

Accurate implementation of DeepMD-v2 potential calculation in HALMD for single species, extension to multi-species and Automatic-Differentiation-Based Force Computation

Sandip Sah

M.Sc. Computational Science, Freie Universität Berlin

January 07, 2026

Supervisor: Prof. Dr. Felix Höfling

1 Introduction

- Motivation
- Objectives and Scope

2 Background

- HALMD
- DeepMD v2

3 Potential computation

- Overview of Implementation
- Model Parameter Extraction
- Coordinate System Extension
- Construction of Configuration Matrix R
- Construction of embedding matrix G

- Descriptor Computation
- Potential Energy calculation
- summary of potential computation

4 Results

- Energy agreement: DeepMD vs. HALMD

5 Force Computation

- Overview
- Automatic differentiation
- Derivative of geometry matrix R
- Derivative of embedding matrix G
- descriptor derivative

6 Conclusion

- Classical potentials are efficient but inaccurate , while *ab initio* methods are accurate but computationally expensive [6, 7].
- Machine-learned potentials (e.g., DeepMD) achieve near-DFT accuracy at classical MD cost [1, 9].
- Current DeepMD–HALMD integration is inaccurate and limited to single-species systems [5].

Objectives and Scope

- Extend the DeepMD integration in HALMD beyond the single-species implementation of Cruz to full *multi-species DeepMD-v2* inference [5].
 - Implement the missing core components of the DeepMD-v2 pipeline:
 - periodic coordinate handling, ghost atoms, and multi-type neighbor lists,
 - species-dependent filter and descriptor networks,
 - normalization, scaling, smooth cutoffs, and force calculations.
- [9, 11].
- Focus on the **inference stage** (energy and force evaluation) for multi-component materials using the DeepPot-SE descriptor;
 - Model training and alternative descriptors are outside the scope.

HALMD: High-Accuracy Large-Scale MD Engine

- HALMD is a high-performance, open-source MD framework for large-scale simulations, optimized for numerical accuracy and GPU acceleration [4].
- Atomic motion follows Newton's equations of motion:

$$m_i \frac{d^2 \mathbf{r}_i}{dt^2} = -\nabla_i U(\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_N),$$

- Traditionally uses efficient interatomic potentials, but are limited for complex chemistry [6, 2].
- This thesis extends HALMD with multi-species DeepMD-v2 force fields, enabling near *ab initio* accuracy at classical MD cost [9, 11].

Neural Network Potentials and Deep Potential MD(DeepMD)-v2

- **Neural Network Potentials** learn interatomic interactions from *ab initio* data, achieving near-DFT accuracy at classical MD cost [1, 8].
- Energy is written as a sum of atomic contributions:

$$E = \sum_i E_i(\mathcal{R}_i), \quad (1)$$

ensuring locality and linear scaling [1].

- **DeepMD-v2**: modern NNP with smooth, symmetry-preserving descriptors, explicit multi-species support, and efficient GPU execution [9, 11].
- Species-specific embedding and fitting networks predict energies; forces follow from

$$\mathbf{F}_i = -\frac{\partial E}{\partial \mathbf{r}_i}. \quad (2)$$

Overview of Implementation

- DeepMD-v2 is integrated into HALMD through a modular, end-to-end inference pipeline.
- Model parameters are extracted from `frozen_model.pb` and `input.json` and converted into a compact HDF5 format for efficient loading.
- HALMD reconstructs local atomic environments using the exact DeepMD-v2 convention:
 - periodic coordinate wrapping,
 - ghost-cell extension,
 - species-ordered neighbor selection.
- From the reconstructed environment, HALMD computes descriptors and evaluates species-specific neural networks to obtain atomic energies and forces.

DeepMD–HALMD Energy Evaluation Pipeline

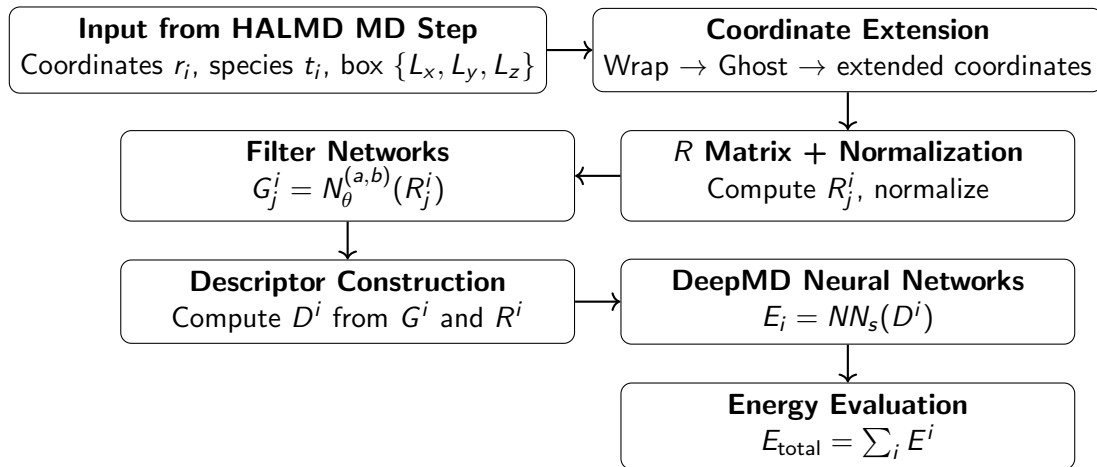


Figure: DeepMD–HALMD energy evaluation pipeline implemented in this thesis.

Model Parameter Extraction

- DeepMD-v2 models are stored as `frozen_model.pb` with hyperparameters in `input.json` [9, 11].
- All parameters are extracted from the TensorFlow graph and converted into a compact HDF5 format for efficient inference in HALMD.
- The extracted model contains:
 - descriptor attributes (cutoffs, normalization, species mapping),
 - species-dependent embedding (filter) networks,
 - species-dependent fitting networks,
 - final outputs: energies, forces, and virials.
- The hierarchical HDF5 model enables full multi-species DeepMD-v2 inference in HALMD, without TensorFlow, extending earlier single-species implementations [5].

Coordinate System Extension

- **Problem:** HALMD's native neighbor handling uses the *minimum-image convention*, sufficient for classical MD, but incompatible with DeepMD's descriptor construction [4, 9, 11].
- **DeepMD Requirement:** Descriptors are computed from *absolute atomic coordinates* inside the primary cell, requiring explicit:
 - coordinate wrapping,
 - ghost-cell periodic expansion,
 - species-aware neighbor organization,
 - descriptor normalization.
- **Implemented Solution:** A new DeePMD-style environment constructor that exactly reproduces the DeepMD-v2 preprocessing pipeline, replacing HALMD's original environment construction [5].
- **Impact:** Enables correct descriptor evaluation and full compatibility with multi-species DeepMD-v2 models.

Explicit Coordinate Wrapping

- DeepMD requires all atoms to be mapped into the primary cell using fractional coordinates:

$$\mathbf{s}_i = \mathbf{r}_i \mathbf{H}^{-1}, \quad \tilde{\mathbf{s}}_i = \mathbf{s}_i - \lfloor \mathbf{s}_i \rfloor, \quad \tilde{\mathbf{r}}_i = \tilde{\mathbf{s}}_i \mathbf{H}. \quad (3)$$

- This procedure is mandatory for general (non-orthorhombic) simulation cells and matches DeepMD's internal pipeline [9].

Explicit Coordinate Wrapping visualization

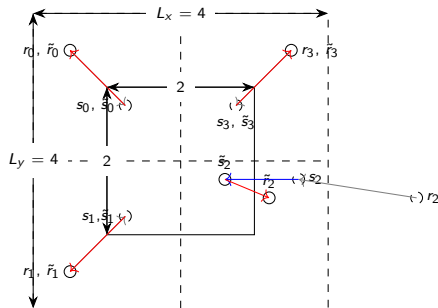


Figure: Explicit coordinate wrapping illustrated in stages: real coordinates r_i , fractional coordinates $s_i = \mathbf{r}_i \mathbf{H}^{-1}$, and wrapped fractional coordinates \tilde{s}_i .

Ghost-Cell Periodic Extension

- **Problem:** HALMD's neighbor list applies the minimum-image convention, which is sufficient for classical MD but does *not* provide the full periodic environment required by DeepMD descriptors [4, 9, 11].
- **DeepMD Requirement:** Every atom must retain a complete neighborhood within the cutoff radius r_c , including neighbors across periodic boundaries.
- **Implemented Solution:** Full **ghost-cell tiling** — explicit replication of the simulation cell in all spatial directions before neighbor construction.
- **Impact:** Ensures descriptor correctness and identical environments for atoms near boundaries and in the interior, enabling full DeepMD-v2 compatibility.

- Periodic images are generated from wrapped coordinates:

$$\mathbf{r}_i^{(s)} = \tilde{\mathbf{r}}_i + s_x L_x \mathbf{e}_x + s_y L_y \mathbf{e}_y + s_z L_z \mathbf{e}_z, \quad s_\alpha \in [-n_{\text{buff},\alpha}, n_{\text{buff},\alpha}] \quad (4)$$

- Buffer size ensures full cutoff coverage:

$$n_{\text{buff},\alpha} = \left\lceil \frac{r_c}{L_\alpha} \right\rceil$$

- For cubic cells with $n_{\text{buff}} = 1$: $3^3 = 27$ replicated cells.

Ghost-Cell construction visualization

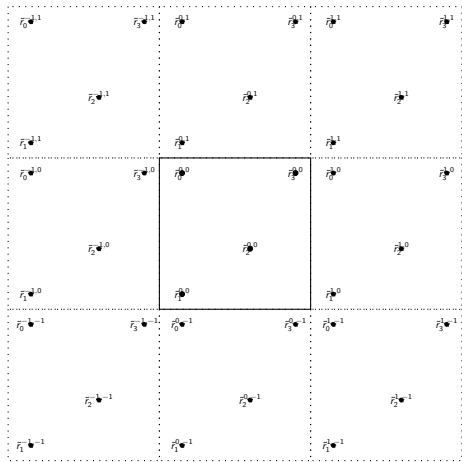


Figure: Periodic replication of the computational cell.

Construction of the Configuration Matrix R I

- **Inputs:** wrapped central coordinate $\tilde{\mathbf{r}}_i$ and ghost-cell neighbour images $\mathbf{r}_j^{(s)}$.

- **Relative displacement:**

$$\mathbf{r}_{ij} = \mathbf{r}_j^{(s)} - \tilde{\mathbf{r}}_i, \quad r_{ij} = \|\mathbf{r}_{ij}\|. \quad (5)$$

- **Smooth cutoff (DeepMD):**

$$s(r) = \begin{cases} \frac{1}{r}, & r < r_s, \\ \frac{1}{r} \left[x^3(-6x^2 + 15x - 10) + 1 \right], & r_s \leq r < r_c, \\ 0, & r \geq r_c, \end{cases} \quad x = \frac{r - r_s}{r_c - r_s}. \quad (6)$$

- **Neighbour feature row (4 components):**

$$(R^i)_j = \left[s(r_{ij}), s(r_{ij}) \frac{x_{ij}}{r_{ij}}, s(r_{ij}) \frac{y_{ij}}{r_{ij}}, s(r_{ij}) \frac{z_{ij}}{r_{ij}} \right]. \quad (7)$$

Construction of the Configuration Matrix R II

- **Species-fixed layout via sel:**

$$N_c^{(b)} = \text{max neighbour slots for species } b, \quad \text{sel} = [N_c^{(1)}, \dots, N_c^{(B)}], \quad (8)$$

$$N_c^{(\text{total})} = \sum_{b=1}^B N_c^{(b)}, \quad R^i \in \mathbb{R}^{N_c^{(\text{total})} \times 4}. \quad (9)$$

Neighbours are grouped by species and truncated/zero-padded to match sel.

- **Normalization (training statistics):**

$$\hat{R}_{k\alpha}^i = \frac{R_{k\alpha}^i - t_{\text{avg},\alpha}}{t_{\text{std},\alpha}}, \quad \hat{s}_{ij} = \hat{R}_{j,0}^i \text{ (input to embedding net)}. \quad (10)$$

Construction of the Embedding Matrix G

- The DeepPot-SE descriptor maps each normalized inverse distance

$$\hat{s}_{ij} = \hat{R}_{j,0}^i \quad (11)$$

to a learned embedding vector using a species-pair-specific filter network.

- For each central-neighbor species pair (a, b) , DeepMD-v2 defines a dedicated neural network

$$N_{\theta}^{(a,b)} : \mathbb{R} \rightarrow \mathbb{R}^M, \quad (12)$$

producing the embedding row

$$G_{j:}^i = N_{\theta}^{(a,b(j))}(\hat{s}_{ij}). \quad (13)$$

- All embedding rows are stacked to form

$$G^i \in \mathbb{R}^{N_c^{(\text{total})} \times M}, \quad N_c^{(\text{total})} = \sum_b N_c^{(b)}. \quad (14)$$

Construction of the Embedding Matrix G II

- Different neighbor species use different filter networks, enabling chemically accurate multi-species modeling.
- HALMD stores the full network family as

$$\text{networks}[a][b] \equiv N_{\theta}^{(a,b)}, \quad (15)$$

and selects the correct one at runtime for each neighbor.

Descriptor Computation I

- The DeepPot-SE descriptor combines geometric information \hat{R}^i and learned embeddings G^i to form the final descriptor D^i used to predict atomic energy.
- After neighbor construction, the normalized geometric matrix is

$$\hat{R}^i \in \mathbb{R}^{N_c^{(\text{total})} \times 4}, \quad (16)$$

containing inverse distances and angular components.

- Each row is embedded via a species-pair neural network:

$$G_{j:}^i = N_{\theta}^{(a,b(j))}(\hat{s}_{ij}), \quad G^i \in \mathbb{R}^{N_c^{(\text{total})} \times M}. \quad (17)$$

- The quadratic descriptor is then constructed as

$$D^i = \frac{1}{(N_c^{(\text{total})})^2} ((G^i)^T \hat{R}^i) ((\hat{R}^i)^T G^{i,\text{trunc}}). \quad (18)$$

- Flattening D^i produces the final descriptor vector

$$\mathbf{D}^i \in \mathbb{R}^{MM'}, \quad (19)$$

which is passed to the fitting network to predict energy and forces.

Potential Energy Evaluation I

- DeepMD expresses the total energy as a sum of atomic energies:

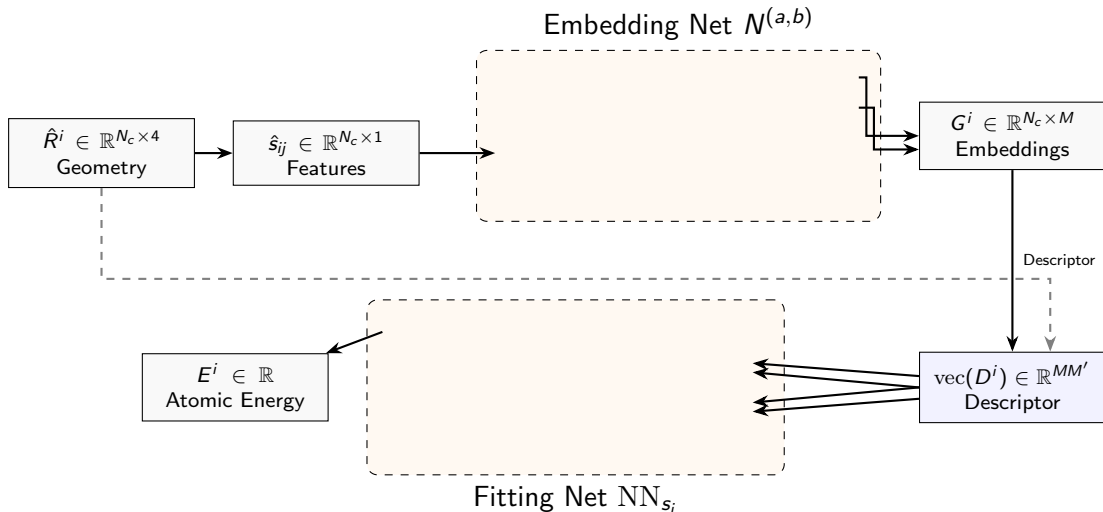
$$E_{\text{tot}} = \sum_{i=1}^N E^i. \quad (20)$$

- For each atom i of species s_i , the atomic energy is obtained from a **species-dependent fitting network**:

$$E^i = \text{NN}_{s_i}(\mathbf{D}^i) + b_{s_i}. \quad (21)$$

- DeepMD-v2 defines one fitting network per species; HALMD reconstructs all networks directly from the frozen TensorFlow graph.
- The descriptor vector \mathbf{D}^i is guaranteed to match the exact structure expected by each fitting network (ordering, dimension, normalization).
- The new HALMD implementation extends previous work from single-species to full **multi-species** DeepMD-v2 inference.

summary of potential computation



Energy Agreement

- HALMD reproduces DeepMD energies to single-precision floating-point accuracy.
- Verified for:
 - Cu (Model A) [3],
 - HEA [10],
 - Garnet [10],
 - Cu (Model B with different statistics) [10].
- Agreement holds across:
 - increasing system sizes,
 - chemically complex multi-species systems,
 - different normalization statistics.
- Confirms correctness of:
 - descriptor construction,
 - embedding networks,
 - fitting networks,
 - energy bias terms.

Energy Agreement Across All Models and Species

Model	Species	Atoms	DeepMD (eV)	HALMD (eV)	Match
Cu A	1	4	-6673.84	-6673.84	✓
Cu A	1	32	-53412.4	-53412.4	✓
Cu A	1	108	-180303	-180303	✓
Cu A	1	256	-427425	-427425	✓
Cu B	1	4	-7.7443	-7.7443	✓
Cu B	1	32	-89.4412	-89.4412	✓
Cu B	1	108	-335.96	-335.96	✓
Cu B	1	256	-836.414	-836.414	✓
HEA	5	16	-66.7551	-66.7551	✓
HEA	5	128	-895.498	-895.498	✓
HEA	5	432	-3490.86	-3490.86	✓
Garnet	5	161	-108445	-108445	✓

- Agreement holds for monoatomic and multi-species systems.
- Verified across different training statistics and descriptor normalizations.
- Confirms correctness of full DeepMD-v2 inference in HALMD.

- In DeepMD, atomic forces are obtained from the energy by

$$\mathbf{F}_i = -\frac{\partial E_{\text{tot}}}{\partial \mathbf{r}_i}. \quad (22)$$

- The total energy depends on atomic coordinates through multiple stages:

$$\mathbf{r} \rightarrow \hat{R} \rightarrow D \rightarrow E.$$

- Force evaluation therefore requires a structured application of the chain rule:

$$\frac{\partial E}{\partial \mathbf{r}} = \frac{\partial E}{\partial D} \frac{\partial D}{\partial \hat{R}} \frac{\partial \hat{R}}{\partial \mathbf{r}}. \quad (23)$$

- HALMD reproduces the DeepMD-v2 derivative pipeline by combining:
 - automatic differentiation for all neural networks,
 - analytic derivatives for geometric and descriptor operations.
- This yields forces that match DeepMD-v2 outputs to floating-point precision.

Automatic Differentiation (AD): How It Works

- **Automatic Differentiation (AD)** computes exact derivatives of a program by applying the chain rule to each elementary operation.
- Key insight: any computation can be decomposed into simple operations

$$+, \times, \sin, \cos, \dots$$

and the chain rule is applied locally to each operation.

- Example computation:

$$z = x y + \sin(x)$$

is evaluated as a sequence of primitives:

$$a = xy, \quad b = \sin(x), \quad z = a + b.$$

- AD differentiates this program automatically, without symbolic formulas and without numerical approximations.

- **Forward-mode AD**

- Propagates derivatives together with values.
- Each variable carries its derivative:

$$(x, \dot{x}), (y, \dot{y}), (a, \dot{a}), \dots$$

- One program run gives the derivative w.r.t. one input.
- Cost scales with number of inputs.

Forward-Mode AD: Worked Example I

Goal: Compute the derivative of

$$z = x y + \sin(x)$$

with respect to x .

Step 1: Decompose computation into primitives

$$a = x y$$

$$b = \sin(x)$$

$$z = a + b$$

Step 2: Attach derivatives to every variable

$$(x, \dot{x}), (y, \dot{y}), (a, \dot{a}), (b, \dot{b}), (z, \dot{z})$$

Forward-Mode AD: Worked Example II

Seed the input derivative:

$$\dot{x} = 1, \quad \dot{y} = 0.$$

Step 3: Propagate derivatives using chain rule

$$a = xy, \quad \dot{a} = y \dot{x} + x \dot{y} = y$$

$$b = \sin(x), \quad \dot{b} = \cos(x) \dot{x} = \cos(x)$$

$$z = a + b, \quad \dot{z} = \dot{a} + \dot{b} = y + \cos(x)$$

Result:

$$\boxed{\frac{\partial z}{\partial x} = y + \cos(x)}$$

AD: Reverse-Mode

- First run computes all intermediate values.
- Second run propagates sensitivities backward.
- One run yields the full gradient of a scalar output.
- Cost scales with number of outputs.

This makes reverse-mode AD ideal for

$$E = f(\mathbf{x}), \quad \mathbf{x} \in \mathbb{R}^n,$$

which is exactly the structure of neural networks.

Automatic Differentiation (AD) in HALMD

- DeepMD force evaluation requires derivatives through: geometry \rightarrow embedding \rightarrow descriptor \rightarrow fitting network.
- **Analytic derivatives** are used for all geometric operations.
- **Automatic differentiation** is used for all neural networks.
- **Current HALMD implementation: Forward-mode AD**

- Used for embedding networks:

$$\hat{s}_{ij} \rightarrow G_j^i, \quad \frac{\partial G_j^i}{\partial \hat{s}_{ij}}.$$

- Used in fitting network to compute

$$\frac{\partial E_i}{\partial D_{i,\alpha}}.$$

- HALMD uses a **hybrid strategy**: analytic geometry + AD for neural networks.

Derivatives of the Geometry Matrix R

- Forces require derivatives of each geometry row

$$\frac{\partial R_{j\alpha}^{(i)}}{\partial \mathbf{r}_i}. \quad (24)$$

- Each row depends on the relative displacement

$$\mathbf{r}_{ij} = \mathbf{r}_j - \mathbf{r}_i, \quad r_{ij} = \|\mathbf{r}_{ij}\|. \quad (25)$$

- Geometry features:

$$R_{j0}^{(i)} = s(r_{ij}), \quad R_{j\alpha}^{(i)} = s(r_{ij}) \frac{d_\alpha}{r_{ij}}. \quad (26)$$

- All derivatives follow directly from the multivariate chain rule.

Derivative of the Embedding Matrix G

- Each embedding row is produced by a species-dependent network:

$$G_{j\cdot}^{(i)} = N_{\theta}^{(a,b)}(\hat{s}_{ij}), \quad \hat{s}_{ij} = \hat{R}_{j0}^{(i)}. \quad (27)$$

- Therefore, $G^{(i)}$ depends on geometry only through the single scalar \hat{s}_{ij} .
- Its derivative reduces to a one-dimensional neural-network derivative:

$$\frac{\partial G_{jp}^{(i)}}{\partial \hat{R}_{j0}^{(i)}} = \frac{d N_{\theta,p}^{(a,b)}}{d \hat{s}}(\hat{s}_{ij}), \quad p = 1, \dots, M. \quad (28)$$

- All other geometric components do **not** affect G :

$$\frac{\partial G_{jp}^{(i)}}{\partial \hat{R}_{j\alpha}^{(i)}} = 0, \quad \alpha \neq 0. \quad (29)$$

Descriptor Structure and Construction

- For each atom i , the descriptor is built from:

$$\hat{R}^{(i)} \in \mathbb{R}^{N_c \times 4}, \quad G^{(i)} \in \mathbb{R}^{N_c \times M}.$$

- **Intermediate contraction:**

$$C^{(i)} = \frac{1}{N_c} (G^{(i)})^T \hat{R}^{(i)}, \quad C^{(i)} \in \mathbb{R}^{M \times 4}.$$

- **Quadratic, permutation-invariant descriptor:**

$$D_{\text{ext}}^{(i)} = C^{(i)} (C^{(i)})^T \in \mathbb{R}^{M \times M}.$$

- **Truncated descriptor used by the fitting network:**

$$D^{(i)} = D_{\text{ext}}^{(i)}[:, 1 : M'] = C^{(i)} (C^{(i)})^T P \in \mathbb{R}^{M \times M'}.$$

Descriptor Derivative: Key Structure

- Descriptor depends on geometry via two paths:

$$\hat{R}^i \rightarrow C^i \rightarrow D^i, \quad \hat{R}^i \rightarrow G^i \rightarrow C^i \rightarrow D^i.$$

- Matrix chain rule:

$$\frac{\partial \text{vec}(D^i)}{\partial \text{vec}(\hat{R}^i)} = \underbrace{\frac{\partial \text{vec}(D^i)}{\partial \text{vec}(G^i)} \frac{\partial \text{vec}(G^i)}{\partial s^i} \frac{\partial s^i}{\partial \text{vec}(\hat{R}^i)}}_{\text{embedding path}} + \underbrace{\frac{\partial \text{vec}(D^i)}{\partial \text{vec}(\hat{R}^i)}}_{\text{direct geometry path}}.$$

Fitting Network Derivative

- Atomic energy:

$$E^i = \text{NN}_{s_i}(\text{vec}(D^i))$$

- Jacobian required for forces:

$$J^i = \frac{\partial E^i}{\partial D^i} = \frac{\partial E^i}{\partial \text{vec}(D^i)} \in \mathbb{R}^{M \times M'}.$$

- Deep nonlinear mapping \rightarrow **automatic differentiation (AD)**.

Final Force Assembly

- Total force:

$$\mathbf{F}_i = - \sum_j \frac{\partial E^j}{\partial \mathbf{r}_i}.$$

- Final factored force expression:

$$\mathbf{F}_i = - \sum_j J^j \left(\underbrace{\frac{\partial \text{vec}(D_j)}{\partial \text{vec}(G_j)} \frac{\partial \text{vec}(G_j)}{\partial s_j}}_{\text{via embedding } (\hat{R} \rightarrow s \rightarrow G \rightarrow D)} \frac{\partial s_j}{\partial \text{vec}(\hat{R}_j)} + \underbrace{\frac{\partial \text{vec}(D_j)}{\partial \text{vec}(\hat{R}_j)}}_{\text{direct geometry } (\hat{R} \rightarrow D)} \right) \frac{\partial \text{vec}(\hat{R}_j)}{\partial \mathbf{r}_i}$$

Force Computation: Hybrid Structure

- **Neural part:**

$$\frac{\partial \text{vec}(D)}{\partial \text{vec}(G)}, \quad \frac{\partial \text{vec}(G)}{\partial s} \quad (\text{via AD})$$

- **Analytic geometry:**

$$\frac{\partial s}{\partial \text{vec}(\hat{R})}, \quad \frac{\partial \text{vec}(\hat{R})}{\partial \mathbf{r}}$$

- Fully explicit, stable and DeepMD-v2–equivalent force pipeline.

Conclusion & Outlook

- First fully explicit *DeepMD-v2 implementation in HALMD* with multi-species descriptors, energies, and force derivatives.
- Verified energy agreement for monoatomic and complex multi-species systems enables *accurate large-scale ML-driven molecular dynamics* without framework overhead.
- This work enables:
 - faster ML-based simulations,
 - improved HPC scalability,
 - closer integration of ML and physics-based modeling.
- With completed forces and further optimisation, HALMD can become a *high-performance platform for next-generation materials simulation*.

References I

- [1] Jörg Behler and Michele Parrinello. “Generalized neural-network representation of high-dimensional potential-energy surfaces”. In: *Physical Review Letters* 98.14 (2007), p. 146401. DOI: 10.1103/PhysRevLett.98.146401.
- [2] Donald W. Brenner et al. “A second-generation reactive empirical bond order (REBO) potential energy expression for hydrocarbons”. In: *Journal of Physics: Condensed Matter* 14.4 (2002), pp. 783–802. DOI: 10.1088/0953-8984/14/4/312.
- [3] Matteo Cioni, Daniela Polino, and Daniele Rapetti. *Cu_fcc_slabs Deep Potential Model*. www.aissquare.com/models/detail?pageType=models&name=Cu_fcc_slabs. Machine-learned interatomic potential trained with DeePMD-kit. 2023.
- [4] Peter H Colberg and Felix Höfling. “Highly accelerated simulations of glassy dynamics using GPUs: Caveats on limited floating-point precision”. In: *Computer Physics Communications* 182.5 (2011), pp. 1120–1129.

References II

- [5] Andres Cruz. “Deep Neural Networks Potentials for Scalable Molecular Dynamics Simulations on Accelerator Hardware”. *Master’s Thesis*. Freie Universität Berlin, Sept. 2025.
- [6] Murray S. Daw and Michael I. Baskes. “Embedded-atom method: Derivation and application to impurities, surfaces, and other defects in metals”. In: *Physical Review B* 29.12 (1984), pp. 6443–6453. DOI: 10.1103/PhysRevB.29.6443.
- [7] Dominik Marx and Jürg Hutter. *Ab initio molecular dynamics: basic theory and advanced methods*. Cambridge University Press, 2009.
- [8] Frank Noé et al. “Machine learning for molecular simulation”. In: *Annual review of physical chemistry* 71.1 (2020), pp. 361–390.
- [9] Han Wang, Linfeng Zhang, Jiequn Han, et al. “DeePMD-kit: A deep learning package for many-body potential energy representation and molecular dynamics”. In: *Computer Physics Communications* 228 (2018), pp. 178–184.

- [10] Jinzhe Zeng and Duo Zhang. *Data for DeePMD-kit v2 paper*.
<https://github.com/deepmodeling-activity/deepmd-kit-v2-paper>. Supporting data for: DeePMD-kit v2: A software package for deep potential models, J. Chem. Phys., 159, 054801 (2023). 2023.
- [11] Jinzhe Zeng et al. “DeePMD-kit v2: A software package for deep potential models”. In: *The Journal of Chemical Physics* 159.5 (2023).

Thank You!