

MATLAB

Finite Difference Method and Initial Part

For PDEs: Heat Equation, Advection-Diffusion
Equation,...



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Part I

Finite Difference

One

Finite Difference

In this method we discretize a space into a finite number of points and use these points to find an approximate solution of a PDE.

1.1 Schemes for Discretization

Let $u = u(x, t)$ be a function in two variables.

Let the interval of the variable x is discretized into m number of points; x_1, x_2, \dots, x_m and of the variable t into n number of points; t_1, t_2, \dots, t_n .

Forward Difference of 1^{st} order

$$\frac{\partial u(x_i, t_j)}{\partial x} = \frac{u(x_i + h, t_j) - u(x_i, t_j)}{h} = \frac{V_{i+1}^j - V_i^j}{h}$$

Likewise,

$$\frac{\partial u}{\partial t} = \frac{V_i^{j+1} - V_i^j}{k}$$

Backward Difference of 1st order

$$\frac{\partial u(x_i, t_j)}{\partial x} = \frac{u(x_i, t_j) - u(x_i - h, t_j)}{h} = \frac{V_i^j - V_{i-1}^j}{h}$$

Likewise,

$$\frac{\partial u}{\partial t} = \frac{V_i^j - V_i^{j-1}}{k}$$

Central Difference of 1st order

It is the average of forward difference and backward difference.

$$\frac{\partial u(x_i, t_j)}{\partial x} = \frac{V_{i+1}^j - V_i^j + V_i^j - V_{i-1}^j}{2h} = \frac{V_{i+1}^j - V_{i-1}^j}{2h}$$

Central Difference of 2nd order

$$\frac{\partial^2 u}{\partial x^2} = \frac{V_{i+1}^j - 2V_i^j + V_{i-1}^j}{h^2}$$

$$\frac{\partial^2 u}{\partial t^2} = \frac{V_i^{j+1} - 2V_i^j + V_i^{j-1}}{k^2}$$

Code Conventions:

Variables	Axis	Loop var.	difference	Grid section
x	X	i	h	m
t/y	Y	j	k	n

Two

Heat Equation

Forward time Central space Scheme (**FTCS**) for the heat equation:

$$u_t = \alpha u_{xx}.$$

We have,

$$\begin{aligned}\frac{\partial u}{\partial t} &= \alpha \frac{\partial^2 u}{\partial x^2} \\ \frac{V_i^{j+1} - V_i^j}{k} &= \frac{V_{i+1}^j - 2V_i^j + V_{i-1}^j}{h^2} \\ V_i^{j+1} - V_i^j &= \frac{\alpha k}{h^2} (V_{i+1}^j - 2V_i^j + V_{i-1}^j) \\ V_i^{j+1} &= V_i^j + c(V_{i+1}^j - 2V_i^j + V_{i-1}^j)\end{aligned}$$

where $c = \frac{\alpha k}{h^2}$. This the required scheme.

Question

$$\begin{aligned}u_t &= \alpha u_{xx} & 0 < x < 1, \quad t > 0, \quad \alpha = 0.05 \\ BCS : \quad u(0, t) &= u(1, t) = 0 & t > 0 \\ IC : \quad u(x, 0) &= \sin \pi x & 0 < x < 1\end{aligned}$$

2.1 Matlab Code

```
1  %initialization
2  L=1;      m=10;   h=L/m;   x=0:h:L;
3  T=1;      n=10;   k=T/n;   t=0:k:T;
4
5  a=0.05;    c=a*k/(h*h);
6  v=zeros(m+1, n+1);
7
8  %checking
9  if (c<0|c>0.5)
10     disp('The FTCS is unstable. ');
11 else
12
13 %boundary equations
14     v(1,:)=0;      v(m+1,:)=0;
15     v(:,1)=sin(pi*x);
16
17 %scheme
18     for j=1:n
19         for i=2:m
20             v(i,j+1)=v(i,j)+c*(v(i+1,j)-2*v(i,j)+v(i-1,j));
21         end
22     end
23 end
24
25 %graph
26 [p,q]=meshgrid(x,t);
27
28 surf(p,q,v);
29 xlabel('space'); ylabel('time'); zlabel('Temperature');
30 title('Numerical solution of heat equation.');
```

Three

Advection Diffusion Equation

Forward Time Backward Space Central Space Scheme (FTBSCS)
for the following advection diffusion equation:

$$\frac{\partial C}{\partial t} + v \frac{\partial C}{\partial x} = D \frac{\partial^2 C}{\partial x^2}$$

where,

C is concentration of dissolved substances

v is velocity of the fluid

D is diffusion coefficient.

We have,

$$\begin{aligned} \frac{V_i^{j+1} - V_i^j}{k} + v \frac{V_i^j - V_{i-1}^j}{h} &= D \frac{V_{i+1}^j - 2V_i^j + V_{i-1}^j}{h^2} \\ V_i^{j+1} - V_i^j &= \frac{Dk}{h^2} (V_{i+1}^j - 2V_i^j + V_{i-1}^j) - \frac{vk}{h} (V_i^j - V_{i-1}^j) \\ V_i^{j+1} &= V_i^j + F(V_{i+1}^j - 2V_i^j + V_{i-1}^j) - G(V_i^j - V_{i-1}^j) \end{aligned}$$

where,

$$F = \frac{Dk}{h^2} \quad G = \frac{vk}{h}$$

Question

$$\begin{aligned}C_t + vC_x &= DC_{xx} \\ 0 \leq t &\leq 4000 * 24, & D &= 10^{-6} * 3600 \\ 0 \leq x &\leq 100, & v &= 10^{-7} * 3600 \\ IC : C(x, 0) &= 100\end{aligned}$$

3.1 Matlab Code

```
1  %Initialization
2  L=100;    m=20;    h=L/m;    x=0:h:L;
3  T=4000*24;  n=20;    k=T/n;    t=0:k:T;
4
5  D=(1E-6)*3600;    F=(D*k)/(h*h);
6  V=(1E-7)*3600;    G=(V*k)/h;
7
8  v=zeros(m+1,n+1);
9
10 %Initial conditon
11 v(:,1)=100;
12
13 %Scheme
14 for j=1:n
15     for i=2:m
16         v(i,j+1)=v(i,j)+F*(v(i+1,j)-2*v(i,j)+v(i-1,j))-G*(v(i,j)-v(i-1,j));
17     end
18 end
19
20 %Graph
21 [p,q]=meshgrid(x,t);
22 surf(p,q,v);
23 xlabel('space';    ylabel('time');    zlabel('concentration');
24 title('Numerical solution of Advection-Diffusion equation.');
```

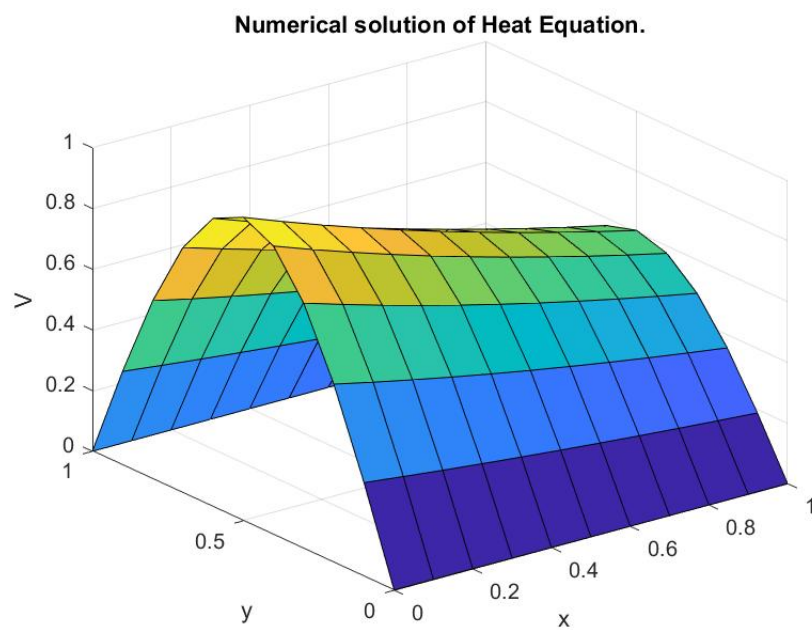


Figure 3.1: Heat Equation

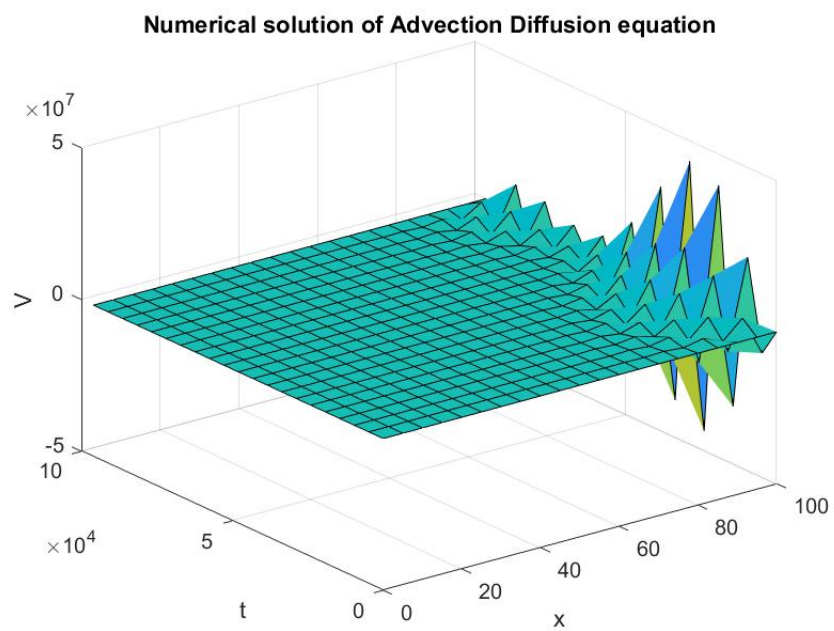


Figure 3.2: Advection Diffusion equation

Four

Laplace Equation

The Laplace equation is

$$u_{xx} + u_{yy} = 0$$

The Central Space Central Space Scheme (**CSCSS**) for the above equation:

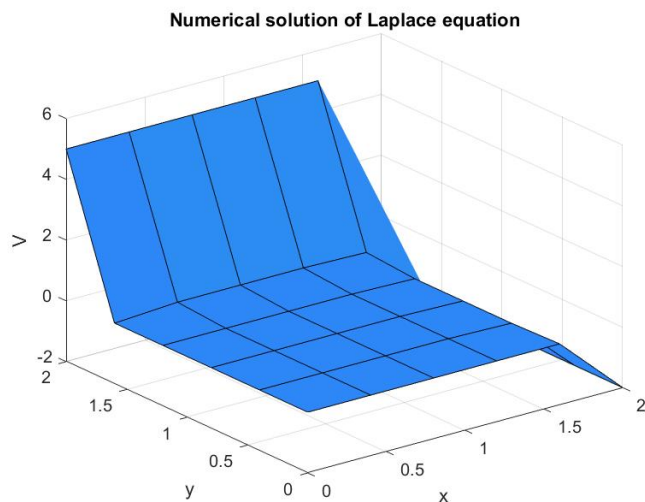
$$\begin{aligned} \frac{V_{i+1}^j - 2V_i^j + V_{i-1}^j}{h^2} + \frac{V_i^{j+1} - 2V_i^j + V_i^{j-1}}{k^2} &= 0 \\ k^2(V_{i+1}^j - 2V_i^j + V_{i-1}^j) + h^2(V_i^{j+1} - 2V_i^j + V_i^{j-1}) &= 0 \\ k^2(V_{i+1}^j + V_{i-1}^j) + h^2(V_i^{j+1} + V_i^{j-1}) &= 2(h^2 + k^2)V_i^j \\ V_i^j &= \frac{k^2(V_{i+1}^j + V_{i-1}^j) + h^2(V_i^{j+1} + V_i^{j-1})}{2(h^2 + k^2)} \end{aligned} \quad (4.1)$$

Question

$$\begin{array}{ll} u_{xx} = u_{yy} & 0 \leq x \leq 2, \quad 0 \leq y \leq 2 \\ BCS : \quad u(0, y) = 0, \quad u(2, y) = 5 & 0 \leq y \leq 2 \\ u(x, 0) = 0, \quad u(x, 2) = -2 & 0 \leq x \leq 2 \end{array}$$

4.1 Matlab Code

```
1  %Initialization
2  L=2;      m=5;   h=L/m;   x=0:h:L;
3  B=2;      n=5;   k=B/n;   t=0:k:B;
4
5  c=1/(2*(h^2+k^2));
6  v=zeros(m+1, n+1);
7
8  %Boundary Conditions
9  v(1,:)=0;   v(m+1,:)=5;
10 v(:,1)=0;   v(:,n+1)=-2;
11
12 %Scheme
13 for j=2:n
14     for i=2:m
15         v(i,j)=c*((h^2*(v(i,j+1)+v(i,j-1)))+(k^2*(v(i+1,j)+v(i-1,j))));
16     end
17 end
18
19 %Graph
20 [p,q]=meshgrid(x,t);
21
22 surf(p,q,v);
23 xlabel('x'); ylabel('y'); zlabel('u');
24 title('Numerical solution of Laplace equation.');
```



Five

Wave Equation

The wave equation is $u_{tt} = au_{xx}$

The Central Space Central Space Scheme (**CTCSS**) for the above equation:

$$\begin{aligned}\frac{V_i^{j+1} - 2V_i^j + V_i^{j-1}}{k^2} &= a \frac{V_{i+1}^j - 2V_i^j + V_{i-1}^j}{h^2} \\ V_i^{j+1} - 2V_i^j + V_i^{j-1} &= \frac{ak^2}{h^2} (V_{i+1}^j - 2V_i^j + V_{i-1}^j) \\ V_i^{j+1} &= 2(1 - c)V_i^j + c(V_{i+1}^j + V_{i-1}^j) - V_i^{j-1}\end{aligned}\quad (5.1)$$

where, $c = \frac{ak^2}{h^2}$

Question

$$\begin{aligned}u_{tt} &= au_{xx} & 0 \leq x \leq 1, \quad t \geq 0 \\ BCs : \quad u(0, t) &= u(1, t) = 0 & t \geq 0 \\ ICs : \quad u(x, 0) &= 10\sin\pi x \quad u_t(x, 0) = 0 & 0 \leq x \leq 1\end{aligned}$$

5.1 Scheme for Initial Condition

The initial condition $u_t(x, 0) = 0$ also needs a separate scheme as it is in a derivative form.

The Central Time Scheme for u_t is :

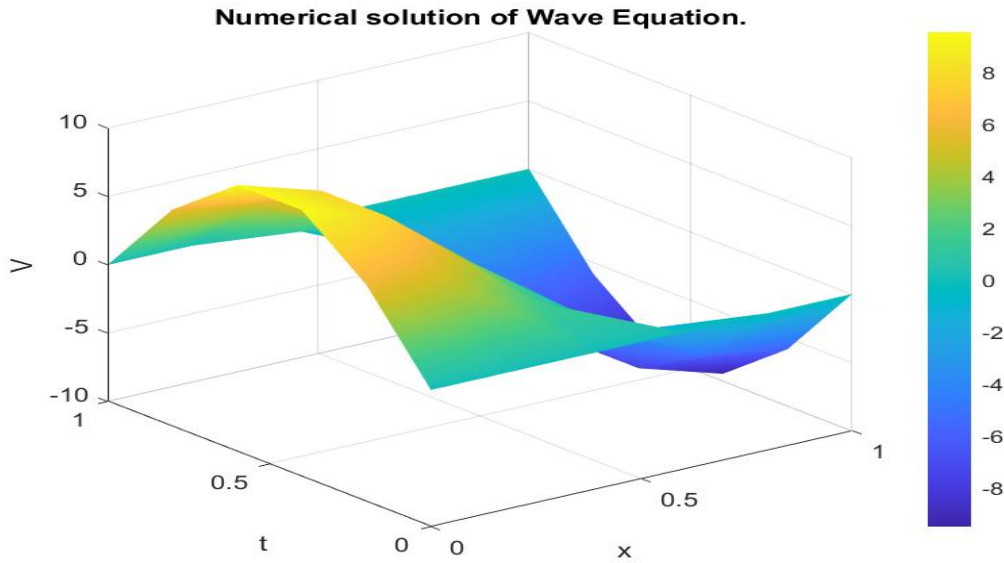
$$\begin{aligned}
 u_t &= \frac{V_i^{j+1} - V_i^{j-1}}{2k} \\
 \implies 2ku_t &= V_i^{j+1} - V_i^{j-1} \\
 \text{For } j &= 0 \\
 2ku_t &= V_i^1 - V_i^{-1} \\
 \implies V_i^{-1} &= V_i^1 - 2ku_t
 \end{aligned} \tag{5.2}$$

Also, Putting $j = 0$ in equation (5.1)

$$V_i^1 = 2(1 - c)V_i^0 + c(V_{i+1}^0 + V_{i-1}^0) - V_i^{-1} \tag{5.3}$$

From equation (5.2) and (5.3)

$$V_i^1 = (1 - c)V_i^0 + 0.5c(V_{i+1}^0 + V_{i-1}^0) + ku_t \tag{5.4}$$



5.2 Matlab Code

```
1  %Initialization
2  L=1;          m=5;          h=L/m;          x=0:h:L;
3  T=1;          n=5;          k=T/n;          t=0:k:T;
4
5  a=1;          c=a*(k^2/h^2);
6  V=zeros(m+1,n+1);
7
8  %Checking
9  if (c<=0|c>1)
10     disp('The CTCSS is unstable')
11 else
12
13 %Boundary Conditions
14     V(1,:)=0;          V(m+1,:)=0;
15
16 %Initial Conditions
17     V(:,1)=10*sin(pi*x);
18
19     for i=2:m
20         V(i,2)=(1-c)*V(i,1)+0.5*c*(V(i+1,1)+V(i-1,1));
21     end
22
23 %Main Scheme
24     for j=2:n
25         for i=2:m
26             V(i,j+1)=2*(1-c)*V(i,j)+c*(V(i+1,j)+V(i-1,j))-V(i,j-1);
27         end
28     end
29
30 %Graph
31     [p,q]=meshgrid(x,t);
32     surf(p,q,V,'Edgecolor','none');
33     xlabel('space');          ylabel('time');          zlabel('u');
34     title('Numerical solution of Wave Equation. ');
35     shading interp;
36 end
```

Part II

Initial Part

Six

Numerical Integration

6.1 Code for Trapezoidal Rule

```
1  % Initialization
2  f=@(x) x*sin(x);
3
4  a=0;      b=(pi/2);
5  n=5;      h=(b-a)/n;
6
7  S=0.5*(f(a)+f(b));
8  S1=0;
9
10 % Scheme
11 for i=1:n-1
12     xi=a+i*h;
13     S1=S1+f(xi);
14 end
15
16 I=h*(S+S1);
17
18 fprintf('The integral is %f\n',I)
19
```

ans = 1.008265

6.2 Code for Simpson's 1/3 rule

```
1  %Initialization
2  f=@(x) x*sin(x);
3
4  a=0;      b=(pi/2);
5  n = 12;   h=(b-a)/n;
6
7  S=f(a)+f(b);
8  S1=0;
9  S2=0;
10
11 % Scheme
12 for i=1:2:n-1
13     xi=a+i*h;
14     S1=S1+f(xi);
15 end
16
17 for i=2:2:n-2
18     xi=a+i*h;
19     S2=S2+f(xi);
20 end
21
22 % Output
23 I=(h/3)*(S+4*S1+2*S2);
24 fprintf('The integral value is %f.\n',I)
25
```

ans = 0.999995

6.3 Code for Simpson's 3/8 rule

```
1  % Initialization
2  f=@(x) x*sin(x);
3
4  a=0;          b=pi/2;
5  n=12;         h=(b-a)/n;
6
7  S1=f(a)+f(b); S2=0;    S3=0;
8
9  % Scheme
10 for i=1:3:n-2
11     x1=a+i*h;
12     x2=a+(i+1)*h;
13     S2=S2+f(x1)+f(x2);
14 end
15
16 for i=3:3:n-3
17     S3=S3+f(a+i*h);
18 end
19
20 % Output
21 I=(3*h/8)*(S1+3*S2+2*S3);
22 fprintf('The integral value is %f.\n',I)
23
```

$ans = 0.999989$

Seven

Numerical Solution Polynomial Equations

7.1 Bisection Method

```
1  %Initialization
2  f=@(x) x^2-26;
3  a=5;    b=6;    toll=0.001;
4
5  % Scheme
6  while abs(a-b)>=toll
7      c=(a+b)/2;
8
9      if f(a)*f(c)<=0
10         b=c;
11     else
12         a=c;
13     end
14 end
15
16 fprintf('The solution by the bisection method is %f.\n',c)
```

$ans = 5.098633$

7.2 Newton Raphson's Method

```
1  %Initialization
2  f=@(x) 3*x*sin(x)-exp(x);
3  df=@(x) 3*x*cos(x)+3*sin(x)-exp(x);
4
5  a0=1;          toll=0.0001;   diff=1;
6
7  % Scheme
8  while diff>=toll
9      a1=a0-f(a0)/df(a0);
10
11     diff=abs(a1-a0);
12     a0=a1;
13 end
14
15 fprintf('The solution by Newton Raphson's method is %f.\n',a0)
```

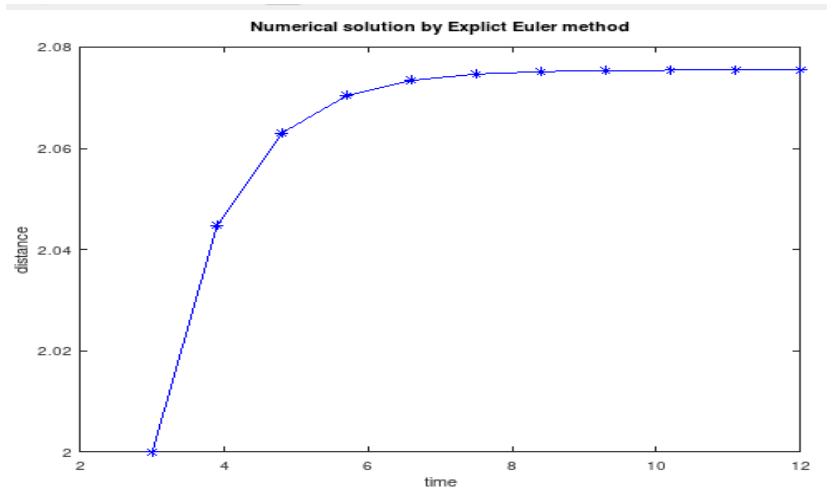
$ans = 1.159431$

Eight

Numerical Solution of ODEs

8.1 Explicit Euler Method

```
1  % Initialization
2  f=@(t,y) exp(-t);
3
4  a=3;      b=12;
5  n=10;     h=(b-a)/n;    t=a:h:b;
6
7  y(1)=2;   % Inital guess
8
9  % Scheme
10 for i=1:n
11     y(i+1)=y(i)+h*f(t(i),y(i));
12
13     fprintf('Solution at t=%d is %f.\n',t(i+1),y(i+1));
14 end
15
16 % Graph
17 plot(t,y,'-b*');
18 xlabel('time');    ylabel('distance');
19 title('Numerical solution by Explict Euler method');
```



8.2 Implicit Euler Method

```

1  % Initialization
2  f=@(t,y) exp(-t);
3
4  a=3;      b=12;
5  n=10;     h=(b-a)/n;    t=a:h:b;
6
7  y(1)=2;   % Inital guess
8
9  % Scheme
10 for i=1:n
11     k(i)=f(t(i),y(i));
12     y(i+1)=y(i)+h*f(t(i+1),y(i)+h*k(i));
13
14     fprintf('Solution at t=%d is %f.\n',t(i+1),y(i+1));
15 end
16
17 % Graph
18 plot(t,y,'-b*');
19 xlabel('time');    ylabel('distance');
20 title('Numerical solution by Implicit Euler method');

```

8.3 Second order Runge-Kutta method

```
1  % Initialization
2  f=@(t,y) exp(-t);
3
4  a=3;      b=12;
5  n=10;     h=(b-a)/n;    t=a:h:b;
6
7  y(1)=2;   % Inital guess
8
9  % Scheme
10 for i=1:n
11     k(i)=f(t(i),y(i));
12     k(i+1)=f(t(i+1),y(i)+h*k(i));
13
14     y(i+1)=y(i)+0.5*h*(k(i)+k(i+1));
15
16     fprintf('Solution at t=%d is %f.\n',t(i+1),y(i+1));
17 end
18
19 % Graph
20 plot(t,y,'-b*');
21 xlabel('time');    ylabel('distance');
22 title('Second order Runge-Kutta method');
23
```

8.4 Fourth order Runge-Kutta Method

```
1  % Initialization
2  f=@(t,y) exp(-t);
3
4  a=3;      b=12;
5  n=10;     h=(b-a)/n;    t=a:h:b;
6
7  y(1)=2;   % Inital guess
8
9  % Scheme
10 for i=1:n
11     k(i)=f(t(i),y(i));
12     k(i+1)=f(t(i)+h/2,y(i)+h/2*k(i));
13     k(i+2)=f(t(i)+h/2,y(i)+h/2*k(i+1));
14     k(i+3)=f(t(i)+h,y(i)+h*k(i+2));
15
16     y(i+1)=y(i)+(h/6)*(k(i)+2*k(i+1)+2*k(i+2)+k(i+3));
17
18     fprintf('Solution at t=%d is %f.\n',t(i+1),y(i+1));
19 end
20
21 % Graph
22 plot(t,y,'-b*');
23 xlabel('time');    ylabel('distance');
24 title('Fourth order Runge-Kutta method');
```

Nine

Solution of System of Equations

9.1 Gauss Elimination Method

```
1  % Initialization
2  A=[13,2,3; 2,15,1; 1,-1,10];    b=[46;33;25];
3  [n,n]=size(A);
4
5  % Non zero diagonal elements
6  for j=1:n-1                      %row1
7      for i=j+1:n                  %row2
8          if A(j,j)==0
9              t=A(j,:);
10             A(j,:)=A(i,:);
11             A(i,:)=t;
12
13             t=b(j,:);
14             b(j,:)=b(i,:);
15             b(i,:)=t;
16         end
17     end
18 end
19
20 %Forward elimination
21 for j=1:n-1                      %column jth
22     for i=j+1:n                  %(j+1)th row
23         m(i,j)=A(i,j)/A(j,j);
24         A(i,:)=A(i,:)-m(i,j)*A(j,:);
25         b(i,:)=b(i,:)-m(i,j)*b(j,:);
```

```

26     end
27 end
28
29 %Backward substitution
30 x(n,:)=b(n,:)/A(n,n); %nth coordinate; i.e last row in 'x'
31
32 for i=n-1:-1:1
33     x(i,:)=(b(i,:)-A(i,i+1:n)*x(i+1:n,:))/A(i,i);
34 end
35 x
36

```

ans : $x = 2.7279, 1.6766, 2.3949$

(same for Gauss-Jordan and Gauss-Seidel method aswell)

9.2 Gauss Seidel Method

```

1 % Initilazion
2 A=[13,2,3; 2,15,1; 1,-1,10];    b=[46;33;25];
3 N=length(b);                    toll=0.0001;
4 x=zeros(N,1);                    y=zeros(N,1);
5
6 for j=1:100
7     for i=1:N
8         num=b(i)-A(i,1:i-1)*x(1:i-1)-A(i,i+1:N)*x(i+1:N);
9         x(i)=num/A(i,i);
10    end
11
12    if abs(x-y)<toll
13        fprintf('Iteration number is %d\n',j);
14        break
15    end
16    y=x;
17 end
18 x
19

```

9.3 Gauss-Jordan Method

```
1  % Initilazion
2  A=[13,2,3,46; 2,15,1,33; 1,-1,10,25];
3  [m,n]=size(A);
4
5  % Non zero diagonal elements
6  for j=1:m-1                                %row1
7      for i=j+1:m                            %row2
8          if A(j,j)==0
9              t=A(j,:);
10             A(j,:)=A(i,:);
11             A(i,:)=t;
12         end
13     end
14 end
15
16 %Forward elimination
17 for j=1:n-2    %column jth; n-2 cause last column is b.
18     for i=j+1:m    %(j+1)th row
19         m(i,j)=A(i,j)/A(j,j);
20         A(i,:)=A(i,:)-m(i,j)*A(j,:);
21         b(i,:)=b(i,:)-m(i,j)*b(j,:);
22     end
23 end
24 % Backward elimination
25 for j=n-1:-1:2    %n-1 is the last column excluding b.
26     for i=j-1:-1:1
27         A(i,:)=A(i,:)-A(j,:)*(A(i,j)/A(j,j));
28     end
29 end
30
31 % making pivot element 1
32 for i=1:m
33     A(i,:)=A(i, :)/A(i,i);
34     x(i)=A(i,n);
35 end
36 x
```

Ten

Grading-System with If

```
1  % Internal Full Marks is 20 and final full marks is 30
2  I=input('Internal Marks Obtained:');
3  F=input('Final Marks Obtained:');
4
5  R=min(I,F/30*20*1.2);
6  fprintf('Revised Internal Marks is %2.2f.\n',R);
7
8  T=R+F;
9  fprintf('Total Marks Obtained is %2.2f.\n',T);
10
11 if I>20||F>30
12     disp('Wrong Information. ');
13 else
14     if T>=45
15         y='A';
16     elseif T>=40
17         y='A-';
18     elseif T>=35
19         y='B';
20     elseif T>=30
21         y='B-';
22     else
23         y='Fail';
24     end
25 end
26 fprintf('The obtained grade is %s.\n',y)
27
```

Eleven

Circle, Ellipse, Hyperbola, Parabola

Circle

```
1 r = input('Enter the value of radius:');
2 h = input('Enter x-coordinate of center:');
3 k = input('Enter y-coordinate of center:');
4
5 theta = 0:0.01:2*pi;
6 x = h+r*cos(theta);
7 y = k+r*sin(theta);
8
9 plot(x,y);
10 axis('equal');    xlabel('x-axis');    ylabel('y-axis');
```

Parabola

```
1 fprintf('A Parabola in parametric-form.\n\n');
2
3 a = input('Enter semi-major axis:');
4 h = input('Enter x-coordinate of center:');
5 k = input('Enter y-coordinate of center:');
6
7 t= -4:0.1:-4;
8 x = 2*a*t;
9 y = a*t.^2;    plot(x,y)
```

Ellipse

```
1  fprintf('A Ellipse in parametric-form.\n\n');
2
3  a = input('Enter the semi-major axis:');
4  b = input('Enter the semi-minor axis:');
5  h = input('Enter x-coordinate of center:');
6  k = input('Enter y-coordinate of center:');
7
8  theta = 0:0.01:2*pi;
9  x = h+a*cos(theta);
10 y = k+b*sin(theta);
11
12 plot(x,y);
13 axis('equal');
14 xlabel('x-axis');
15 ylabel('y-axis');
```

Hyperbola

```
1  fprintf('A Hyperbola in parametric-form.\n\n');
2
3  a = input('Enter the semi-major axis:');
4  b = input('Enter the semi-minor axis:');
5  h = input('Enter x-coordinate of center:');
6  k = input('Enter y-coordinate of center:');
7
8  theta = (-pi/3):0.1:(pi/3);
9  x = h+a*sec(theta);
10 y = k+b*tan(theta);
11
12 plot(x,y);
13 axis('equal');
14 xlabel('x-axis');
15 ylabel('y-axis');
```

11.1 Plotting

Multi-plot

```
1 x = -2:0.1:4;
2 y = 3*x.^3-26*x+6;
3 yd = 9*x.^2-26;
4 ydd = 18*x;
5
6 plot(x,y,'-b');
7
8 hold on
9 plot(x,yd,'-.k');
10 plot(x,ydd,'--m');
11 title('Fucntion and its Derivatives');
12 xlabel('x-axis');
13 ylabel('y_axis');
14 legend('Function', 'First-Deri', 'Second-Deri')
15 hold off
```

Sub-Plot

```
1 x = -2:0.1:4;
2 y = 3*x.^3-26*x+6;
3
4 yd = 9*x.^2-26;
5 ydd = 18*x;
6
7 subplot(1,3,1), plot(x,y), xlabel('x-axis'),
8 ylabel('y-axis'), %1-row 3-column 1-positon.
9 subplot(1,3,2), plot(x,yd);
10 subplot(1,3,3), plot(x,ydd);
```

3D-Plot

```
1 x = -2:0.01:4;
2 y = sin(x);
3 z = x.^2 + y.^2;
4
5 plot3(x,y,z);
6 xlabel('x');    ylabel('y');    zlabel('z');
7 title('Curve in 3D');
```

Surface-Plot

```
1 x = -2:0.01:4;
2 y = -3:0.01:4;
3 [u,v] = meshgrid(x,y);
4
5 z = sin(u) + cos(v);
6
7 surf(x,y,z);
8
9 xlabel('x');    ylabel('y');    zlabel('z');
10 title('Surface Plotting');
11 shading interp;
12 colorbar;
```
