

1.

MP

$$MRTS = \frac{MP_L}{MP_K}$$

規模報酬

產量彈性

生產力彈性

替代彈性

$$(\sigma = \frac{d \ln \frac{K}{L}}{d \ln MRTS})$$

$$q = 5LK$$

$$MP_L = 5K$$

$$MP_K = 5L$$

$$\frac{K}{L}$$

IRS

$$\varepsilon_L = \varepsilon_K = 1$$

$$2$$

$$1$$

$$AP_L = 5K$$

$$AP_K = 5L$$

$$q = 2L + 3K$$

$$MP_L = 2$$

$$MP_K = 3$$

$$\frac{2}{3}$$

CRS

$$\varepsilon_L = \frac{2L}{2L+3K} \quad \varepsilon_K = \frac{3K}{2L+3K}$$

$$1$$

$$\infty$$

$$AP_L = \frac{2L+3K}{L}$$

$$AP_K = \frac{2L+3K}{K}$$

$$q = \min\{L, K\}$$

X

$$1, 0, \infty$$

CRS

X

$$1$$

$$0$$

$$q = (0.2L^{-\frac{1}{2}} + 0.8K^{-\frac{1}{2}})^{-2}$$

$$MP_L = 0.2L^{-\frac{3}{2}}(0.2L^{-\frac{1}{2}} + 0.8K^{-\frac{1}{2}})^{-3}$$

$$MP_K = 0.8K^{-\frac{3}{2}}(0.2L^{-\frac{1}{2}} + 0.8K^{-\frac{1}{2}})^{-3}$$

$$\frac{1}{4} \left(\frac{K}{L}\right)^{-1.5}$$

CRS

$$\varepsilon_L = 0.2L^{-\frac{1}{2}}(0.2L^{-\frac{1}{2}} + 0.8K^{-\frac{1}{2}})^{-1}$$

$$\varepsilon_K = 0.8K^{-\frac{1}{2}}(0.2L^{-\frac{1}{2}} + 0.8K^{-\frac{1}{2}})^{-1}$$

$$1$$

$$\frac{2}{3}$$

$$AP_L = \frac{(0.2L^{-\frac{1}{2}} + 0.8K^{-\frac{1}{2}})^{-2}}{L}$$

$$AP_K = \frac{(0.2L^{-\frac{1}{2}} + 0.8K^{-\frac{1}{2}})^{-2}}{K}$$

$$2. Q = 3K + 2L$$

$$(1) \quad \varepsilon_L = \frac{2L}{3K+2L}$$

$$\varepsilon_K = \frac{3K}{3K+2L}$$

$$\varepsilon^D = \varepsilon_L + \varepsilon_K = 1 \Rightarrow CRS.$$

$$(2) \quad MP_L = 2$$

$$MP_K = 3$$

為固定

$$(3) \quad MRTS = \frac{MP_L}{MP_K} = \frac{2}{3}$$

為固定.