## Count number of coins required to make a given value

Greedy algorithms do not necessarily give the optimal solution . I n the Link provided they have given the have used Dynamic programming Approach

Dynamic problem Breaks down the code to find the optimal Solution. It builds up a final solution using the sub problems

Steps for Coin Change Problem Using DP:

- 1. Create a table in which rows represent possible change amounts (0 to the target amount) and Columns represent different coin denominations.
- 2. Fill in the base cases as 0
- 3. Fill in the rest of the table:
  - For each change amount (row) and coin denomination (column):
    - Check if the coin is smaller than or equal to the change amount.
    - If it is, calculate the minimum number of coins needed for that change amount using two options:
      - Option 1: Use the current coin plus the minimum number of coins needed for the remaining change (change amount minus coin value).
      - Option 2: Don't use the current coin, and use the minimum number of coins from the previous row (same change amount, different coin).
    - Choose the option that results in the smaller number of coins and store it in the table.
- 4. Find the optimal solution:
  - The minimum number of coins for the target change amount is in the last row, last column of the table.
- 5. Backtrack to find the actual coins used:
  - Start from the last row, last column of the table.
  - $\circ\quad$  Follow the decisions made in step 3 to trace back the coins used.

## Example:

For denominations [1, 2, 5, 8, 10] and change 7, the DP table would look like this:

```
1 2 5 8 10
0 0 0 0 0 0
1 1 1 1 1 1
2 2 1 1 1 1
3 3 2 1 1 1
4 4 2 2 1 1
5 5 3 1 1 1
6 6 3 2 1 1
7 7 3 2 2 1
```

The optimal solution is 2 coins (5 and 2), as found in the last row, last column.

Start from the last row, last column (7, 2).

- Check which option was chosen to fill that cell (in this case, Option 2, as it's smaller than Option 1).
- Follow Option 2, which refers to the previous row (6, 2).
- Repeat this process until you reach a base case (o coins).
- The traced path reveals the coins used: 5 and 2.

• count() function:

- Recursively explores different combinations of coins to make the sum.
- Uses a 2D DP table (dp) to store previously calculated results, enhancing efficiency.
- Base cases:
  - o If the sum is 0, there's 1 way to make it (using no coins).
  - If the number of coins is 0 or the sum is negative, there's no way to make it.
- Recursive calls:
  - Considers two options for each coin:
    - *Include* the current coin and explore making the remaining sum with the same set of coins.
    - *Exclude* the current coin and explore making the sum with the remaining coins.
- Memoization:
  - Stores calculated results in dp for reuse, avoiding redundant computations.

## Scenarios:

Scenario 1: coins = [1, 2, 3], sum = 5

- Output: 5
- Explanation: 5 ways to make 5:
  - 0 1+1+1+1+1
  - 0 1+1+3
  - o 1+3+1
  - 0 3+1+1
  - 0 2+3

Scenario 2: coins = [2, 5, 3, 6], sum = 10

- Output: 5
- Explanation: 5 ways to make 10:

- 0 2+2+2+2+2
- o 2+3+5
- o 3+2+5
- o 5+2+3
- 0 2+2+3+3

Scenario 3: coins = [1, 4], sum = 6

- Output: 2
- Explanation: 2 ways to make 6:
  - 0 1+1+1+1+1
  - 0 4+2