

# Effective mass fitting strategy

1) Start with  $N$  configurations of the correlator  $C_n(t)$

2) Generate  $N_b$  bootstrap samples,  $C_b(t) = \frac{1}{N} \sum_{n=1}^N C_{\text{rand}(n)}(t)$

3) Compute effective mass for each bootstrap sample:  $E_b(t) = \frac{1}{t_J} \log \frac{C_b(t)}{C_b(t+t_J)}$   
and the mean value  $\bar{E}(t) = \frac{1}{N_b} \sum_{b=1}^{N_b} E_b(t)$

4) Compute covariance matrix  $\text{cov}(t, t') = \frac{N}{N-1} \frac{1}{N_b} \sum_{b=1}^{N_b} [E_b(t) - \bar{E}(t)] [E_b(t') - \bar{E}(t')]$

5) Fit the effective mass data with some function  $f(t) \overset{c}{\leftarrow} c + a e^{-bt}$  by minimizing  $\chi^2$ ,  
$$\chi^2 = \sum_{t, t'} [\bar{E}(t) - f(t)] (\text{cov}^{-1})_{tt'} [\bar{E}(t') - f(t')]$$
  
extract central values for the parameters  $\bar{c}$  or  $\{\bar{a}, \bar{b}, \bar{c}\}$

6) To obtain the uncertainty on the fitted parameters, repeat the fit but replace  $\bar{E}(t) \rightarrow E_b(t)$ :

$$\chi^2 = \sum_{t, t'} [E_b(t) - f(t)] (\text{cov}^{-1})_{tt'} [E_b(t') - f(t')]$$

and we will obtain  $N_b$  values for  $\{c\}$  or  $\{a, b, c\}$ . Then, the 1-sigma error bars on

the parameters will be obtained as  $\sigma_c = \frac{q_{5/6}(\{c\} - \bar{c}) - q_{1/6}(\{c\} - \bar{c})}{2}$

when  $q_{5/6}$  and  $q_{1/6}$  are the  $\frac{5}{6}$ th and  $\frac{1}{6}$ th quantiles.

7) Repeat steps 4)-6) for different  $\{t, t'\}$ , and then choose your central value and statistical error from the result with best  $\chi^2_{\text{dof}}$ , and the systematic error as the max difference between the central value and the results from different  $\{t, t'\}$ .

