MATDIP401

Fourth Semester B.E. Degree Examination, June/July 2018

Advanced Mathematics - II

Time: 3 hrs. Max. Marks:100

Note: Answer any FIVE full questions.

- 1 a. Find the ratio in which the point C, (9, 8, -10) divides the line segment joining the points A(5, 4, -6) and B(3, 2, -4). (06 Marks)
 - b. If $\cos \alpha$, $\cos \beta$. $\cos \gamma$ are the direction cosines of a straight line, prove that (i) $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2$ (ii) $\cos 2\alpha + \cos 2\beta + \cos 2\gamma = -1$. (07 Marks)
 - c. Find the constant K such that the angle between the lines with direction ratios (-2, 1, -1) and (1, -K, 1) is 90°. (07 Marks)
- 2 a. Show that the angles between the diagonals of a cube is $\theta = \cos^{-1}(1/3)$. (06 Marks)
 - b. Find the equation of the plane through the points (1, 0, -1) and (3, 2, 2) and parallel to the line $\frac{x-1}{1} = \frac{1-y}{2} = \frac{z-2}{3}$. (07 Marks)
 - c. Show that the points A(-6, 3, 2), B(3, -2, 4), C(5, 7, 3) and D(-13, 17, -1) are coplanar. Also find the equation of the plane containing them. (07 Marks)
- 3 a. Find the angle between the vectors $\vec{a} = 2i + 6j + 3k$, $\vec{b} = 12i 4j + 3k$. (06 Marks)
 - b. Find the area of a parallelogram whose adjacent sides are i-2j+3k and 2i+j-4k.

 (07 Marks)
 - c. Find a unit vector perpendicular to both vectors $\vec{a} = 2i 3j + k$, $\vec{b} = 7i 5j + k$. (07 Marks)
- 4 a. Show that the four points whose position vectors are 3i-2j+4k, 6i+3j+k, 5i+7j+3k and 2i+2j+6k are coplanar. (06 Marks)
 - b. A particle moves along the curve $x = t^3 + 1$, $y = t^2$, z = 2t + 3 where t is the time. Find the components of velocity and acceleration at t = 1 in the direction of i + j + 3k. (07 Marks)
 - c. Find the directional derivative of $f(x, y, z) = xy^2 + yz^3$ at the point (2, -1, 1) in the direction of vector i + 2j + 2k. (07 Marks)
- 5 a. Find div F and curl F where $E = \operatorname{grad}(x^3 + y^3 + z^3 3xyz)$. (06 Marks)
 - b. Show that F = x(y-z)i + y(z-x)j + z(x-y)k is solenoidal. (07 Marks)
 - Find the constants a and b so that the vector $\vec{F} = (axy + z^3)\hat{i} + (3x^2 z)\hat{j} + (bxz^2 y)\hat{k}$ is irrotational. (07 Marks)
- 6 a. Find the Laplace transforms of $1+2t^3-4e^{3t}+5e^{-t}$. (07 Marks)
 - b. Find the Laplace transform of $t^2 \sin^2 t$. (07 Marks)
 - c. Find the Laplace transform of $\frac{\sin at}{t}$. (06 Marks)

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- 7 a. Find the inverse Laplace transform of $\frac{3s-4}{16-s^2}$. (06 Marks)
 - b. Find the inverse Laplace transform of $\frac{1}{s^2 + 4s + 9}$. (07 Marks)
 - c. Evaluate $L^{-1} \left\{ \frac{1}{(s+1)(s+2)} \right\}$. (07 Marks)
- 8 a. Obtain the Laplace transforms of f'(t), f"(t).
 b. Solve the differential equation using Laplace transforms y"-3y'+2y=1-e^{2t} under the conditions y(0) = 1, y'(0) = 0.
 (08 Marks)
 (12 Marks)