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## Fourth Semester B.E. Degree Examination, Dec.2016/Jan.2017 Advanced Mathematics – II

Time: 3 hrs. Max. Marks:100

Note: Answer any FIVE full questions.

- a. Find the angle between any two diagonals of a cube.
  b. The direction cosines of three mutually perpendicular lines are l<sub>1</sub>, m<sub>1</sub>, n<sub>1</sub> l<sub>2</sub>, m<sub>2</sub>, n, and
  - In direction cosines of three mutually perpendicular lines are  $l_1$ ,  $m_1$ ,  $n_1$ ,  $l_2$ ,  $m_2$ ,  $n_2$  and  $l_3$ ,  $m_3$ ,  $n_3$ . Show that the line with direction cosines  $l_1 + l_2 + l_3$ ,  $m_1 + m_2 + m_3$ ,  $l_1 + l_2 + l_3$  is equally inclined to the above lines. (07 Marks)
  - c. Find the equations of the plane passing through the points (1, 2, 3) (0, 1, 4) and (0, 0, 1). (07 Marks)
- 2 a. Derive the equation to the plane in the intercept form  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ . (06 Marks)
  - b. Find the angle between the lines  $\frac{x-1}{1} = \frac{y-5}{0} = \frac{z+1}{2}$  and  $\frac{x+3}{3} = \frac{y}{5} = \frac{z-5}{2}$ . (07 Marks)
  - c. Find the image of the point (1, 2, 3) in the line  $\frac{x+1}{2} = \frac{y-3}{3} = -z$ . (07 Marks)
- 3 a. Show that the position vectors of the vertices of a triangle 2i-j+k, i-3j-5k, 3i-4j-4k form a right angled triangle. (06 Marks)
  - b. Find a vector of magnitude 12 units which is perpendicular to the vectors  $\vec{a} = 4i j + 3k$  and  $\vec{b} = -2i + j 2k$ . (07 Marks)
  - c. Find  $\lambda$  so that the points A(-1, 4, -3), B(3, 2, -5), C(-3, 8, -5) and D(-3,  $\lambda$ , 1) are coplanar. (07 Marks)
- 4 a. Find the unit tangent vector of the space curve  $x = 1 + t^3$ ,  $y = 2t^3$ ,  $z = 2 t^3$  at t = 1.
  - b. Find the angle between the tangents to the curve  $\vec{r} = \left(t \frac{t^2}{2}\right)i + t^2j + \left(t + \frac{t^2}{2}\right)k$  at  $t = \pm 1$
  - c. A particle moves along the curve whose parametric equations are  $x = t \frac{t^3}{3}$ ,  $y = t^2$  and  $z = t + \frac{t^3}{3}$ , where 't' is the time. Find the velocity and acceleration at any time 't'. Also find their magnitudes at t = 3.
- 5 a. Find the angle between the surfaces  $x^2 + y^2 + z^2 = 9$  and  $x = z^2 + y^2 3$  at (2,-1,2).
  - b. Find the constants a, b, c such that the vector,
    - $\overrightarrow{F} = (x + y + az)i + (bx + 2y z)j + (x + cy + 2z)k \text{ is irrotational.}$  (07 Marks)
  - c. If  $\overrightarrow{A} = \operatorname{grad}(x^3 + y^3 + z^3 3xyz)$  then find div  $\overrightarrow{A}$  and curl  $\overrightarrow{A}$ . (07 Marks)