                                                                         pixel15
             0
                  107
                         118
                                127
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                                                      143
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                         157
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            5 rows × 784 columns
In [56]: print(labels.shape)
            (27455,)
```

```
In [92]: plt.figure(figsize=(10,10))
    ids = 2

    data_matrix = data.iloc[ids].as_matrix().reshape(28,28) # reshape from 1d to 2d pixel arra
    plt.imshow(data_matrix, interpolation = "none", cmap = "gray")
    plt.show()

    print(labels[ids])
```



2D Representation and Visualisation using PCA

```
In [58]: data = data.head(15000)
    labels = labels.head(15000)
    print("The shape of the data becomes",data.shape," and labels become",labels.shape)

The shape of the data becomes (15000, 784) and labels become (15000,)

In [59]: from sklearn.preprocessing import StandardScaler
    scaler = StandardScaler()
    standardised_data = scaler.fit_transform(data)
    print("The standardised data shape is",standardised_data.shape)
```

The standardised data shape is (15000, 784)

Covariance Matrix

Covariance matrix is used to understand how the variables of input data set are varying from mean wrt to each other or is there any relation ship among one another.

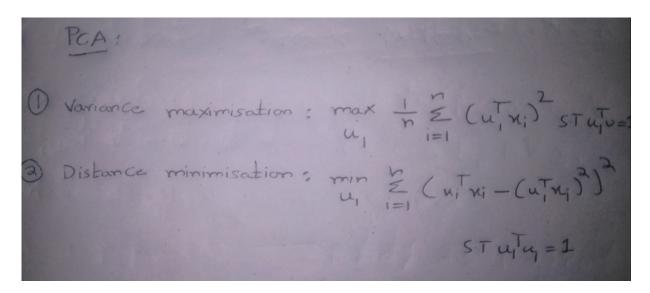
- It is a Symmetric matrix obtained by X^T * X
- cov(a,a) ---> var(a)
- cov(xi,yi) ---> sum[(xi-Ux) * (yi-Uy)] where sum means summation over i=1 to n && U means mean
- Covarince matrix is not more than a table that summarises correlation between all possible pairs of variables

```
In [60]: resultant_data = standardised_data
# matrix multiplication using numpy
covariance_matrix = np.matmul(resultant_data.T , resultant_data)
print ( "The shape of co_variance matrix = ", covariance_matrix.shape)
```

The shape of co_variance matrix = (784, 784)

What is the use of Eigen Values and Eigen Vectors?

Eigen vectors are the unit vectors which gives the direction of gives the direction of maximum spread of the points in that dimension



```
In [61]: # finding the top two eigen-values and corresponding eigen-vectors
         from scipy.linalg import eigh
         # eigh gives eigen values and vectors in ascending order and eigvals of parameters 782,783
         values, vectors = eigh(covariance_matrix, eigvals=(782,783))
         print("Shape of eigen vectors = ", vectors.shape)
         # transposing of vector to give(2,d) dimension
         vectors = vectors.T
         print("Updated shape of eigen vectors = ",vectors.shape)
         # here the vectors[1] represent the eigen vector corresponding 1st principal eigen vector
         # here the vectors[0] represent the eigen vector corresponding 2nd principal eigen vector
         Shape of eigen vectors = (784, 2)
         Updated shape of eigen vectors = (2, 784)
In [62]: # projecting the original data sample on the plane
         import matplotlib.pyplot as plt
         reshaping of original coordinates = np.matmul(vectors, resultant data.T)
         print (" resultanat new data point's shape ", vectors.shape, "X", data.T.shape," = ", resha
          resultanat new data point's shape (2, 784) \times (784, 15000) = (2, 15000)
```

```
In [0]: words dict ={
              0:'A',
              1:'B',
              2:'C',
3:'D',
              4:'E',
              5:'F',
              6:'G',
              7:'H',
8:'I',
9:'J',
              10: 'K'
              11: 'L',
              12:'M',
              13:'N',
              14:'0',
              15: 'P',
              16:'Q',
              17: 'R',
              18:'S',
              19: 'T'
              20:'U',
              21: 'V',
              22:'W',
              23:'X',
              24: 'Y'
              25: 'Z'
          }
In [73]: | words_dict[1]
Out[73]: 'B'
In [84]: for i in range(len(labels)) :
            if(labels[i] in words dict.keys()) :
              labels[i] = words_dict[labels[i]]
          labels = pd.Series(labels)
          print(labels.head())
          0
               Α
          1
               Α
         2
               В
          3
               C
               D
          dtype: object
In [85]: import pandas as pd
          # appending label to the data
          final_coordinates = np.vstack((reshaping_of_original_coordinates, labels)).T
          # Final2d Data set
          two_d_data = pd.DataFrame(data=final_coordinates, columns=("1st_principal_component", "2nd_
          print(two_d_data.head())
            1st_principal_component 2nd_principal_component labels
          0
                            0.347344
                                                       4.62431
                                                                     Α
          1
                            -4.45913
                                                       6.69406
                                                                     Α
                            -20.6547
         2
                                                     -0.336218
                                                                     В
          3
                            -20.3266
                                                      -9.53171
                                                                     C
          4
                            -2.89753
                                                      -6.60637
                                                                     D
```

Visualising our data using seaborn

```
In [87]:
            import seaborn as sn
            sn.FacetGrid(two_d_data, hue="labels", size=6).map(plt.scatter, '1st_principal_component',
            plt.show()
                60
                40
            2nd_principal_component
                20
               -20
               -40
                     -30
                             -20
                                     -10
                                                               20
                                                       10
                                     1st_principal_component
```

PCA using Scikit-Learn

Let's implement same using sklearn's implementation

```
In [89]: from sklearn import decomposition
    pca = decomposition.PCA(n_components = 2)
    pca_data = pca.fit_transform(resultant_data)
    print("shape of sklearn's pca implemented data's shape = ", pca_data.shape)
```

shape of sklearn's pca implemented data's shape = (15000, 2)

```
In [90]: pca_data = np.vstack((pca_data.T, labels)).T

# creating a new data fram which help us in ploting the result data
pca_resultant_data = pd.DataFrame(data=pca_data, columns=("lst_principal_component", "2nd_p
sns.FacetGrid(pca_resultant_data, hue="labels", size=6).map(plt.scatter, 'lst_principal_com
plt.show()

**The principal component is a principal compon
```

PCA estimation using cumulative sum of percentage Variance Share

40

20

1st_principal_component

• lambda_i gives eigen values

-40

-20

-30

lambda_i/(sum(lambda_i)) gives percentage of variance explained and we plot the cummulative sums of percentage
of variances explained

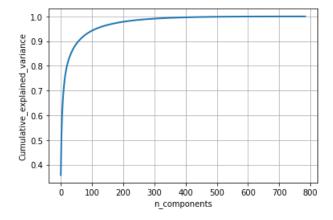
```
In [91]: pca.n_components = 784
    pca_data = pca.fit_transform(resultant_data)

    percentage_var_explained = pca.explained_variance_ / np.sum(pca.explained_variance_);

    cum_var_explained = np.cumsum(percentage_var_explained)

#plotting values of PCA
    plt.figure(1, figsize=(6, 4))

    plt.clf()
    plt.plot(cum_var_explained, linewidth=2)
    plt.axis('tight')
    plt.grid()
    plt.xlabel('n_components')
    plt.ylabel('Cumulative_explained_variance')
    plt.show()
```



CONCLUSIONS: By just considering only 100 components we preserves 95% of data

LIMITATIONS OF PCA:

- · Won't work for Sinusoidal data sets
- · Won't work for equally distributed data along axis
- Data Loss to some extent