## Homework 3

## February 20, 2022

GaAs HBT, surface recombination, base resistance and performance over time.

1. (a) Resistivity is given as:

 $R = \rho \frac{L}{A}$ 

where:

$$\rho = \frac{1}{nq\mu_n + pq\mu_p}$$

Assuming GaAs' intrinsic carrier concentration  $n_i$  is 2.1E+6 cm<sup>-3</sup>, the collector width  $W_c$  is 1.5  $\mu m$ , and the subcollector length  $L_s$  is 2  $\mu m$ , the resistivity can be calculated.

From the graph given, the electron and hole mobilities can be obtained, resulting in  $\mu_n = 6000 \frac{\text{cm}^2}{\text{V s}}$ for the collector, and  $\mu_n = 1700 \frac{\text{cm}^2}{\text{V s}}$  for the subcollector. This leads to a resistance of 18  $\Omega$ for the  $0.5 \times 4.5$  model, and 54  $\Omega$ for the  $0.25 \times 1.5$  model.

- (b) For this model, we take the same assumptions as above, but using a base width  $W_b$  of 0.25 µm. This leads to a resistance of 5.56  $\Omega$ for the 0.5×4.5 model, and 16.7  $\Omega$ for the 0.25×1.5 model.
- (c) Capacitance is given as:

$$C = \frac{\epsilon A}{d}$$

The permittivity of SiO<sub>2</sub> is 3.4515E-13  $\frac{F}{cm}$ , and the oxide width  $W_O$  is 0.6  $\mu$ m. By sweeping the oxide depth from 0 to 800 cm, the graphs in figures 1a and 1b are generated.

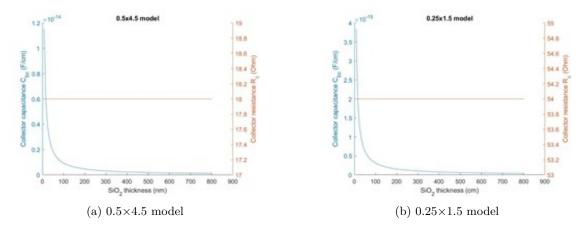


Figure 1: Thickness vs capacitance for both models.

2. The steady state diffusion equation is given as:

$$\frac{d^2 \delta p}{dx^2} = \frac{\delta p}{D_p \tau_p} - \frac{G_{op}}{D_P} \equiv \frac{\delta p}{L_p^2} - \frac{G_{op}}{D_p}$$

with a general solution of:

$$\delta p(x) = G_{op} \tau \left( 1 - \frac{\cosh \frac{x}{L}}{\cosh \frac{a}{2L}} \right)$$

However, this does not include the effects of an arbitrary surface recombination velocity, as discussed in slide 43 of Lectures 11 and 12. Skipping the derivation, the diffusion equation with the included surface recombination velocity is given as:

$$\delta p(x) = G_{op} \tau \left( 1 - \frac{s \cosh \frac{x}{L}}{s \cosh \frac{a}{2L} + \frac{D}{L} \sinh \frac{a}{2L}} \right)$$

where  $G_{op}$  and  $\tau$  are constants in this case, D is the diffusion coefficient, and L is the length of the semiconductor. This is to be solved for all combinations of  $s = \{1E+3, 1E+4, 1E+5, 1E+6\}$   $\frac{cm}{s}$ , and  $a = \{\frac{L_n}{5}, L_n, 5L_n\}$ , leading to 12 cases to solve for.

To graph this, the vertical axis can be modified by  $y' = \frac{\delta p(x)}{G_{op}\tau}$ , and the horizontal axis can be normalized by  $x' = \frac{x}{a}$ . This leads to the formula:

$$y' = 1 - \frac{s \cosh \frac{x'a}{L}}{s \cosh \frac{a}{2L} + \frac{D}{L} \sinh \frac{a}{2L}}$$

As an example of the mathematics, the first combination of a surface recombination rate of 1E+3  $\frac{cm}{s}$  and a thickness of  $\frac{L_n}{5}$ , the problem would simplify to:

$$y' = 1 - \frac{1000 \cosh \frac{Lx'}{5L}}{s \cosh \frac{L}{10L} + \frac{D}{L} \sinh \frac{L}{10L}}$$
$$= 1 - \frac{1000 \cosh 0.2x'}{1000 \cosh \frac{1}{10} + \frac{D}{L} \sinh \frac{1}{10}}$$
$$\approx 1 - \frac{1000 \cosh 0.2x'}{1005 + \frac{0.1002D}{L}}$$

As diffusion coefficient D and diffusion length L are not given nor can they be omitted from the equation, I chose random numbers for them to accentuate the important curves.

All 12 combinations are graphed in figure 2. Since this graph is very cluttered, I have also provided graphs holding the surface recombination rates constant, at  $s = \{1E + 3, 1E + 4, 1E + 5, 1E + 6\}$  in figures 3, 4, 5, and 6, respectively.

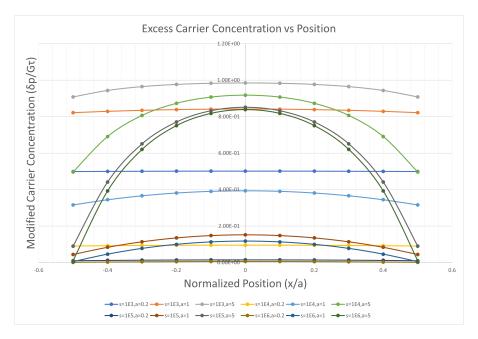


Figure 2: All twelve combinations of surface recombination rates and thicknesses.

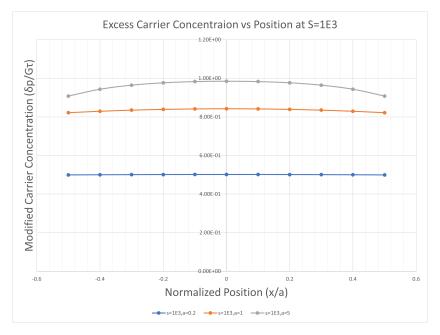


Figure 3: Graph for only s = 1E3.

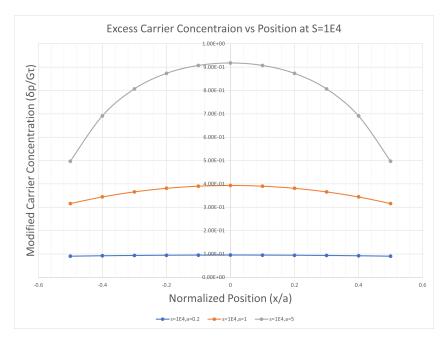


Figure 4: Graph for only s = 1E4.

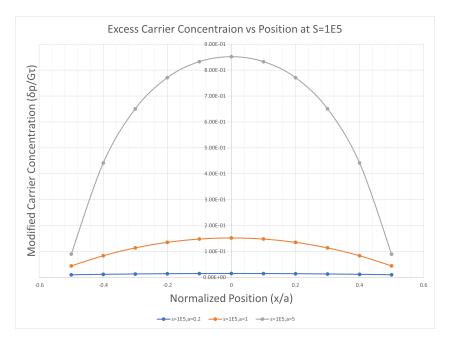


Figure 5: Graph for only s=1E5.

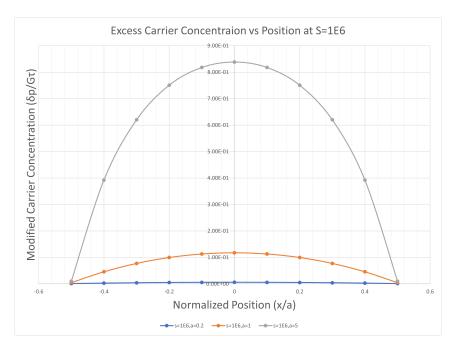


Figure 6: Graph for only s = 1E6.

3. (a) Base resistance is given as:

$$R_{sbi} = \frac{1}{q \int_0^{W_B} p_p(x) \mu_p(x) dx}$$

For constant base doping, we assume that  $P_p(x) \approx N_{aB} = 1E + 20$ , and the hole mobility is constant at 450. We also assume that the emitter and metal plugs are uniform in the same direction. This allows us to simplify the equation to:

$$R_{sbi} = \frac{1}{q \int_0^{W_B} N_{aB} \mu_p dx} = \frac{1}{q W_B N_{aB} \mu_p}$$

Because of the symmetry, we can divide by two for each side:

$$R_t = \frac{1}{2} R_{SiGe} + \frac{1}{2} R_{Si}$$

$$= \frac{1}{2} \frac{1}{1.609E - 19 * 0.025E + 18 * 450} + \frac{1}{2} \frac{1}{1.609E - 19 * 0.025E + 20 * 450}$$

$$= 0.279 \Omega \mu m$$

(b) In this case, simply take the resistance of the SiGe:

$$R_{SiGe} = \frac{1}{1.609E - 19*0.025E + 18*450} = 0.552$$
Ωμm

(c) To find the percent improvement, use the formula for percentage increase:

$$\frac{0.552 - 0.279}{0.279} * 100\% = 97.84\%$$

(d)  $\tau_B$  can be approximated as:

$$\tau_B \approx \frac{W_B^2}{2D_{nB}}$$

where

$$D_{nB} = \frac{kT}{q} \mu_{nB}$$

With the values as described in previous parts, this leads to  $D_{nB} = 8.90 \frac{\text{cm}^2}{\text{s}}$ . Therefore:

$$\tau_B \approx \frac{(2.5E - 6)^2}{2 * 8.90} \approx 3.511E - 13s$$

The frequency is simply the inverse of lifetime:

$$f = \frac{1}{\tau_B} \approx 284.8 \text{GHz}$$

The reported  $f_t$  is given to be about 320 GHz, which is greater than the found  $f_{SiGe}$  above.

(e) From the results above, by allowing epitaxial growth, the intrinsic resistance goes down, but the transit time goes up.

4.

Base	Device Size	Unity	Base	Base	Base	Reference
Width	$(L_E, W_E)$	current	transit	collector	Resistance	
		gain cutoff	time (ps)	capacitance	$(R_b b)$	
		frequency,		$(C_{bc})$		
		$f_t$				
0.1µm	0.12*2.5μm	$350~\mathrm{GHz}$				1.
0.1µm	0.12*1.0μm	$352~\mathrm{GHz}$	0.36		304	2.
0.1µm	0.12*0.96µm	300 GHz		13.9		3.
0.1µm	10*3μm	32 GHz				4.
0.14µm	3*10μm	40 GHz	6			5.
$0.055 \mu m$	1*1μm	20 GHz				6.

## References:

- 1: https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=1175952 (SiGe)
- 2: https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=1644829 (SiGe)
- 3: https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=6082749 (IHP2 SiGe)
- 4: https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=108180 (Table IV, Device A)
- 5: https://ieeexplore.ieee.org/document/32211 (GaAs)
- 6: https://aip.scitation.org/doi/10.1063/1.5058717 (GaAs)

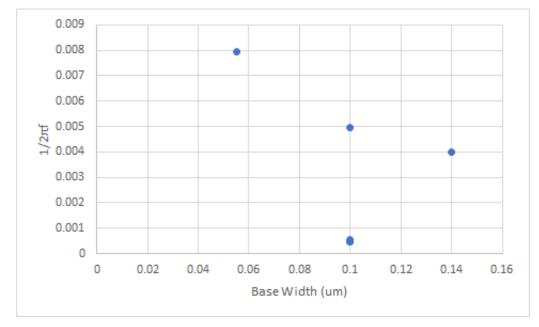


Figure 7:  $\frac{1}{2\pi f_t}$  as a function of  $W_b$ .