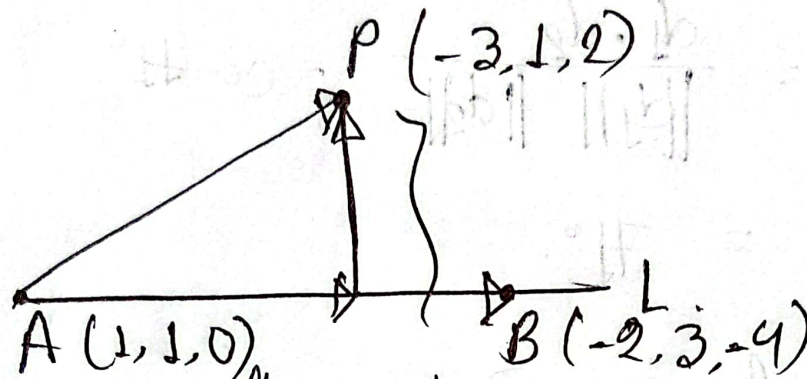


33.



Use the method of exercise 32 to find the distance from the point  $P(-3, 1, 2)$  to the line through  $A(1, 1, 0)$  and  $B(-2, 3, -4)$ .

$$\vec{AP} = -4\mathbf{i} + 2\mathbf{k}$$

$$\vec{AB} = -3\mathbf{i} + 2\mathbf{j} - 4\mathbf{k}$$

$$v = \text{Proj}_{\vec{AB}} \vec{AP}$$

(v.e.) 4

$$\begin{aligned} \text{Proj}_{\vec{AB}} \vec{AP} &= \left( \vec{AP} \cdot \frac{\vec{AB}}{\|\vec{AB}\|} \right) \frac{\vec{AB}}{\|\vec{AB}\|} \quad (-4\mathbf{i} + 2\mathbf{k}) - \\ &= \left( \frac{\vec{AP} \cdot \vec{AB}}{\|\vec{AB}\|^2} \right) \cdot \vec{AB} \quad \left( -\frac{12}{29}\mathbf{i} + \frac{8}{29}\mathbf{j} - \frac{16}{29}\mathbf{k} \right) \\ &= \frac{12 - 8}{29} \cdot (-3\mathbf{i} + 2\mathbf{j} - 4\mathbf{k}) \cdot \left( 2 + \frac{16}{29} \right) \end{aligned}$$