

# Uncertainty in Neural Network Word Embedding: Exploration of Threshold for Similarity

NeuIR at SIGIR, 21st July 2016

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### Similar Terms

#### book

books	0.82
foreword	0.77
author	0.74
published	0.73
preface	0.69
republished	0.68
reprinted	0.68
afterword	0.67
memoir	0.67

#### dwarfish

corpulent	0.44
hideous	0.43
unintelligen	0.42
wizened	0.42
catoblepas	0.42
creature	0.42
humanoid	0.41
grotesquely	0.41
tomtar	0.41

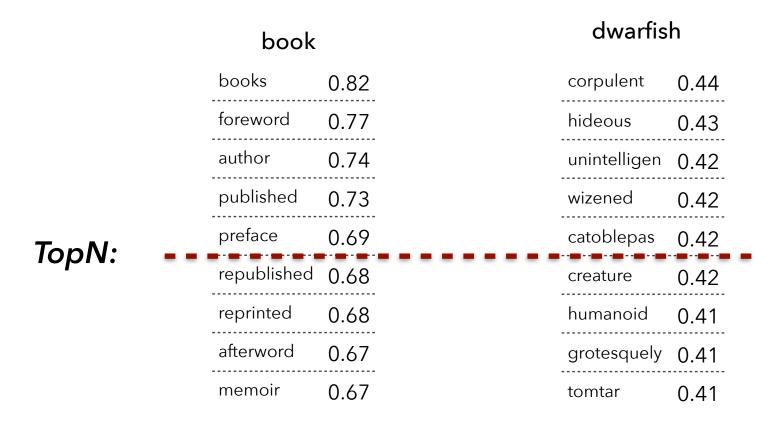


### Similar Terms

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### 🔛 Similar Terms



Using *threshold* in SIGIR 2016, tuned by brute-force search:

Scalable Semantic Matching of Queries to Ads in Sponsored Search Advertising. Mihajlo Grbovic et al.

Robust and Collective Entity Disambiguation through Semantic Embeddings. Stefan Zwicklbauer et al.





### Contribution

#### Our Contribution

- Analytical exploration of a general threshold on term similarity
  - Defined for all the terms in the lexicon
  - Tested on Ad Hoc retrieval
- Showing the advantage of threshold-based rather than TopNbased approach



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#### Roadmap

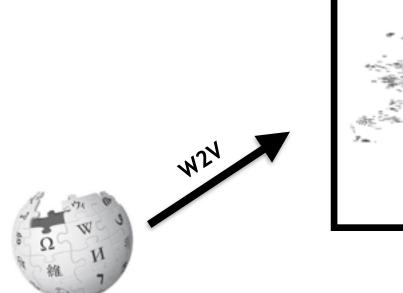
- Uncertainty in NN-based word embeddings
- Similarity distribution
- Proposing threshold
- Experiments

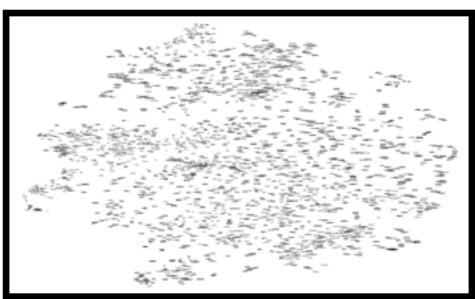




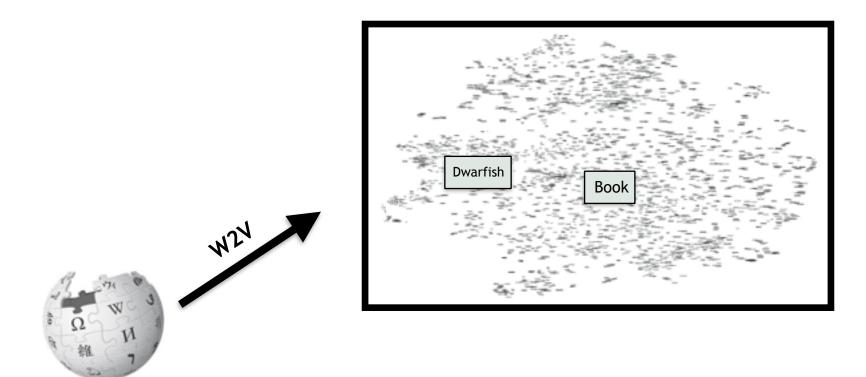




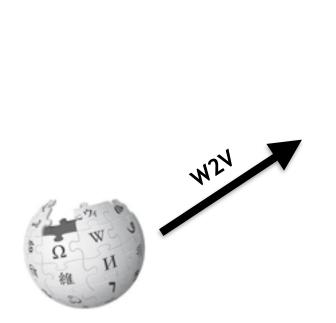


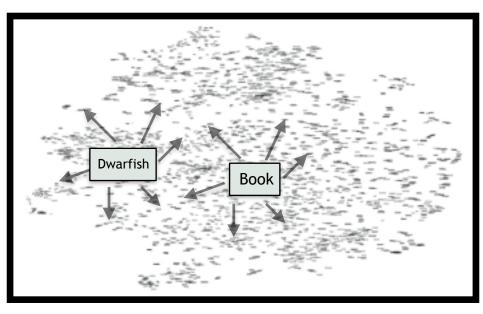




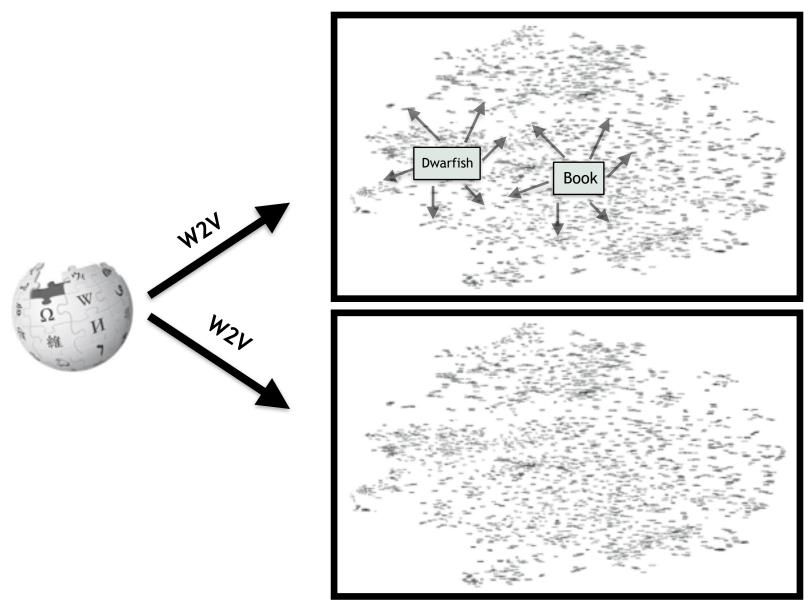




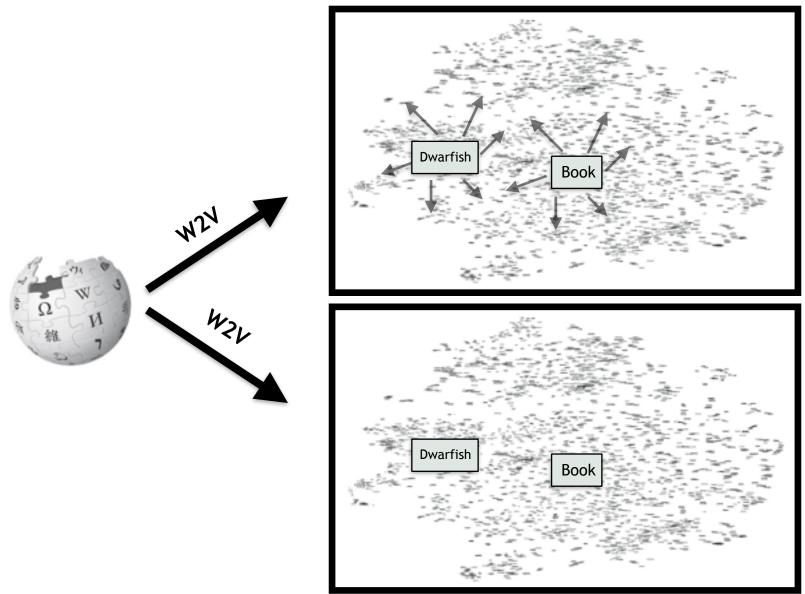




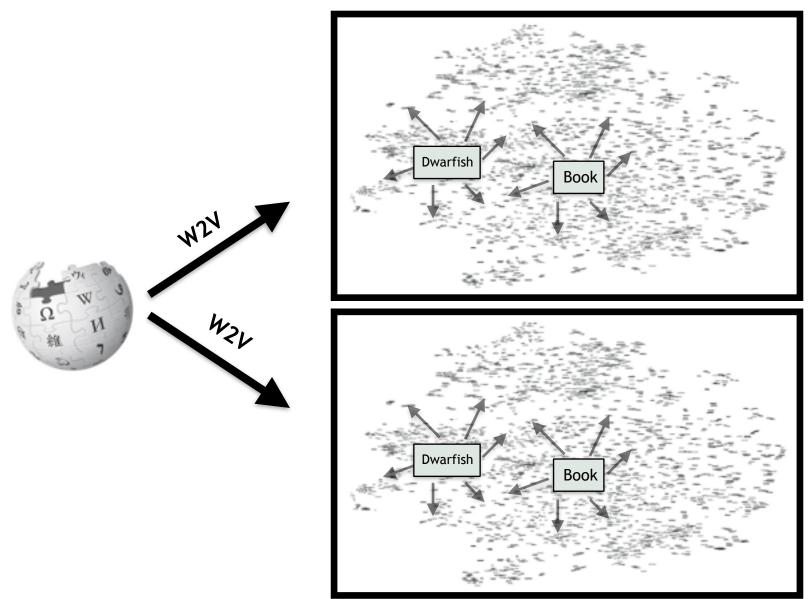




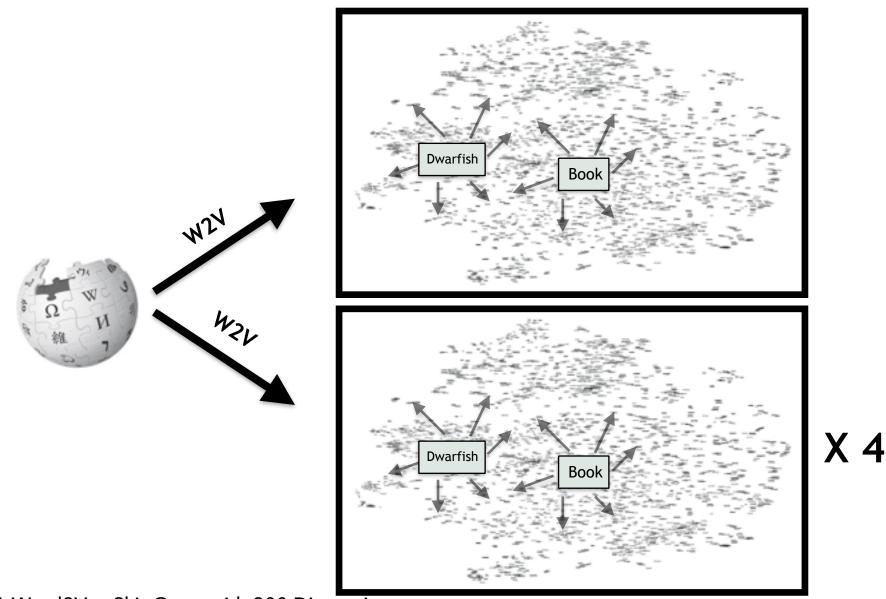






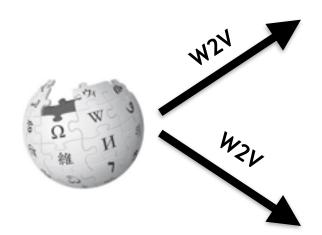




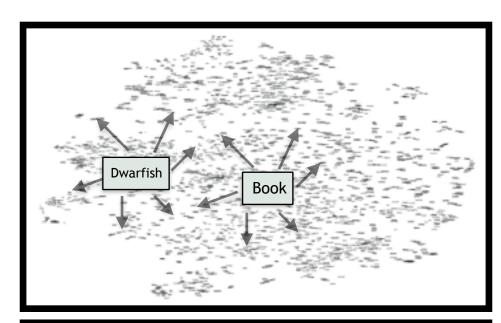


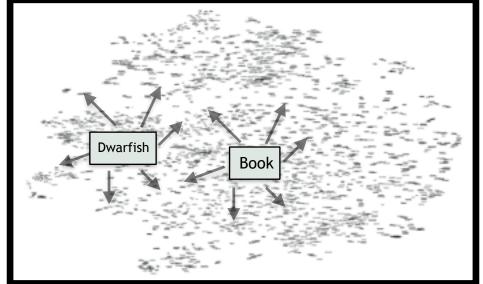


Similarity values: **Base** 



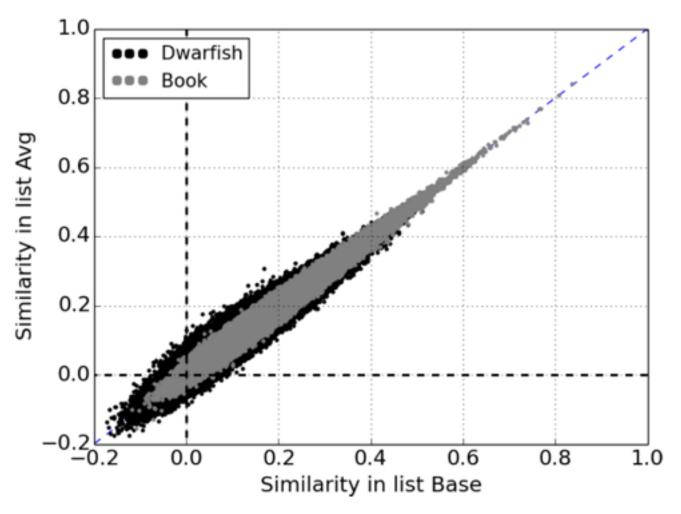
Average of similarity values of 5 models: Avg





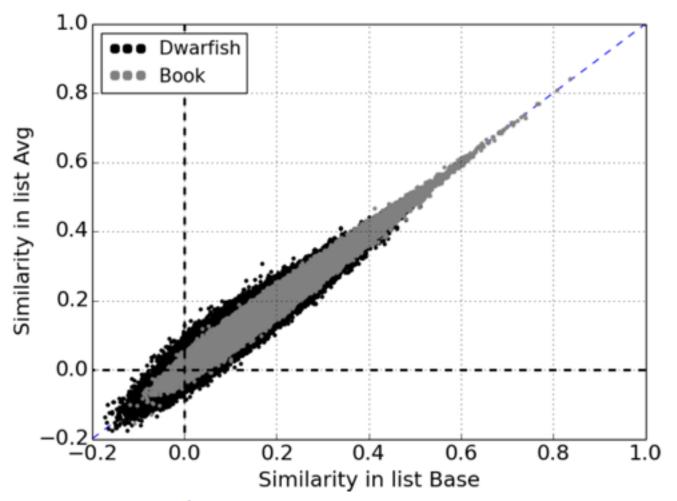
#### TU

### Uncertainty



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Uncertainty: 
$$\varrho(s) = rac{1}{|\mathcal{S}_s|} \sum_{(x,y) \in \mathcal{S}_s} |sim(ec{x}_M, ec{y}_M) - sim(ec{x}_P, ec{y}_P)|$$

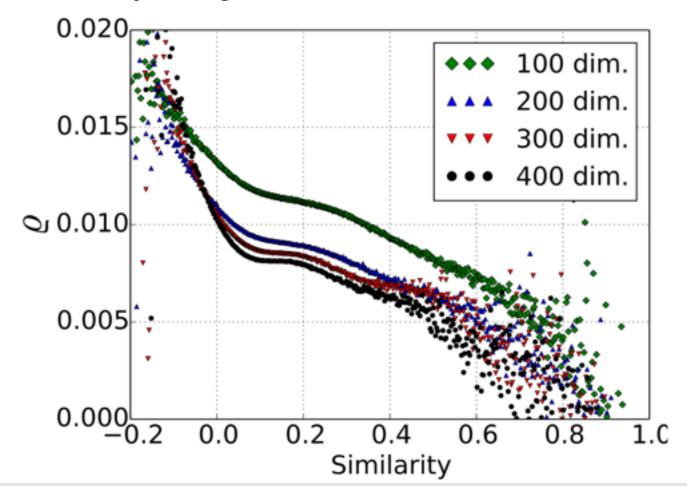
$$\mathcal{S}_s = \{(x,y) : sim(\vec{x}_M, \vec{y}_M) \in (s,s+\epsilon)\}$$

### Uncertainty

• Arbitrary term: Average of 100 representative terms [Schnabel et al. 2015]

### Uncertainty

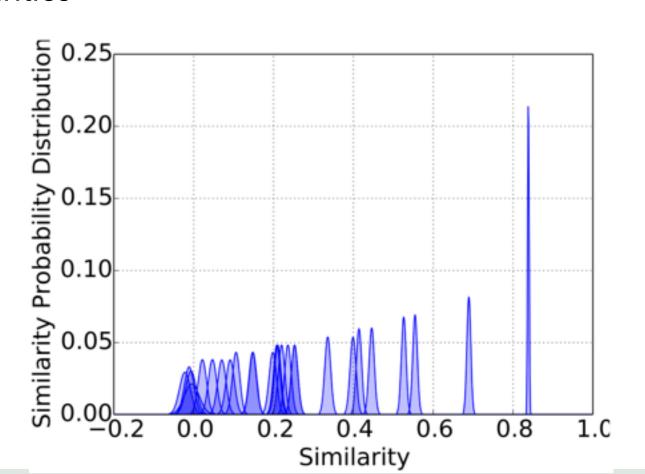
- Arbitrary term: Average of 100 representative terms [Schnabel et al. 2015]
- Less uncertainty in higher similarity values
- Less uncertainty in higher dimensions





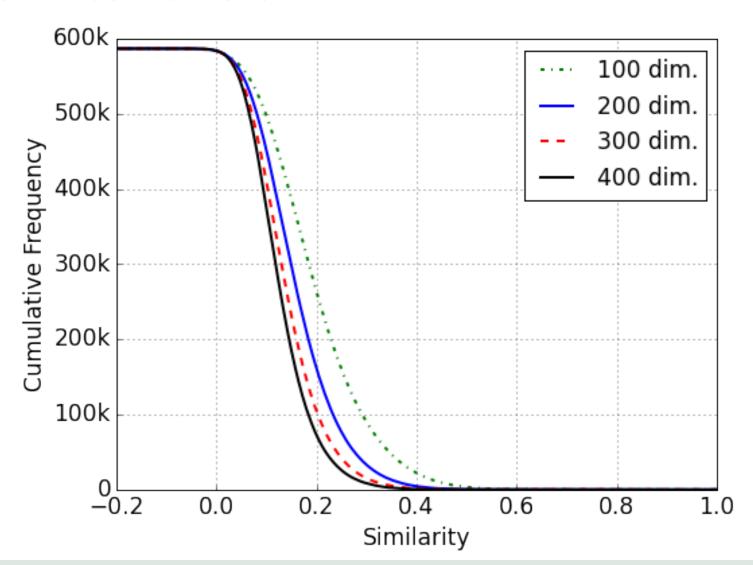
### Similarity Probability Distribution

- Similarity between terms as probability distribution instead of concrete values
- Assumption: normal distribution based on 5 observed similarities



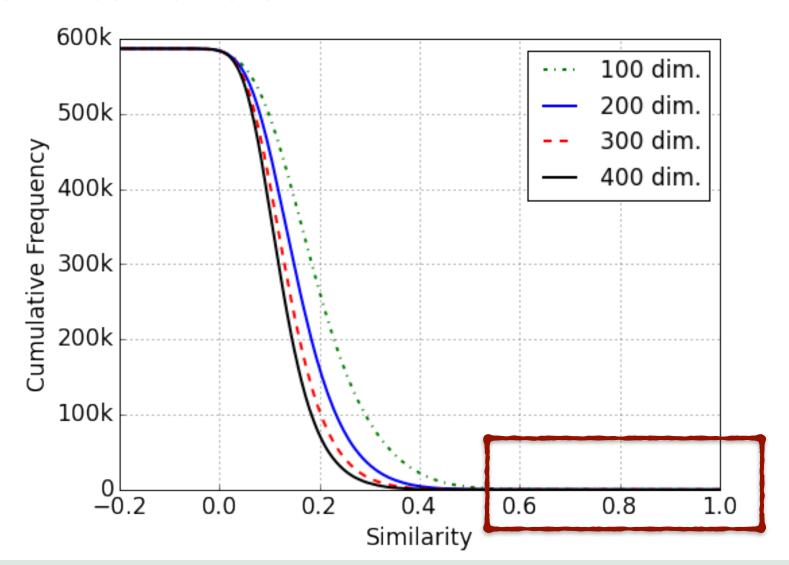


 Y axes: number of neighbors, located in the space between the X value and the term



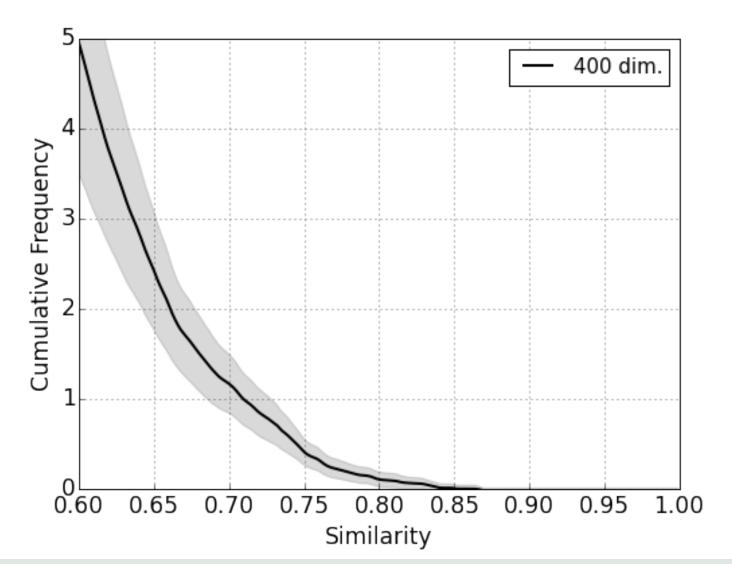


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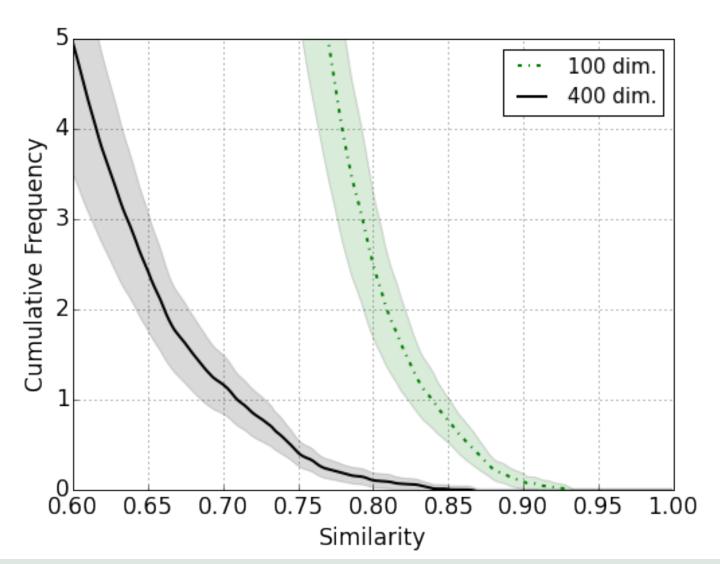


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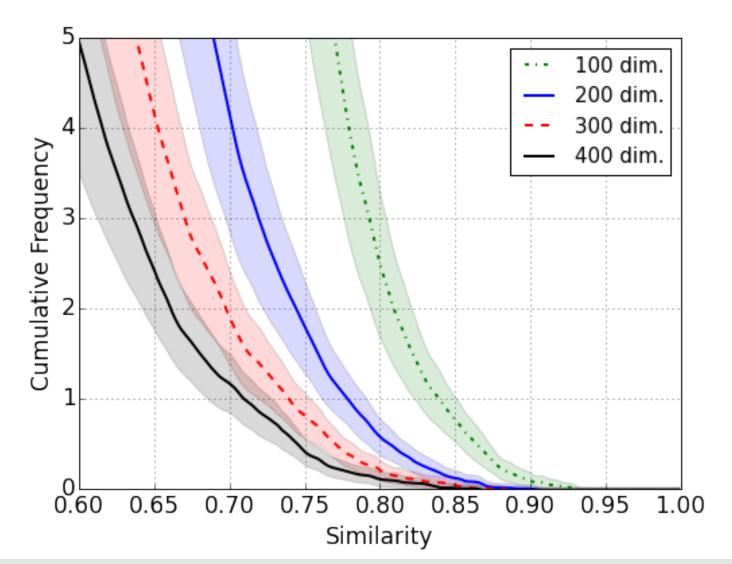


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What is the expected number of synonyms for a word in English?

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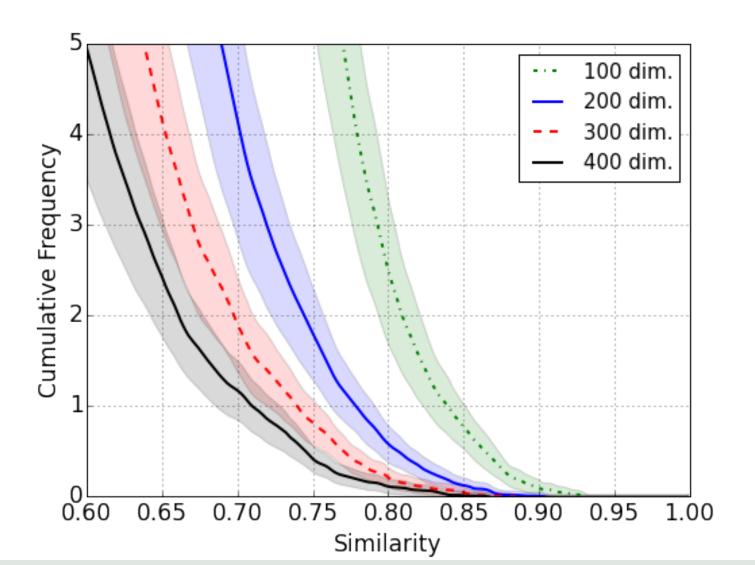
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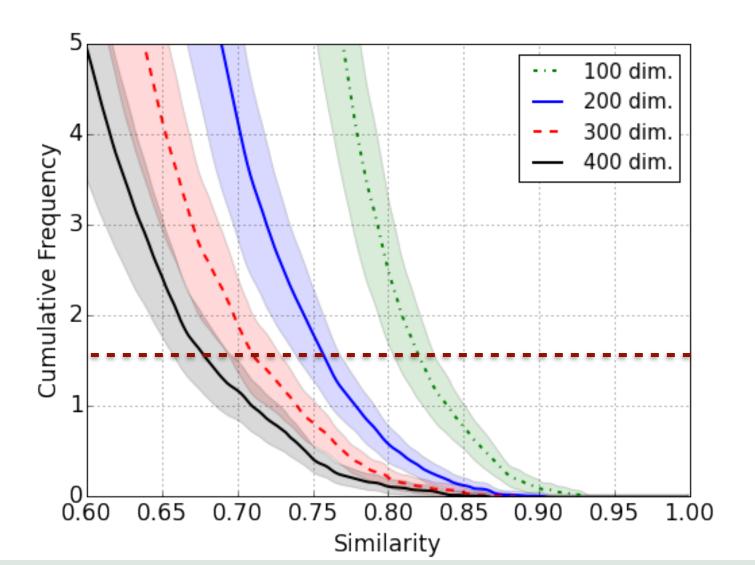


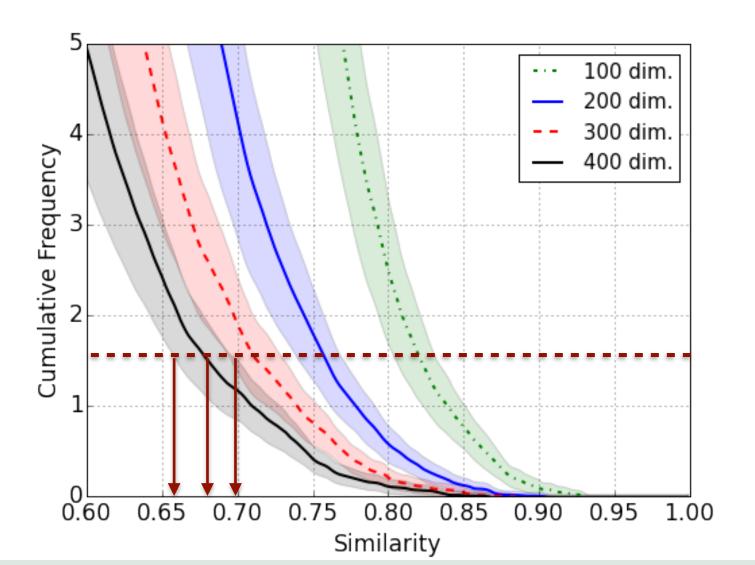
# of terms: 147306

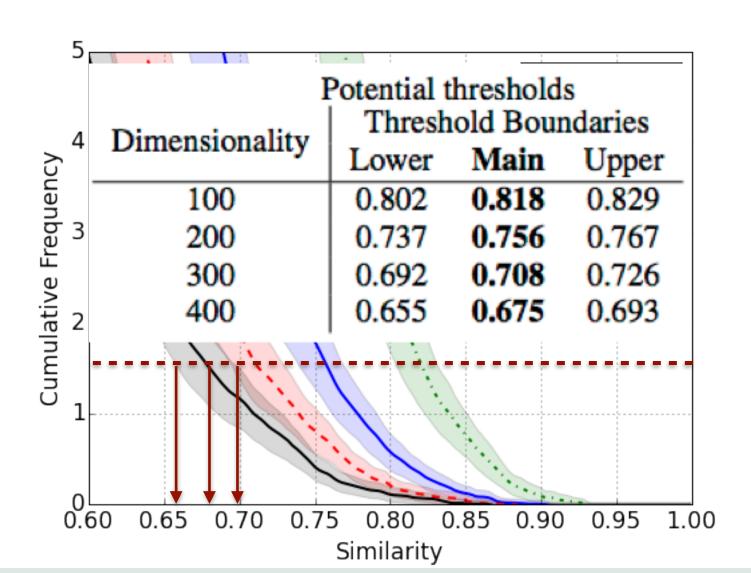
Average # of synonyms per term: 1.6

Standard deviation: 3.1









### TU

### **Experiments Setup**

- Translation Language Model with Dirichlet smoothing
- Use word embedding similarity value for translation probability Zuccon et al. [2015]
- Apply the proposed threshold to select the similar words
- Brute-force search to find the optimal threshold

$$P(q|M_d) = \prod_{t_q \in q} \left( \sum_{t_d \in d} P_T(t_q|t_d) P(t_d|M_d) 
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Test collections:

•	Name	Collection	# Doc
	TREC 6	Disc4&5	551873
	TREC 7, 8	Disc4&5 without CR	523951
	<b>HARD 2005</b>	AQUAINT	1033461

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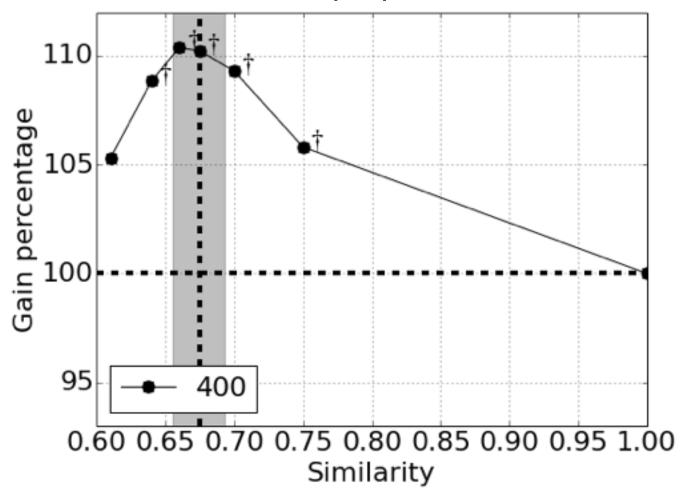
  TREC 7, 8 Disc4&5 without CR

  HARD 2005 AQUAINT 1033461
- Baseline: language model (Dirichlet smoothing)
- Significance Test: T-Test p<0.05



### **Experiments Results**

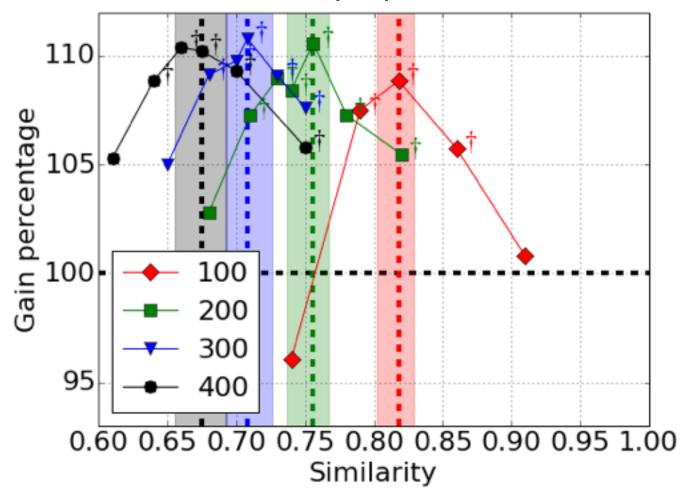
- Gain of MAP over baseline, averaged on four collections.
- Conclusion1: Optimal threshold is either the same or in the confidence interval of the proposed threshold.



### TU

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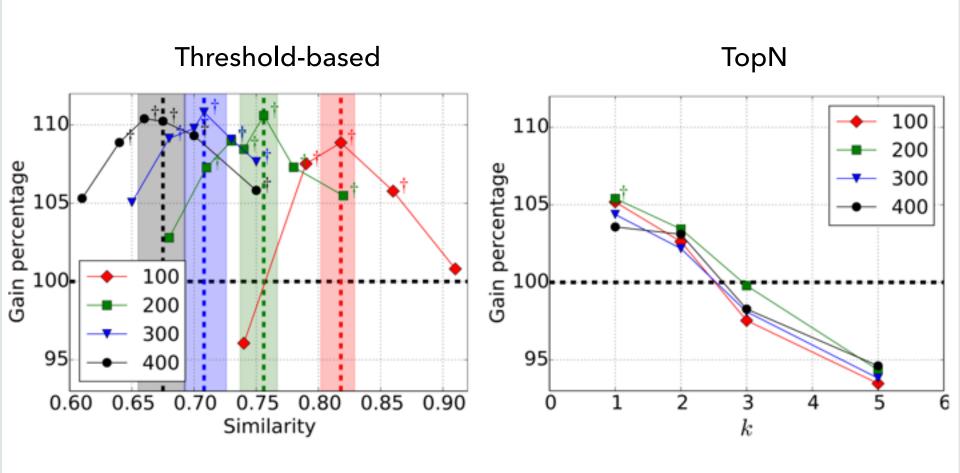
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### Threshold vs. TopN

Conclusion2: Threshold outperforms TopN



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### Take Home Message

- Uncertainty in neural network word embeddings:
  - depends on similarity value
  - depends on dimensionality

- Threshold to filter *unrelated* terms :
  - Proposed threshold as good as optimal threshold
  - Threshold approach much better than Top-N approach

## Questions?

### Ideas!

Follow-up paper in CIKM 2016:

Generalizing Translation Models in the Probabilistic Relevance Framework

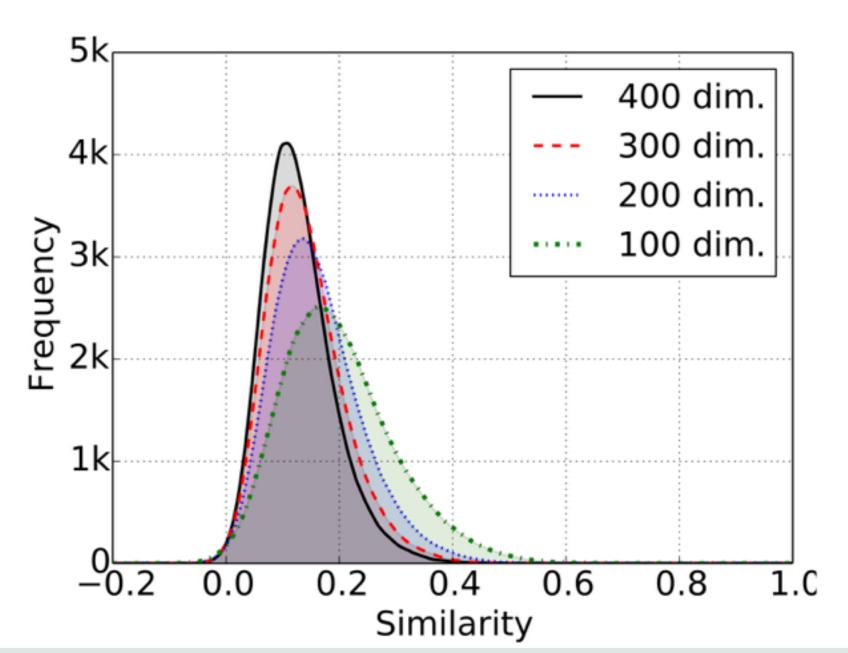
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### Dimensionality





### Proposed vs. Optimal Threshold

