

## ECE F344 - Information Theory and Coding Assignment 2

Group 22

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### Question:

Write a computer program that takes in a polynomial with coefficients in  $GF(q)$  and returns whether it is irreducible?

### THEORY:

A polynomial  $f(x)$  in  $F[x]$  is said to be reducible if  $f(x) = a(x)b(x)$ , where  $a(x)$ ,  $b(x)$  are elements of  $F[x]$  and  $\deg a(x)$  and  $\deg b(x)$  are both smaller than  $\deg f(x)$ . If  $f(x)$  is not reducible, it is called irreducible. An irreducible monic polynomial of degree at least one is called a prime polynomial. It is helpful to compare a reducible polynomial with a positive integer that can be factorized into a product of prime numbers. Any monic polynomial in  $f(x)$  can be factorized uniquely into a product of irreducible monic polynomials (prime polynomials). Prime polynomials of every degree exist over every Galois Field.

So the idea is to divide the polynomial  $f(x)$  given with all the possible polynomials in  $GF(q)$  with a degree less than that of  $f(x)$ . if none of them divide  $f(x)$  (remainder = 0),  $f(x)$  is said to be irreducible. If it's reducible at least two factors will exist.

Another idea is to substitute all the elements of  $GF(q)$  in  $f(x)$  and if the values obtained are non-zero for all the elements, then too the polynomial is said to be irreducible. We implemented the first idea in the code given below.

## CODE:

The assignment was coded in MATLAB. A function “npermutek” is required to run the code. The function is also attached in the zip folder.

1. Read the input from the user. The user needs to provide a prime number for the field ( $p$  in  $GF(p)$ ) and the polynomial to be tested for irreducibility. The polynomial coefficients are to be entered in square brackets separated by spaces in the ascending order of degree (Example:  $[1\ 1\ 0\ 1]$  translates to  $1 + x + x^3$ ). The default input for  $p$  is 2 and the default polynomial is  $[1\ 1\ 1\ 1]$ .

```
1 - clc;
2 - clear all;
3 - close all;
4 - %=====
5 - %Input dialog
6 - prompt = {'Enter p(in GF(p)):' , 'Enter the coefficients of the polynomial inside square brackets separated by spaces (increasing order of degree):'};
7 - dlgtitle = 'Input';
8 - definput = {'2' , '[1,1,1,1]'};
9 - dims = [1 35];
10 - inp = inputdlg(prompt,dlgtitle,dims,definput);
11 - %=====
```

2. The input is processed. A vector  $v$  containing all possible elements in the Galois field is created ( $0$  to  $p-1$  for  $GF(p)$ ). The input polynomial is displayed in the traditional format using  $x$  as a variable. “npermutek” is used to generate all possible polynomials with degree less than the input polynomial and having coefficients from the  $GF(p)$  and is stored in “a\_”.

```
12 - %Input processing
13 - p = str2double(inp{1}); %GF(p)
14 - v = 0:p-1; %Possible elements in GF(p)
15 - % Example: b = [1 0 1 0 0 0 0 1] Input polynomial 1 + x^2 + x^7 + x^8
16 - b = str2num(inp{2});
17 - disp('Input polynomial:')
18 - gfppretty(b)
19 - m_ = size(b);
20 - m = m_(2); %Size of the input polynomial array
21 - a_ = npermutek(v,m-1); %All possible polynomials in GF(p) with a degree less than the input polynomial
22 - n_ = size(a_);
23 - n = n_(1);
24 - %=====
```

3. A boolean ("is\_irreducible") is created to keep track of the reducibility of the polynomial. The input polynomial is divided with all polynomials in "a\_". The loop is exited when a factor is found (the remainder is 0) and the factor is printed.

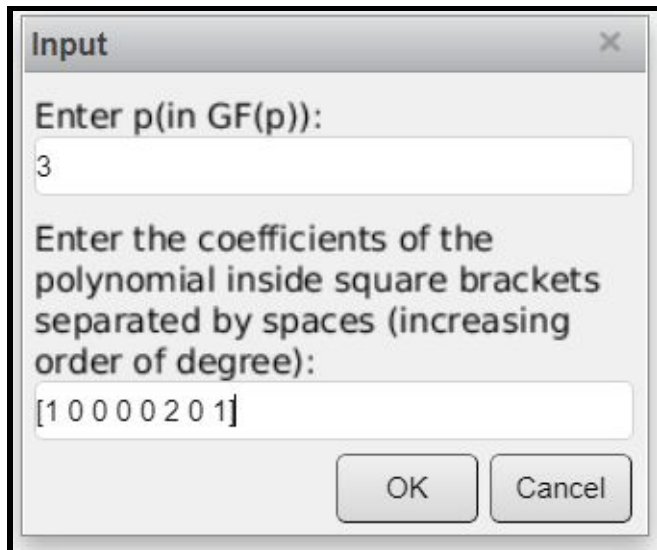
```
25 %Check for irreducibility
26 - is_irreducible = true;
27 - r = -1;
28 - for i = 1:n
29 -     is_zero = false;
30 -     for j = 0:p-1
31 -         if isequal(a_(i,:), [j,zeros(1,m-2)]) %Check if all zeros or constant. If so, skip checking with that polynomial.
32 -             is_zero = true;
33 -         end
34 -     end
35 -
36 -     if is_zero == true
37 -         continue
38 -     end
39 -
40 -     [q,r] = gfdeconv(b,a_(i,:),p); %Divide all polynomials and check the remainder
41 -
42 -     if r == 0 %If remainder is 0, the
43 -         is_irreducible = false;
44 -         disp("Factor:")
45 -         gfprefty(a_(i,:))
46 -         break
47 -     end
48 - end
49 %=====
```

4. Print the corresponding message using the Boolean.

```
50 %Print the result
51 - if is_irreducible == true
52 -     disp("The input polynomial is irreducible over GF(p)");
53 - else
54 -     disp("The input polynomial is reducible over GF(p)");
55 - end
56 %=====
```

## OUTPUTS:

Case 1:



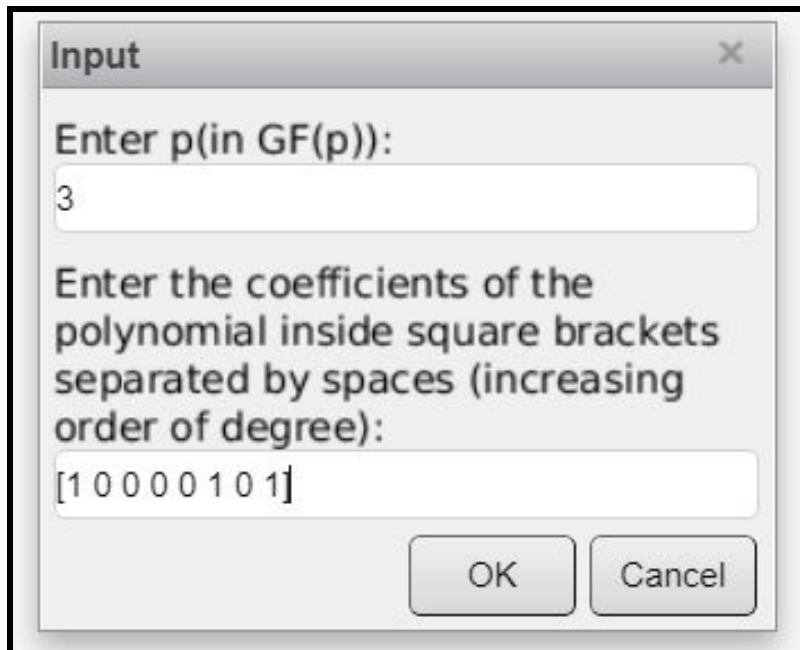
A screenshot of a software input dialog box titled "Input". It contains two text input fields. The first field is labeled "Enter p(in GF(p)):" and contains the value "3". The second field is labeled "Enter the coefficients of the polynomial inside square brackets separated by spaces (increasing order of degree):" and contains the value "[1 0 0 0 0 2 0 1]". At the bottom right of the dialog are "OK" and "Cancel" buttons.

Input polynomial:

$$1 + 2X^5 + X^7$$

The input polynomial is irreducible over GF(p)

Case 2:



A screenshot of a software input dialog box titled "Input". It contains two text input fields. The first field is labeled "Enter p(in GF(p)):" and contains the value "3". The second field is labeled "Enter the coefficients of the polynomial inside square brackets separated by spaces (increasing order of degree):" and contains the value "[1 0 0 0 0 1 0 1]". At the bottom right of the dialog are "OK" and "Cancel" buttons.

```
Input polynomial:
                5      7
            1 + X  + X

Factor:
                2      3
            1 + X  + X

The input polynomial is reducible over GF(p)
```