

Test Two Review

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Kernels

- The kernel trick

- doesn't depend on actual values of features – just ordering within each feature

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- With bagging, how can we get an estimate of test performance while still using all our data for training?
 - “out-of-bag” error

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 - True, if you map the output to $\{-1, 1\}$ with a modified sign function.
- T/F: We can view AdaBoost a method for minimizing the exponential loss using forward stagewise additive modeling.
 - True

Gradient Boosting

- Know how to do gradient boosting with a new loss function and a black box regression algorithm.

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- go through examples in slides (Poisson regression, Gaussian regression, binomial, multinomial)

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- note that you can use these same losses for gradient boosting

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- What can we use for f ?

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- Likelihood of $y | x$ is then

$$p_w(y | x) = \exp(w^T x) e^{-\exp(w^T x)y}$$

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- Log-likelihood of $y \mid x$ is then

$$\begin{aligned} p_w(y|x) &= \exp(w^T x) e^{-\exp(w^T x)y} \\ \implies \log p_w(y|x) &= w^T x - y \exp(w^T x) \end{aligned}$$

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- Log-likelihood of $(x_1, y_1), \dots, (x_n, y_n)$ is

$$\sum_{i=1}^n [w^T x_i - y_i \exp(w^T x_i)]$$

- MLE is then

$$\hat{w}_{\text{MLE}} = \arg \max_{w \in \mathbf{R}^d} \sum_{i=1}^n [w^T x_i - y_i \exp(w^T x_i)]$$

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- Differentiate w.r.t. $g(x_i)$... etc...