

Homework 3

1) Sample Space

Our sample space was defined as $\mathcal{G}_n = (\mathcal{X}, \mathcal{Y}, \mathcal{Z})$

Where $\mathcal{X} = (0,1)^{n \times n}$ is the adjacency matrix describing the connection of neurons (nodes),

$\mathcal{Y} = \{0,1\}^n$ describes whether the neuron is excitatory or inhibitory and

$\mathcal{Z} = (0,2\pi)^n$ is the tuning property of the neuron.

2) Model

The chosen model is a stochastic block model, $SBM_n^2(\vec{\rho}, \vec{\beta}) = \{P_\theta : \theta \in \Theta\}$, $\Theta \Delta_k \times (0,1)^{k \times k}$

Defining \mathcal{Z}

Instead of defining the tuning over the whole interval $(0,2\pi)$, binning the orientation might be useful in order to reduce the variance (although increasing the bias). Bock et al used 8 bins, but to increase the resolution we could e.g. use 18 bins over the range 0-180° instead.

Defining the block model parameters, $\vec{p}(z)$, $\vec{\beta}(z)$

As defined in class, $\vec{p}(z) \in \Delta_k$ and $\vec{\beta}(z) = (0,1)^{k \times k}$ where k is the number of blocks in our model and β , the distribution of edges in our model is a Bernoulli distribution. This would be the simplest distribution we could use for β . Using $k=2$, i.e. one cluster for excitatory neurons (showing some orientation preference) and another for inhibitory neurons (not showing any preference), $\vec{p} \in \Delta_2$ and $\vec{\beta} = (0,1)^{2 \times 2}$