

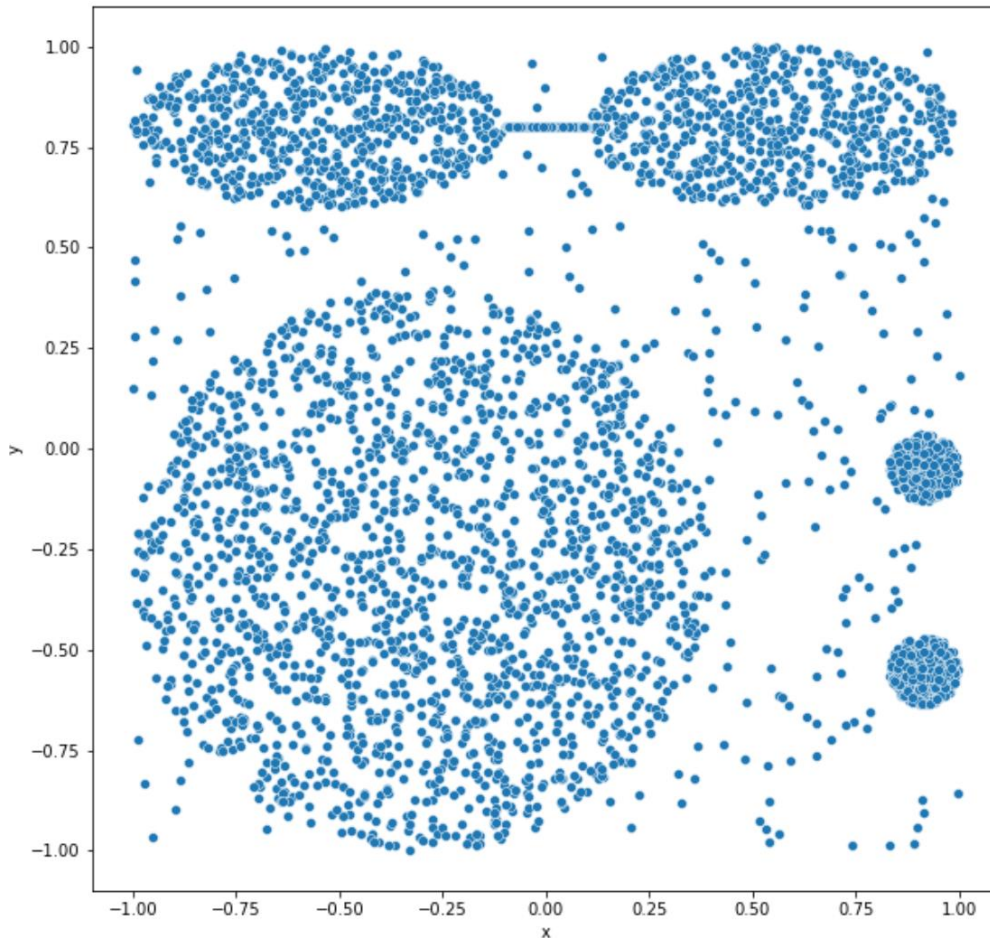
Homework Assignment 2

STAT430 Unsupervised Learning - Fall 2021

Due: Friday, September 10 on Compass

Question #1: [1.5 pt]

What type of cluster definition would be most useful in describing the five clusters represented in the plot shown below?



- * Clusters are well separated
- * There are two density based clusters
- * Dense clusters on bottom right confirm to prototype based cluster.

Question #2: [3 pt]

Calculate the silhouette score of object 5 using the information below. Then interpret what this silhouette score says about object 5 with respect to this clustering.

Data				Distance Object 5 is away from this object.
		x	y	
Cluster 1	Object 1	1	1	4.53
	Object 2	2	2	3.54
	Object 3	1	2	3.54
	Object 4	2	1	4.53
	Object 5	1.5	5.5	--
Cluster 2	Object 6	1	7	1.58
	Object 7	1	8	2.55
	Object 8	2	7	1.58
	Object 9	2	8	2.55
Cluster 3	Object 10	5	7	3.81
	Object 11	5	8	4.30
	Object 12	6	7	4.74
	Object 13	6	8	5.15

$$a_5 = (4.53 + 3.54 + 3.54 + 4.53) / 4 = 4.035$$

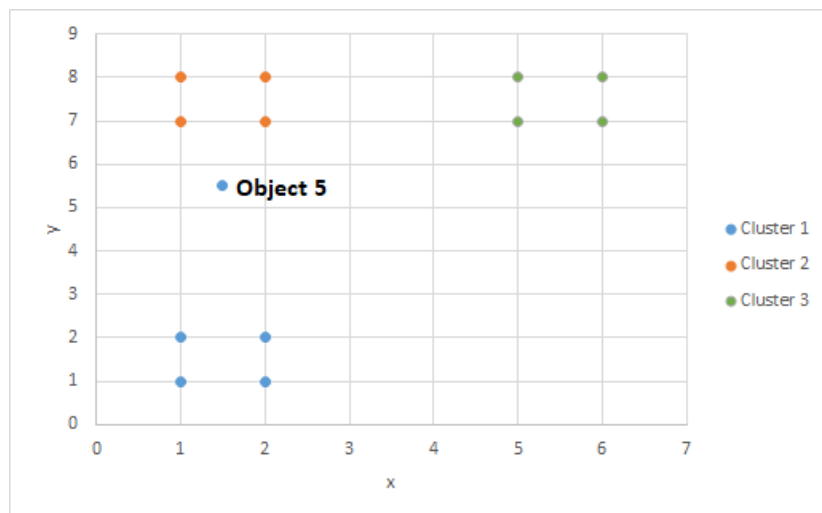
$$b_{5_orng} = (1.58 + 2.55 + 1.58 + 2.55) / 4 = 2.065$$

$$b_{5_grn} = (3.81 + 4.30 + 4.74 + 5.15) / 4 = 4.5$$

$$\text{Hence, } b_5 = 2.065$$

$$\text{Silhouette}_5 = (2.065 - 4.035) / 4.035 = -0.48823$$

* Silhouette score of object 5 is -0.48823. The object 5 is actually closer to cluster_2 (orange) than cluster_1 (blue).



Question #3: [2 pt]

Suppose we have a dataset comprised of three objects (*object 1*, *object 2*, and *object 3*). Each object has two dimensions (ie. x and y dimensions). Suppose we come up with a clustering that assigns *objects 1 and 2* to cluster 1 and *object 3* to cluster 2 (see below). Come up with an example of (x,y) values for *objects 1, 2, and 3* below such that *object 2* has a silhouette score of exactly 0. (Ie: fill in the blanks below).

Clustering:

Cluster 1:

Object 1: (x1 = 1 , y1 = 1)

Object 2: (x2 = 2 , y2 = 2)

Cluster 2:

Object 3: (x3 = 3 , y3 = 1)

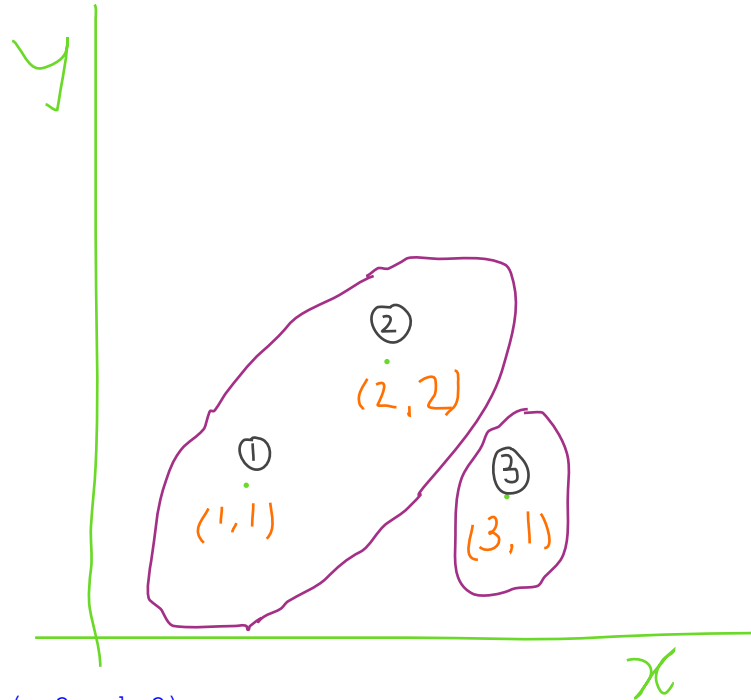
$$b_{2_1} = 1.414$$

$$b_{2_3} = 1.414$$

$$\text{Hence } b_2 = 1.414$$

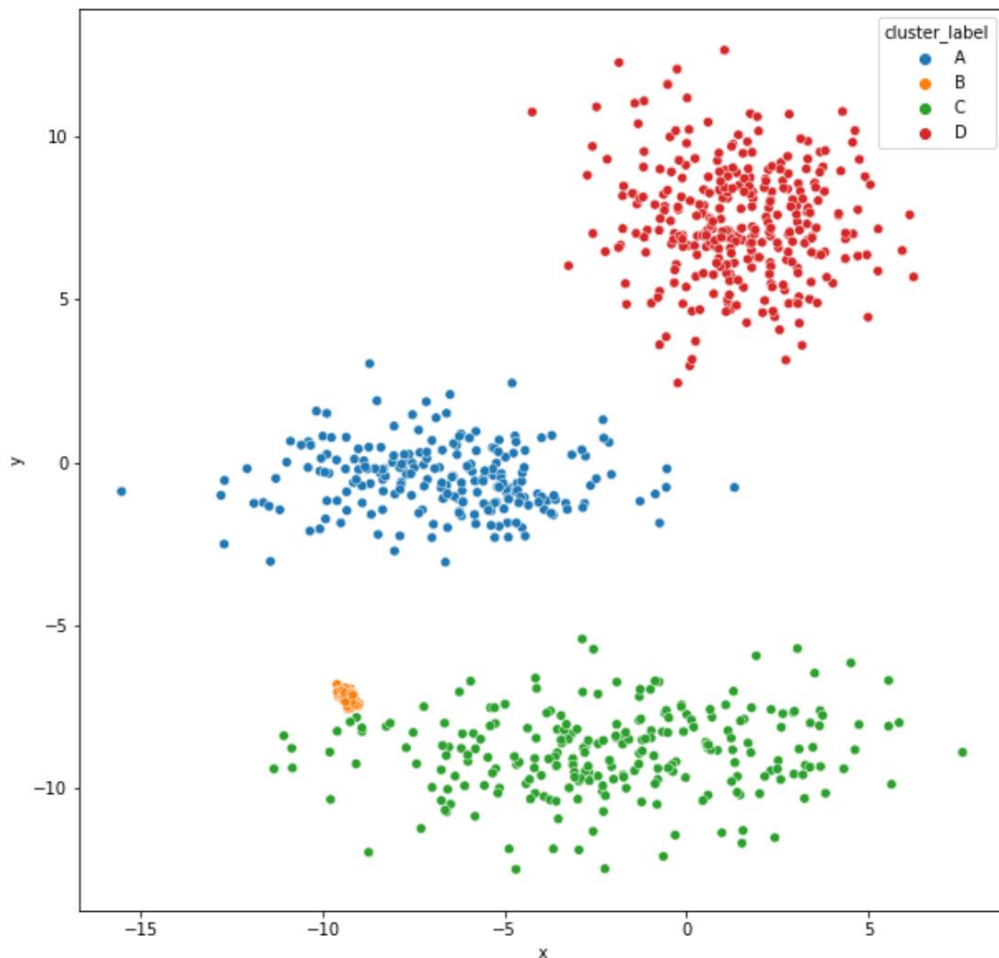
$$\text{Now, } a_2 = 1.414$$

$$\text{Hence Silhouette score of object 2 is zero. } (a_2 = b_2)$$



Question 4: [4 pt]

The silhouette plot below was created from the following clustering and dataset shown in the scatterplot below. Match the cluster labels (A-D) shown in the scatterplot to the corresponding cluster labels (0-3) in the silhouette plot. Explanations are not required, but may help with partial credit if you get something wrong.



C-1

> Some of the objects are very close to cluster B than C giving negative Silhouette for some objects

B-3

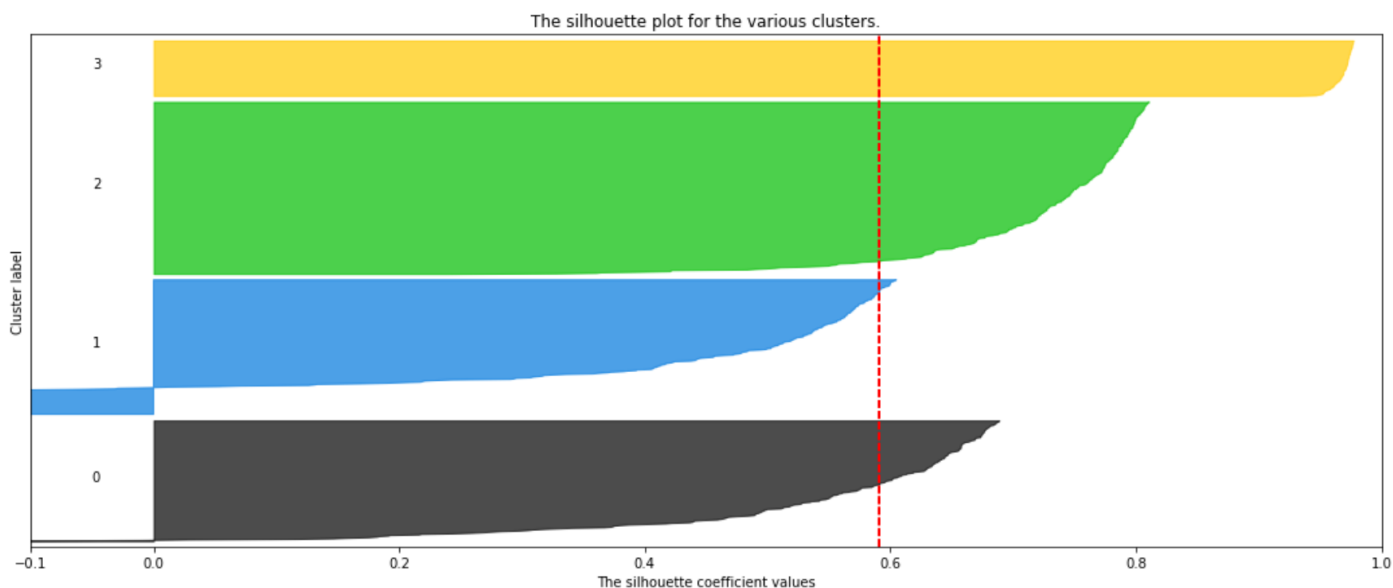
> All objects are tightly packed and closer to its centroid, giving Silhouette of ~1 for all objects

D-2

Has very similar looking plot with A. There are fewer objects away from its centroid and closer to other cluster compared to cluster A.

A-0

> Objects are scattered and away from centroid



Question #5:

1. Download the Assignment_02.zip file from Compass.
2. Edit the Jupyter notebook (.ipynb) file to complete/answer questions for question 5.
3. Submit your completed Jupyter notebook (.ipynb) file as well as any other files you used to answer Question 1-4 to compass.