

Drill Handout    Section 2.5    September 10, 2019    Name: \_\_\_\_\_

- (1) Determine  $\lim_{x \rightarrow \infty} f(x)$  and  $\lim_{x \rightarrow -\infty} f(x)$  for the following function. Then give the horizontal asymptotes of  $f$  (if any).

$$f(x) = \frac{3x + \sqrt{4x^2 + 1}}{x + 2}$$

- (2) Determine  $\lim_{x \rightarrow \infty} g(x)$  and  $\lim_{x \rightarrow -\infty} g(x)$  for the following function. Then give the horizontal asymptotes of  $g$  (if any).

$$g(x) = 2x - \sqrt{4x^2 + x + 1}$$

- (3) Determine  $\lim_{x \rightarrow \infty} h(x)$  and  $\lim_{x \rightarrow -\infty} h(x)$  for the following function. Then give the horizontal asymptotes of  $h$  (if any).

$$h(x) = e^{-x} \cos x$$

- (4) Sketch a possible graph of a function  $f$  that satisfies all of the given conditions. Be sure to identify all vertical and horizontal asymptotes.

$$\begin{aligned} \lim_{x \rightarrow 3} f(x) = \infty, \quad \lim_{x \rightarrow 1^+} f(x) = -\infty, \quad \lim_{x \rightarrow 1^-} f(x) = \infty, \quad f(2) = 0 \\ \lim_{x \rightarrow \infty} f(x) = 1, \quad \lim_{x \rightarrow -\infty} f(x) = 2. \end{aligned}$$