# Stan code for Husain et al paper, PLoS ONE 2014

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# 1 Paper reference

This code is for the paper:

Samar Husain, Shravan Vasishth, and Narayanan Srinivasan. Strong Expectations Cancel Locality Effects: Evidence from Hindi. PLoS ONE, 9(7):1-14, 2014.

Available from: http://tinyurl.com/pnaykvs.

### 2 Abstract

Expectation-driven facilitation (Hale, 2001; Levy, 2008) and locality-driven retrieval difficulty (Gibson, 1998, 2000; Lewis & Vasishth, 2005) are widely recognized to be two critical factors in incremental sentence processing; there is accumulating evidence that both can influence processing difficulty. However, it is unclear whether and how expectations and memory interact. We first confirm a key prediction of the expectation account: a Hindi self-paced reading study shows that when an expectation for an upcoming part of speech is dashed, building a rarer structure consumes more processing time than building a less rare structure. This is a strong validation of the expectation-based account. In a second study, we show that when expectation is strong, i.e., when a particular verb is predicted, strong facilitation effects are seen when the appearance of the verb is delayed; however, when expectation is weak, i.e., when only the part of speech  $\hat{a}AIJverb\hat{a}AI$  is predicted but a particular verb is not predicted, the facilitation disappears and a tendency towards a locality effect is seen. The interaction seen between expectation strength and distance shows that strong expectations cancel locality effects, and that weak expectations allow locality effects to emerge.

#### 3 Session Info

- R version 3.1.1 (2014-07-10), x86\_64-apple-darwin13.1.0
- Locale:
   en\_US.UTF-8/en\_US.UTF-8/en\_US.UTF-8/C/en\_US.UTF-8/en\_US.UTF-8

- Base packages:
- $\bullet$  Other packages: rstan 2.4.0
- Loaded via a namespace (and not attached): base 3.1.1, datasets 3.1.1, graphics 3.1.1, grDevices 3.1.1, inline 0.3.13, methods 3.1.1, Rcpp 0.11.2, stats 3.1.1, stats4 3.1.1, tools 3.1.1, utils 3.1.1

# 4 Experiment 1

### 4.1 Data preparation

Load data and format for Stan:

### 4.2 Define model (method 1)

```
> expt1_code <-
+ 'data {
+ int<lower=1> N;
+ real lrt[N];
                                    //outcome
+ real<lower=-1,upper=1> dist[N];
                                   //predictor
                                    //predictor
+ real rctype[N];
+ real interaction[N];
                                    //predictor
+ int<lower=1> I;
                                    //number of subjects
+ int<lower=1> K;
                                    //number of items
+ int<lower=1, upper=I> subj[N];
                                    //subject id
+ int<lower=1, upper=K> item[N];
                                    //item id
+ vector[4] mu_prior;
                                    //vector of zeros passed in from R
+ }
+ transformed data {
+ real ZERO;
                                   // like #define ZERO 0 in C/C++
+ ZERO <- 0.0;
+ }
```

```
+ parameters {
+ vector[4] beta;
                                  // intercept and slope
+ vector[4] u[I];
                                  // random intercept and slopes subj
+ vector[4] w[K];
+ real<lower=0> sigma_e;
                                  // residual sd
+ vector<lower=0>[4] sigma_u;
                                // subj sd
+ vector<lower=0>[4] sigma_w;
                                 // item sd
+ corr_matrix[4] Omega_u;
                                  // correlation matrix for random intercepts and slopes a
+ corr_matrix[4] Omega_w;
                                   // correlation matrix for random intercepts and slopes
+ }
+ transformed parameters {
+ matrix[4,4] D_u;
+ matrix[4,4] D_w;
+ D_u <- diag_matrix(sigma_u);
+ D_w <- diag_matrix(sigma_w);
+ }
+ model {
+ matrix[4,4] L_u;
+ matrix[4,4] DL_u;
+ matrix[4,4] L_w;
+ matrix[4,4] DL_w;
+ real mu[N]; // mu for likelihood
+ //priors:
+ beta ~ normal(0,10);
+ sigma_e ~ normal(0,10);
+ sigma_u ~ normal(0,10);
+ sigma_w ~ normal(0,10);
+ Omega_u ~ lkj_corr(4.0);
+ Omega_w ~ lkj_corr(4.0);
+ L_u <- cholesky_decompose(Omega_u);
+ L_w <- cholesky_decompose(Omega_w);
+ for (m in 1:4) {
+ for (n in 1:m) {
+ DL_u[m,n] <- L_u[m,n] * sigma_u[m];
+ }
+ for (m in 1:4){
+ for (n in (m+1):4){
+ DL_u[m,n] <- ZERO;
+ }
+ }
+ for (m in 1:4){
+ for (n in 1:m){
+ DL_w[m,n] <- L_w[m,n] * sigma_w[m];
+ }
+ }
```

```
+ for (m in 1:4){
+ for (n in (m+1):4){
+ DL_w[m,n] <- ZERO;
+ }
+ }
+ for (i in 1:I)
                                                                                    // loop for subj random effects
+ u[i] ~ multi_normal_cholesky(mu_prior, DL_u);
+ for (k in 1:K)
                                                                                    // loop for item random effects
+ w[k] ~ multi_normal_cholesky(mu_prior, DL_w);
+ for (n in 1:N) {
+ mu[n] \leftarrow beta[1] + beta[2]*dist[n] + beta[3]*rctype[n] + beta[4]*interaction[n] + u[subj[n] + u[subj[n
                                                                                      // likelihood
+ lrt ~ normal(mu,sigma_e);
+ }
+ generated quantities {
+ cov_matrix[4] Sigma_u;
+ cov_matrix[4] Sigma_w;
+ Sigma_u <- D_u * Omega_u * D_u;
+ Sigma_w <- D_w * Omega_w * D_w;
+ }
+ '
      Fit data:
> set_cppo('fast')
> fit <- stan(model_code = expt1_code, data = e1data,
                                   iter = 500, chains = 4)
TRANSLATING MODEL 'expt1_code' FROM Stan CODE TO C++ CODE NOW.
COMPILING THE C++ CODE FOR MODEL 'expt1_code' NOW.
SAMPLING FOR MODEL 'expt1_code' NOW (CHAIN 1).
Iteration:
                               1 / 500 [ 0%]
                                                                        (Warmup)
Iteration: 50 / 500 [ 10%]
                                                                        (Warmup)
Iteration: 100 / 500 [ 20%]
                                                                       (Warmup)
Iteration: 150 / 500 [ 30%]
                                                                     (Warmup)
Iteration: 200 / 500 [ 40%] (Warmup)
Iteration: 250 / 500 [ 50%]
                                                                        (Warmup)
Iteration: 251 / 500 [ 50%]
                                                                       (Sampling)
Iteration: 300 / 500 [ 60%]
                                                                        (Sampling)
Iteration: 350 / 500 [ 70%]
                                                                        (Sampling)
Iteration: 400 / 500 [ 80%]
                                                                        (Sampling)
Iteration: 450 / 500 [ 90%]
                                                                        (Sampling)
Iteration: 500 / 500 [100%]
                                                                        (Sampling)
# Elapsed Time: 12.7522 seconds (Warm-up)
                                          5.3349 seconds (Sampling)
```

```
SAMPLING FOR MODEL 'expt1_code' NOW (CHAIN 2).
Iteration:
             1 / 500 [ 0%]
                              (Warmup)
Iteration: 50 / 500 [ 10%]
                              (Warmup)
Iteration: 100 / 500 [ 20%]
                              (Warmup)
Iteration: 150 / 500 [ 30%]
                              (Warmup)
Iteration: 200 / 500 [ 40%]
                              (Warmup)
Iteration: 250 / 500 [ 50%]
                              (Warmup)
Iteration: 251 / 500 [ 50%]
                              (Sampling)
Iteration: 300 / 500 [ 60%]
                              (Sampling)
Iteration: 350 / 500 [ 70%]
                              (Sampling)
Iteration: 400 / 500 [ 80%]
                              (Sampling)
Iteration: 450 / 500 [ 90%]
                              (Sampling)
Iteration: 500 / 500 [100%]
                              (Sampling)
  Elapsed Time: 14.4072 seconds (Warm-up)
#
                 24.3153 seconds (Sampling)
#
                 38.7225 seconds (Total)
SAMPLING FOR MODEL 'expt1_code' NOW (CHAIN 3).
             1 / 500 [ 0%]
Iteration:
                              (Warmup)
Iteration: 50 / 500 [ 10%]
                              (Warmup)
Iteration: 100 / 500 [ 20%]
                              (Warmup)
Iteration: 150 / 500 [ 30%]
                              (Warmup)
Iteration: 200 / 500 [ 40%]
                              (Warmup)
Iteration: 250 / 500 [ 50%]
                              (Warmup)
Iteration: 251 / 500 [ 50%]
                              (Sampling)
Iteration: 300 / 500 [ 60%]
                              (Sampling)
Iteration: 350 / 500 [ 70%]
                              (Sampling)
Iteration: 400 / 500 [ 80%]
                              (Sampling)
Iteration: 450 / 500 [ 90%]
                              (Sampling)
Iteration: 500 / 500 [100%]
                              (Sampling)
  Elapsed Time: 10.2164 seconds (Warm-up)
```

18.0871 seconds (Total)

#

#

#

#### SAMPLING FOR MODEL 'expt1\_code' NOW (CHAIN 4).

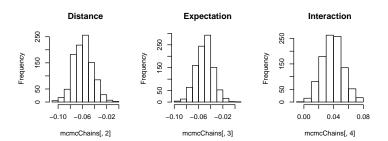
```
Iteration: 1 / 500 [ 0%] (Warmup)
Iteration: 50 / 500 [ 10%] (Warmup)
Iteration: 100 / 500 [ 20%] (Warmup)
```

10.2089 seconds (Sampling)

20.4253 seconds (Total)

```
Iteration: 150 / 500 [ 30%]
                              (Warmup)
Iteration: 200 / 500 [ 40%]
                              (Warmup)
Iteration: 250 / 500 [ 50%]
                              (Warmup)
Iteration: 251 / 500 [ 50%]
                              (Sampling)
Iteration: 300 / 500 [ 60%]
                              (Sampling)
Iteration: 350 / 500 [ 70%]
                              (Sampling)
Iteration: 400 / 500 [ 80%]
                              (Sampling)
Iteration: 450 / 500 [ 90%]
                              (Sampling)
Iteration: 500 / 500 [100%]
                              (Sampling)
   Elapsed Time: 10.877 seconds (Warm-up)
#
                 10.9669 seconds (Sampling)
#
                 21.844 seconds (Total)
> ## not run, too verbose:
> #print(fit)
```

Plot the posterior distributions of the three coefficients of interest:



# 4.3 Run model (Method 2)

- > library(parallel)
- > ## uncomment to save results to a file:
- > #sink("expt1resultsrun2.txt")

```
> ## the model is defined in a separate file:
> e1.sm <- stan_model("expt1subjitem.stan", model_name = "e1subjitem")</pre>
TRANSLATING MODEL 'e1subjitem' FROM Stan CODE TO C++ CODE NOW.
COMPILING THE C++ CODE FOR MODEL 'e1subjitem' NOW.
> sflist <- mclapply(1:4, mc.cores = detectCores(),
                    function(i) sampling(e1.sm, data = e1data,
                                         chains = 1, chain_id = i,
                                         seed = 12345))
> e1.sf <- sflist2stanfit(sflist)</pre>
> #print(e1.sf,digits=4)
  Comparison with lmer:
> library(lme4)
> m1<-lmer(lrt~dist+RCType+int+(1+dist+RCType+int|subj)+(1+dist+RCType+int|item),RC1)
> summary(m1)
Linear mixed model fit by REML ['lmerMod']
Formula: lrt ~ dist + RCType + int + (1 + dist + RCType + int | subj) +
    (1 + dist + RCType + int | item)
  Data: RC1
REML criterion at convergence: 2051.9
Scaled residuals:
   Min 1Q Median
                            3Q
                                   Max
-5.6366 -0.6089 -0.1853 0.4630 4.6925
Random effects:
Groups
         Name
                     Variance Std.Dev. Corr
subj
         (Intercept) 0.0901560 0.30026
         dist
                     0.0031861 0.05645 -0.60
                     0.0005826 0.02414 -0.56 0.70
         RCType
                     int
 item
         (Intercept) 0.0034894 0.05907
                     0.0018261 0.04273 -0.39
         dist
                                       0.60 -0.35
         RCType
                     0.0007440 0.02728
                     0.0010803 0.03287 -0.61 -0.38 0.05
         int
                     0.2089150 0.45707
Residual
Number of obs: 1440, groups: subj, 60; item, 24
Fixed effects:
           Estimate Std. Error t value
(Intercept) 6.65832
                      0.04234 157.24
```

```
dist
            -0.05746
                         0.01656
                                   -3.47
            -0.04974
                         0.01363
                                   -3.65
RCType
int
             0.03712
                         0.01487
                                    2.50
Correlation of Fixed Effects:
       (Intr) dist
                     RCType
dist
       -0.301
RCType -0.047 -0.005
        0.176 -0.245 -0.067
```

# 5 Experiment 2

### 5.1 Data preparation

Load data:

#### 5.2 Define model

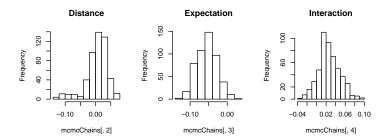
```
> expt2_code <-'
+ data {
      int<lower=0> N;
                                        //outcome
      real lrt[N];
+ real dist[N];
                                     //predictor
+ real expectation[N];
                                            //predictor
+ real interaction[N];
                                            //predictor
                                   //number of subjects
+ int<lower=1> I;
+ int<lower=1> K;
                                   //number of items
+ int<lower=1, upper=I> subj[N];
                                     //subject id
+ int<lower=1, upper=K> item[N];
                                     //item id
+ vector[4] mu_prior;
                                   //vector of zeros passed in from R
+ transformed data {
                                  // like #define ZERO 0 in C/C++
+ real ZERO;
```

```
+ ZERO <- 0.0;
+ }
+ parameters {
+ vector[4] beta;
                                  // intercept and slope
+ vector[4] u[I];
                                  // random intercept and slopes subj
+ vector[4] w[K];
+ real<lower=0> sigma_e;
                                  // residual sd
+ vector<lower=0>[4] sigma_u;
                                // subj sd
+ vector<lower=0>[4] sigma_w;
                                // item sd
                                  // correlation matrix for random intercepts and slopes a
+ corr_matrix[4] Omega_u;
+ corr_matrix[4] Omega_w;
                                  // correlation matrix for random intercepts and slopes :
+ }
+ transformed parameters {
+ matrix[4,4] D_u;
+ matrix[4,4] D_w;
+ D_u <- diag_matrix(sigma_u);
+ D_w <- diag_matrix(sigma_w);
+ }
+ model {
+ matrix[4,4] L_u;
+ matrix[4,4] DL_u;
+ matrix[4,4] L_w;
+ matrix[4,4] DL_w;
+ real mu[N]; // mu for likelihood
+ //priors:
+ beta ~ normal(0,10);
+ sigma_e ~ normal(0,10);
+ sigma_u ~ normal(0,10);
+ sigma_w ~ normal(0,10);
+ Omega_u ~ lkj_corr(4.0);
+ Omega_w ~ lkj_corr(4.0);
+ L_u <- cholesky_decompose(Omega_u);
+ L_w <- cholesky_decompose(Omega_w);
+ for (m in 1:4) {
+ for (n in 1:m) {
+ DL_u[m,n] <- L_u[m,n] * sigma_u[m];
+ }
+ }
+ for (m in 1:4){
+ for (n in (m+1):4){
+ DL_u[m,n] <- ZERO;
+ }
+ }
+ for (m in 1:4){
+ for (n in 1:m){
+ DL_w[m,n] <- L_w[m,n] * sigma_w[m];
```

```
+ }
+ }
+ for (m in 1:4){
+ for (n in (m+1):4){
+ DL_w[m,n] <- ZERO;
+ }
+ }
+ for (i in 1:I)
                                                                                      // loop for subj random effects
+ u[i] ~ multi_normal_cholesky(mu_prior, DL_u);
+ for (k in 1:K)
                                                                                      // loop for item random effects
+ w[k] ~ multi_normal_cholesky(mu_prior, DL_w);
+ for (n in 1:N) {
+ mu[n] \leftarrow beta[1] + beta[2]*dist[n] + beta[3]*expectation[n] + beta[4]*interaction[n]
+ + u[subj[n], 1] + u[subj[n], 2]*dist[n] + u[subj[n], 3]*expectation[n] + u[subj[n], 4]*interpolation for the subject of th
+ }
+ lrt ~ normal(mu,sigma_e);
                                                                                        // likelihood
+ }
+ generated quantities {
+ cov_matrix[4] Sigma_u;
+ cov_matrix[4] Sigma_w;
+ Sigma_u <- D_u * Omega_u * D_u;
+ Sigma_w <- D_w * Omega_w * D_w;
+ }
+ '
              Run model (Method 1)
> set_cppo('fast')
> fit <- stan(model_code = expt2_code, data = e2data,</pre>
                                   iter = 500, chains = 2)
TRANSLATING MODEL 'expt2_code' FROM Stan CODE TO C++ CODE NOW.
COMPILING THE C++ CODE FOR MODEL 'expt2_code' NOW.
SAMPLING FOR MODEL 'expt2_code' NOW (CHAIN 1).
                                1 / 500 [ 0%]
Iteration:
                                                                          (Warmup)
Iteration: 50 / 500 [ 10%]
                                                                         (Warmup)
Iteration: 100 / 500 [ 20%]
                                                                          (Warmup)
Iteration: 150 / 500 [ 30%]
                                                                          (Warmup)
Iteration: 200 / 500 [ 40%]
                                                                          (Warmup)
Iteration: 250 / 500 [ 50%]
                                                                          (Warmup)
Iteration: 251 / 500 [ 50%]
                                                                          (Sampling)
Iteration: 300 / 500 [ 60%]
                                                                          (Sampling)
Iteration: 350 / 500 [ 70%]
                                                                          (Sampling)
Iteration: 400 / 500 [ 80%]
                                                                         (Sampling)
```

```
Iteration: 450 / 500 [ 90%]
                              (Sampling)
Iteration: 500 / 500 [100%]
                              (Sampling)
  Elapsed Time: 5.85641 seconds (Warm-up)
#
                 4.26557 seconds (Sampling)
#
                 10.122 seconds (Total)
SAMPLING FOR MODEL 'expt2_code' NOW (CHAIN 2).
                              (Warmup)
Iteration:
             1 / 500 [ 0%]
Iteration: 50 / 500 [ 10%]
                              (Warmup)
Iteration: 100 / 500 [ 20%]
                              (Warmup)
Iteration: 150 / 500 [ 30%]
                              (Warmup)
                              (Warmup)
Iteration: 200 / 500 [ 40%]
Iteration: 250 / 500 [ 50%]
                              (Warmup)
Iteration: 251 / 500 [ 50%]
                              (Sampling)
Iteration: 300 / 500 [ 60%]
                              (Sampling)
Iteration: 350 / 500 [ 70%]
                              (Sampling)
Iteration: 400 / 500 [ 80%]
                              (Sampling)
Iteration: 450 / 500 [ 90%]
                              (Sampling)
Iteration: 500 / 500 [100%]
                              (Sampling)
  Elapsed Time: 5.76126 seconds (Warm-up)
                 3.07824 seconds (Sampling)
#
                 8.8395 seconds (Total)
```

Plot posterior distributions:



## 5.4 Run model (Method 2)