Proposing an alternative method for trap constant calculation for optical tweezers

males me wonder, which is good

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Supervisor?

Abstract 1

This report contains our findings on methods of finding the trap stiffness of an optical trap or optical tweezer setup and the conversion of an MATLAB data processing script to Python. Optical trapping is a technique in which a small particle is being held in place by a focussed laser beam, commonly used in the imaging recording

The trap stiffness in relation to laser output power was determined by photographing a particle in an optical trap multiple times for a set laser power output setting, then repeating this for multiple laser power output settings. The resulting image stacks were processed by an automated MATLAB script that calculates the movement of the centre of mass of the bead and uses this to calculate the restoring force of the optical trap against the Brownian motion of the particle. The resulting trap constants were then plotted for each laser power output setting. The predicted direct proportionality between the laser power and the trap constant could be observed. However, given the distance from the data to the best fit, the values for the slope coefficient is not of much use

Due to the current Corona-virus outbreak we were unable to do the optical trap measurements ourselves so to make up for this we were also tasked with rewriting part of a MATLAB script in Python. Whilst doing this a problem presented itself, there is no efficient way to interpolate a non-evenly spaced data grid in Python. With no knowledge of how to write such a function ourselves we opted to use a function that was able to interpolate at one point at a time which resulted in a slowdown of the data processing speed and allowed errors to creep in. The two other functions that had to be rewritten were the subpixel interpolation function and the symmetry centre finding function, both of these our now working in Python. The presented Python file is therefore capable of roughly following the symmetry centre of the bead in an optical trap.

Using the covariance matrix of the data, the values for the semi-major and semi-minor axis of the covariance ellipse were found for both data sets. The values match the theoretical inverse proportionality with respect to the laser power. The difference between the values for the major and minor axis compared to the MATLAB script shows the advantage of calculation of the trap constant using the covariance matrix. For this method incorporates the shape and direction of the optical trap.

resulted in errors

Werkte de code die we inleverde het enigzins goed? Waarom was ie ook alweer niet goed? Was ie te traag of niet nauwkeurig?

Kan jij dat even aanvullen Jeroen?

funny, the other report was emphasizing on what went wrong, and you coneupwith a solution.

Content isole, abit lengthy though.

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2 Introduction

An optical trap, or optical tweezers, is a technique that is frequently used in molecular biology to study particles at the micro- and nanometre scale. By trapping a particle in a focussed laser beam, the particle is limited in movement. This allows the user to study microscopic manipulations and measurements on microscopic particles and therefore proves to be very useful in the field of biophysics. Examples of which are sorting of cells, unzipping of DNA and enzyme interactions [1] [2]. In order to perform quantitative measurements using optical tweezers, it is vital to know what force it exerts on the particle. This force is defined by the trap constant and is dependent on various parameters such as the particle size and laser power. The aim of this report is to find the relation between the laser power and the trap constant. Secondly this report serves to get familiarised with the optical tweezers technique and to investigate its limitations and possibilities. Due to the COVID-19 virus no experiments were carried out for this report and data of previous experiments by other students is used. This data contains images of a trapped bead for laser beams with different powers. For each laser intensity, there is a set of images at fixed time intervals such that the movement of the bead can be studied. For this report, the images are processed by a MATLAB algorithm which calculates the trap constant in two perpendicular directions. The relation between each trap constant and the laser power is found using a distance regression method and the theoretical linear dependence. Another part of this practicum involves designing a PYTHON algorithm that can perform the same calculation as the provided MATLAB code. In this report, the result of our programming is described and suggestions are made for improvement of the PYTHON code and further analysis of the trap constant is different directions. In section 2 the theory regarding the report will be described followed by the experimental method in section 3. The results and discussion can be found in section 4. Lastly the conclusions in section 5.

Sounds like F= ktrap defined. Sounds fancy I'm eager to see it explained

Overall: Quite ou, but with no indents, enters, sectioning: malleit well structured

Theory

the optical tweezers technique was used in the experiment that corresponds with the data that is used in this report. The basic principles of optical tweezers and the theory for further calculations is described in this section.

Couldbe left out.

3.1 Optical trapping

To understand the working principle of optical tweezers we consider a spherical dielectric particle, a bead, in a coherent light beam with a symmetrical intensity gradient such as in figure 1a. The light beam will exert a force on the bead in the direction of the highest light intensity of the gradient. To understand this, we need to consider two situations. For the situation in which the dimensions of the bead are much greater than the wavelength of the light we can apply straight forward ray optics. In the situation where the size of the bead is much smaller than the wavelength we can approximate the bead as a dipole that feels Lorentz force due to a gradient in the electric field. For the situation where the dimensions of the bead are much larger than the wavelength of the light beam, we consider that photons can exert a radiation force on the bead. This force is a result of the momentum that photons carry and will be directly proportional to the light intensity. We now consider two rays of light that reach the bead symmetrical with respect to its centre. Due to the bead's spherical symmetric shape, the light rays will be refracted by the dielectric particle at the same rate, but in opposite directions (see figure 1a). Both light rays will, given the change in direction of the light and the third law of Newton, exert a force on the bead. The light ray with the higher intensity will, however, exert a greater force. If the intensity gradient is greater in the centre of the light beam, such as in figure 1a, this would lead to a net force pointing in the direction of the symmetry axis of the light beam. This force would trap the bead to the centre on the beam. In the case of a flow beam of light being focussed such as in figure 1b, the bead would not only be trapped in the direction perpendicular to the beam axis, but also in the direction of the axis. This is also a result of the change of the refraction of light exerting a force on the bead (see figure 1b). However, to light scattering, the bead is in the axial direction trapped slight behind the waist of the light beam. [1] In the situation where the dimensions of the bead are much smaller of than the wavelength of the light beam, we approximate the bead as a perfect dipole. According to shaevitz (2006), if we also consider the laser to have a Gaussian intensity profile in

personally Iwould place the figures horizontally. Makes the text easier to read

(a) Schematic diagram of the ray optics explanation for optical trapping (unfocused laser). The intensity profile of the light beam is symmetric around the centre. When the bead is displaced from the beam center (right image), the net force is towards the centre due to a larger momentum change of more intense light in closer to the centre. The net force is zero in the horizontal direction when the bead is placed in the centre of the beam.





(b) Schematic diagram of the ray optics explanation for optical trapping (focused laser). The light beam is now focussed. Due to the angle of incoming light, the momentum change of the light causes a net force points towards the focus. The equilibrium position is slightly behind the focus to compensate for the light scattering force.

Figure 1: Both figures were taken from Wikipedia [3].

the plane perpendicular to propagation, the Lorentz Force is given by:

$$F = (p \cdot \nabla)E + \frac{1}{c}\frac{d\,p}{dt} \times B \tag{1}$$

Where $p = \alpha E$ is the dipole field, α is the polarizability, E the electric field induced by the light and B the magnetic field induced by the light. Optical traps are typically used with a continuous wave (CW) laser such that $\frac{\partial}{\partial t}(E \times B) = 0$. In this case the time-averaged force becomes [1]:

$$\langle F \rangle = \frac{\alpha}{2} \nabla \langle E^2 \rangle \tag{2}$$

egain, improve the structure

This force is pointing towards the centre of the laser beam. Most optical trapping and also the experiment in this report includes beads with the same order of magnitude dimensions as the wavelength of the light beam. The physics of such a system is complicated and somewhat in between the cases explained above. This comprehensive theory will not be discussed in this report. However, from the latter derivations we can conclude that the trapping force is directly proportional with the laser intensity.

3.2 Trap constant derivation

According to Shaevitz (2006), 'for small motions of a bead near the centre of an optical trap, the forces acting on the bead approximate a zero rest-length, linear spring at the trapping centre.' Therefore, for small motions of the bead, the stored energy in the optical 'spring' is $1/2k_{trap}\langle x^2\rangle$ with k_{trap} a constant defining the strength of the optical trap and $\langle x^2\rangle$ the variance in the motion. According to the equipartition theory, the energy of the Brownian motion of a particle is given by $\frac{1}{2}k_bT$ with k_b the Boltzmann constant and T the temperature. [1] Equating the two energies yields:

 $k_{trap} = \frac{k_B T}{\langle x^2 \rangle} \tag{3}$

From this we can conclude that by following the position of the bead over time, it is possible to find the the value of k_{trap} .

In the latter definition of k_{trap} , the 3 dimensions of real life are not taken into account. In this report we will only consider the trap constants in the plane perpendicular to the propagation direction of the laser beam. This plane will in this report be addressed as the plane of interest, POI. For the POI we can consider two definitions for k_{trap} . We define $k_{trap,r}$ as the 'average' trap constant and is calculated using only the motion of the bead in the radial direction. $k_{trap,r}$ gives a good indication of the force in any arbitrary direction in the POI. It does, however, ignore the shape of the probability distribution of the bead. In the case where the potential well would be elongated such as in figure 2, the values for $\langle x^2 \rangle$ and therefore also k_{trap} can differ depending on the direction. We define the trap constant in an arbitrary direction as $k_{trap,i}$. Note that this is defined as a line in the POI which cuts the expectation value of the bead. To find the value for $k_{trap,i}$ we first realize that for realistic laser beams that are used for optical trapping, we expect a 2-dimensional gaussian intensity profile in the POI [1]. The shape of this gaussian profile can be described by a 2 dimensional covariance

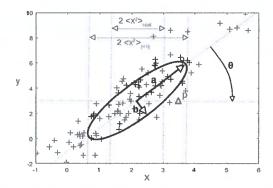


Figure 2: Schematic diagram of a data set with a bivariate gaussian distribution. The ellipse represents the variance of the distribution with it's semimajor and semi-minor axis a and b. θ represents the angle between a and line from the centre of the ellipse to an arbitrary point p. $\langle x^2 \rangle_{real}$ and $\langle x^2 \rangle_{proj}$ represent respectively the real variance in the x-direction and the projection of the variance ellipse on the x-axis.

matrix. The iso-contours and therefore also the variance for such 2-dimensional gaussians are ellipses with their centre at the expectation value [4] (see figure 2. According to Rojas (2009), the eigenvectors of the covariance matrix point in the direction of the axis of an ellipse describing the variance in the POI. The largest of the two eigenvectors, \vec{v}_1 , will point in the direction of the major axis and the smallest eigenvector, \vec{v}_2 , in the direction of the minor axis. The magnitude of the semi-major axis and semi-minor axis, a and b respectively, are given by the eigenvalues corresponding to the eigenvectors. [5] In order to find the variance in any arbitrary direction in the POI, $\langle x_i^2 \rangle$, we use the formula for an ellipse in polar coordinates:

$$\langle x_i^2 \rangle(\theta) = \frac{a b}{\sqrt{(b \cos \theta)^2 + (a \sin \theta)^2}}$$
 (4)

Where θ corresponds to the angle of the direction of interest with respect to the major axis and the ellipse centre as origin. (see figure 2) Note that the latter definition of the variance is different than just projecting each point on an axis and subsequently calculating the variance. The difference between the

I wonder whether in the analysis you also check whether your axis(ab) or ientation vouries produbetween datasets

two methods is clearly visible in figure 2 where $\langle x^2 \rangle_{real}$ is much smaller than $\langle x^2 \rangle_{proj}$. We can conclude from this, that when the position distribution is not symmetrical in the x- and y-direction, calculation of $k_{trap,x}$ or $k_{trap,y}$ without taking into account the covariance could give inaccurate results. Using equation 3 with the value for $\langle x_i^2 \rangle$ should yield better values for $k_{trap,i}$.

3.3 Error calculation

For this report, since we are not fully acquainted with the set-up and the corresponding error, when no error is specified the error is estimated to be half of the finest scale. For example for a size of 1.34 meter, the error would be 0.005 meter.

If Y is a variable which is a function of A,B,C,... Then the error of Y, u_Y , is given by equation 5.

$$u_Y = \sqrt{\left(u_A \frac{\partial Y}{\partial A}\right)^2 + \left(u_B \frac{\partial Y}{\partial B}\right)^2 + \left(u_C \frac{\partial Y}{\partial C}\right)^2 + \dots}$$
 (5)

Using the latter equation we find that the error in the average position, $u_{\bar{x}}$ is given by:

$$u_{\bar{x}} = \frac{\sqrt{\sum_{i=1}^{n} u_{x_i}^2}}{n} \tag{6}$$

Since $\langle x^2 \rangle$ is given by the average of the squared of the distance to the average position we find that the error in the variance, $u_{\langle x^2 \rangle}$ is given by:

$$u_{\langle x^2 \rangle} = \sqrt{\frac{4 \sum_{i=1}^{n} \left(u_{\bar{x}}^2 + u_{x_i}^2 \right) (\bar{x} - x_i)^2}{n^2}}$$
 (7)

For large values of n we can neglect the $u_{\bar{x}}^2$ term. Therefore we find:

$$u_{\langle x^2 \rangle} \approx \sqrt{\frac{4 \sum_{i=1}^{n} u_{x_i}^2 (\bar{x} - x_i)^2}{n^2}}$$
 (8)

If u_{x_i} is constant we can rewrite this as:

$$u_{\langle x^2 \rangle} \approx \sqrt{4 \, u_{x_i}^2 \langle x^2 \rangle} \tag{9}$$

Using equation 3 in equation 5 we find that the error in the trap constant, $u_{k_{trap}}$, is given by:

$$u_{k_{trap}} = \frac{u_{\langle x^2 \rangle} k_B T}{\langle x^2 \rangle^2} \tag{10}$$

In the case of a constant value of u_{x_i} we can use equation 9 to find that:

Using equation 3 we can rewrite this as: $u_{k_{trap}} = 2 u_{x_i} k_B T \langle x^2 \rangle^{-\frac{3}{2}}$ (11) $u_{k_{trap}} = 2 u_{x_i} (k_B T)^{-\frac{1}{2}} k_{trap}^{\frac{3}{2}}$ (12) Thorough, to be checked in results whether error boars are in reasonable range whether error boars are in reasonable range.

Overall: I appreciate the effort in 3.283.35

4 Experimental Method

No experiments were carried out for this report, but measurements from previous students are used. The experimental set-up that they used and the computer algorithms that were used for this report will be discussed in this section.

4.1 Experimental set-up

The experimental set-up that was used for this report can be seen in figure 3. According to the practicum manual, the red light from the laser has a wavelength $oi\lambda = 658$ nm and passes through a beam expander in order to completely fill the back (back focal plane) of the objective. The beads that are used in the experiment have a diameter of approximately $2\mu m$. The mirrors M1 and M2 are used for compacting the beam path and aligning the beam to the optical axis of the objective. The used objective is meant to be used in an infinity corrected microscope. L4 focusses the light back to an image at focal distance. In the setup, the L1 and L2 have focal length of

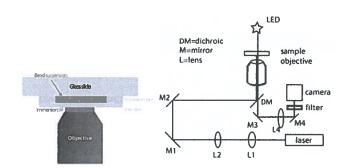


Figure 3: Schematic diagram of the experimental set-up that was used for the experiments corresponding with the treated data in this report. This diagram was taken from the practicum manual [6].

up, the L1 and L2 have focal length of respectively 50 and 350 mm. The front focal distance of the objective lens is 1.8 mm and the second objective lens has a focal length of 200 mm. Using simple division and equation 5 we find that the magnification is $M = \frac{200}{1.8} = 1.1 \pm 0.3 \cdot 10^2$. Given the pixel size of the camera of $5.2 \, \mu$ and equation 5 we find that the conversion factor for pixels to length is given by $l_{pixel} = \frac{5.2}{M} \cdot 10^{-6} \approx 4.7 \pm 0.1 \cdot 10^{-8} m/pixel$.

Using the discussed set-up, a bead was to be trapped by a laser beam and 1000 images were taken at fixed time intervals. This was performed for laser beams with different powers. The involved powers were 0, 5, 10, 20, 30 and 40 mW. For this report, two data sets from different students are analysed.

4.2 Computation

A MATLAB algorithm was provided for this practicum in order to calculate the trap constant in a x- and y-direction, $k_{trap,x}$ and $k_{trap,y}$. This algorithm involves noise removal of the images and tracking the bead using a 'quadrant-interpolation (QI) algorithm which makes use of the circular geometry of the diffraction pattern to resample the image on a circular grid.' [7] Subsequently, power spectrum analysis is performed to calculate the values for $k_{trap,x}$ and $k_{trap,y}$. Since the trapping force is directly proportional to the light intensity the correlation between the laser power P and the trap constant k_{trap} is given by: $k_{trap} = \alpha \cdot P$. Using the MATLAB code and a linear regression method, the value for α is determined for the two data sets.

Secondly, a PYTHON algorithm is used with the same noise cancelling technique, but with a trackpy function to follow the bead. This algorithm subsequently calculates the covariance matrix and the vectors describing the covariance ellipse. Using this PYTHON code, the change of this covariance ellipse is analysed.

clear story nicely condensed

Results 5

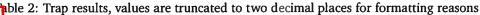
5.1 Results of the datasets

The results of the MATLAB code calculating $k_{trap,x}$ and $k_{trap,y}$ for the two data sets are presented in table 1. Since the MATLAB code failed to track the bead for some of the measurements in the first data set, not all values are used for fitting. The second dataset was much better and did not have any faulty measurements, its values are shown in table 2.

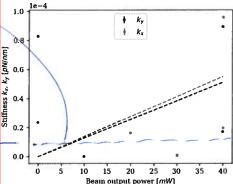
Laser Power [mW]	0*	10*	20	30*	40	40
$k_{trap,x} [pN/nm]$	$2.36\cdot 10^{-5}$	$2.45 \cdot 10^{-7}$	$1.60 \cdot 10^{-5}$	$8.35 \cdot 10^{-7}$	$1.99 \cdot 10^{-5}$	$9.60 \cdot 10^{-5}$
$k_{trap,y} [pN/nm]$	$8.29\cdot 10^{-5}$	$2.94 \cdot 10^{-7}$	$1.65 \cdot 10^{-5}$	$9.71 \cdot 10^{-7}$	$1.72\cdot 10^{-5}$	$8.96\cdot 10^{-5}$

Table 1: Results of the first dataset. The values are truncated to two decimal places. * denotes a faulty measurement

Laser Power [mW] 0		5	10	20	30	40		
$k_x [pN/nm]$	$3.64 \cdot 10^{-7}$	$8.24 \cdot 10^{-5}$	$1.08 \cdot 10^{-4}$	$3.03 \cdot 10^{-4}$	$6.14 \cdot 10^{-4}$	$7.55 \cdot 10^{-4}$		
$k_y [pN/nm]$	$5.55 \cdot 10^{-7}$	$4.18 \cdot 10^{-5}$	$2.53\cdot 10^{-5}$	$1.10 \cdot 10^{-4}$	$1.69 \cdot 10^{-4}$	$2.54\cdot 10^{-4}$		







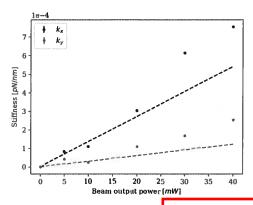


Figure 4: Results of the first dataset plot-

Figure 5: Results of the second dataset

We cannot calculate the exact value of the error since the MATLAB algorithm does not provide us with the locations and its error. However, if we estimate the error of the bead location to be not provide us with the know that 1000 frames were used for the calculate.

 $u_{k_{trap}} = l_{pixel}(k_BT)^{\frac{1}{2}}k_{trap}^{\frac{3}{2}}$. However when these values are calculated we see an error between 0.1% and 0.00001% of that of the k_i value, these values are lower then we believe they should be. We suspect that his is the case since the MATLAB algorithm confidently tracks a incorrect stationary artefact on the trap surface.

The data individual da individual data points for the k_x and k_y values. spectively. In the plots the the least squares fit of these

The resulting values of α for the least squares fit to the function $k_{trap} = \alpha \cdot P$ are shown below in table 3.

coefficient for	$\alpha_x [pN/(nm \cdot mW)]$	
dataset 1	$1.382 \cdot 10^{-6}$	$1.280 \cdot 10^{-6}$
dataset 2	$1.478 \cdot 10^{-5}$	$3.974 \cdot 10^{-6}$

Table 3: The results of the linear fits for the trap stiffness as a function of laser output power.

Volgens mij probeert ze te zeggen dat een fit eigenlijk nergens op slaat. Zou jij een plot kunnen maken zonder een gefitte lijn, maar enkel data punten? Ik heb de tekst daar al voor aangepast.6

5.2 Python program results

During this practical we were also tasked with rewriting a MATLAB script in to Python. The piece of script we needed to rewrite was the function that tracks the centre of the bead in the image, this function was comprised of interpolation method and a method that found the symmetry centre of the bead using Fourier transforms. The second part was easily implemented in Python as it was mostly just finding the right Python functions that were equivalent to their MATLAB counterparts. The interpolation function was a lot harder to implement in Python since most of the existing Python interpolation functions did not have the same functionality. The documentation of this part of the practical can be found in the appendix 8

As outlined in the section 3.2 a method for deriving the trap constants was proposed that differs from the one from the MATLAB script. This method was implemented in a second different python script to try and show its usefulness. This python script can be found in the appendix.

The result speaks for itself, it shows a clear connection between the laser output power and the length of the semi-major and semi-minor axis of the ellipses that encircle the points describing the symmetry centres of the beads. The points were fitted with a function with shape $L_{axis} = \frac{\beta}{P} + \gamma$, this seems to fit well as can be seen in figure 6 & 7. This also shows that while the tran stiffness seems to increase linearly with the laser power the area of the ellipse in which we expect a bead to be found decreases by the inverse of the laser power. In the appendix three more plots showing the spread can be seen.

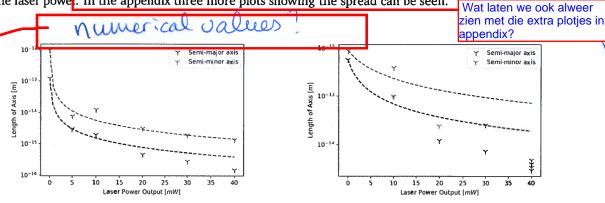


Figure 6: Semi-major and minor axis of the first dataset plotted and fitted.

Figure 7: Semi-major and minor axis of the second dataset plotted and fitted.

Kan jij een tabelletje invoegen van de waardes voor a en b?

based on theory, what type of function would you expect.

With your & the first dataset seems P the first dataset seems to be fitted perfectly, while fight looked auful-

Heb ik toch iets over geschreven, lijkt me wel prima zo

6 Discussion

As expected the values for $k_{trap,x}$ and $k_{trap,y}$ increase with an increasing laser power. For the second data set, a reasonable fit can be made using the theoretical relation between P and k_{trap} . The fit does however not fit the errors. Therefore one could doubt the accuracy of the result for the corresponding α . For the first data set we find that the data does not match the theoretical direct proportionality between R and Rity between P and k_{trap} . This seems to be the result of a failing MATLAB code which does not follow the bead. This seems to be caused by other particles in the image which were not trapped but clearly visible. This could have thrown off the program. Studying the images also reveals that the bead makes some large jumps possibly caused by vibrations of the experimental set-up during the experiment.

The practical manual asks for a calculation of the average trap constant. It was proposed to calculate this as follows: $k_{trap,tot} = \sqrt{k_{trap,x}^2 + k_{Trap,y}^2}$. This would however give inaccurate results since the orientation and shape of the variance is not taken into account. For the calculation of the trap constant we take the inverse of the variance. As explained in the theory we expect the variance to be ellips shaped. However, if we take the inverse of the radius of an ellipse we get a complicated shape such as in figure 8. Comparing the shape to a circle with radius $\sqrt{k_{trap,x}^2 + k_{Trap,y}^2}$ shows that the proposed method for the calculation is nonsense. The method described in section 3.2 could provide more accurate results. The results for the semi-major and semi-minor axis of the covariance ellipse indicates a inverse correlation of the axis length to the laser power. This is expected given equation 3 and the direct proportionality between the trap constant and laser power. It is interesting that the values for a and b for the

point me at which par of the data Ishould

Figure 8: An ellipse (blue) and the inverse of its radius (red).

- values

first data set seem to have more than a factor 5 difference which would indicate an elongated covariance ellipse. Comparing this to the MATLAB results, there seems to be virtually no difference between $k_{trap,x}$ and $k_{trap,y}$ (only taking into account correct measurements). This points out that the MATLAB algorithm, only projecting the positions on two axis, fails to incorporate the shape of the variance (see figure 2). Therefore, the method as outlined in section 3.2 seems to be promising for calculation of trap constants in any direction independent of the orientation and shape of the trap.

The task of recreating a MATLAB script in Python was partially successful. The symmetry centre finding function was successfully implemented as well as the subpixel interpolation function. Due to some dissimilarities in the way MATLAB and Python functions interpolate an unstructured set of data we were unable to get the main tracking function to work. The resulting estimates of the symmetry centre location were not far of but were not dead-on either.

Although the MATLAB code works fine in many cases, it showed that it does not always work well. Moreover, for students, the code is long and involves some complicated steps. For these reasons we would suggest using the trackpy for particle tracking. This function shows promising results in speed and accuracy. By visual inspection it is clear that this function had no trouble whatsoever with the data covered in this report. The down side is, although there is elaborated documentation of the function, the maths used for the tracking is not explicitly noted. Therefore students would perhaps have less insight in the tracking mechanism. More information about the trackpy function can be found in the appendix.

please show me results

Snap niet hoe ze dit wil zien, het best kan ze gewoon de trackpy functie openen en runnen. Lijkt me te veel werk om een nu een hele numerieke analyse te gaan doen door MATLAB en Trackpy waardes te vergeijken.

Title the ellipticity of approach, but need more values and link to theory to be fully convinced.



The predicted direct proportionality between the laser power and the trap constant could be observed. However, given the distance from the data to the best fit, the values for the slope coefficient is not of much use.

Rewriting the MATLAB script using Python was a partial success, the symmetry centre finding function and the subpixel interpolation function were successfully implemented in Python but the tracking function currently uses a slow and not very useful interpolation method which results in an undesirable offset and delay in the predicted symmetry centre. With a properly functioning interpolation function the python script would probably yield s similar result as the MATLAB script.

Using the method described in the theory, the values for the semi-major and semi-minor axis of the covariance ellipse were found for both data sets. The values match the theoretical inverse proportionality with respect to the laser power. The difference between the values for the major and minor axis compared to the MATLAB script shows the advantage of calculation of the trap constant using the covariance matrix. For this method incorporates the shape and direction of the optical trap.

great!

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8 Appendix

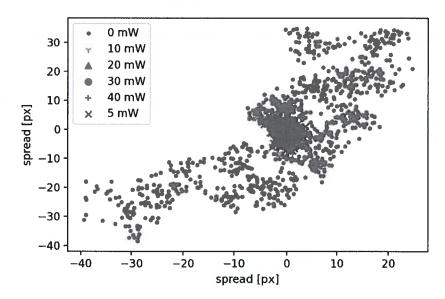


Figure 9: Spread of the first dataset shifted towards origin by average displacement from centre

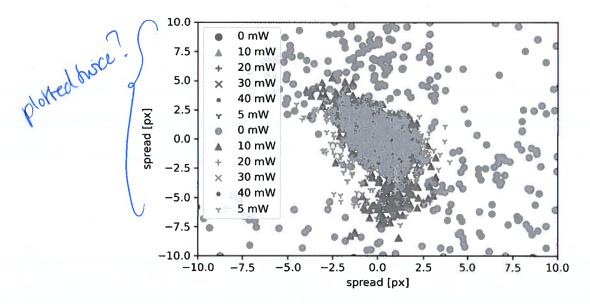


Figure 10: Spread of the first dataset shifted towards origin by average displacement from centre, and zoomed in

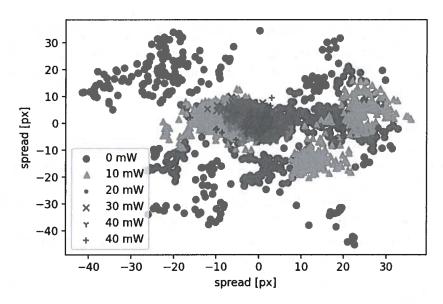


Figure 11: Spread of the first dataset shifted towards origin by average displacement from centre

You show first dataset 3x What do you want to tell me? Please add some 'viewing guidelines' in the text.

Documentation MATLAB to Python, RP Optical Tweezers Round 15 Stijn van der Lippe, Stein Glastra, Jeroen Sangers and Reinaart van Loon

We elaborate upon the issues we encountered in converting the MATLAB code of step 8 in GUI7_MDTIF to Python. Furthermore we elaborate upon some changes we made in the implementation of the code in Python and explain what some of the functions we added do.

Documentation step 8: QI tracker

The part of the code we were stuck on implementing is the interpolation of a non-rectangular grid. Several functions were tested in Python. Below we discuss why they do not give the results we want.

scipy.interpolate.griddata:

https://docs.scipy.org/doc/scipy/reference/generated/scipy.interpolate.griddata.html

This function has to perform a triangulation for every data point in the input array to find the nearest neighbour if the input array is irregular (as is the case for us). This happens every iteration. This is extremely slow and therefore this function is unusable. More details can be found here.

scipy.interpolate.RectBivariateSpline:

https://docs.scipy.org/doc/scipy/reference/generated/scipy.interpolate.RectBivariateSpline.html This creates a class that takes in two 1D arrays of coordinates and a single 2D array of values at the coordinates.

Calling this class using .ev() allows the interpolation at data points using 1D arrays of x and y coordinates. Calling the class normally can't work since it needs an array of points of all (x,y) coordinates we want to evaluate at, in ascending order which is something we can't do since we can't sort our points in such a way that the (x,y) coordinates stay linked.

scipy.interpolate.interp2d:

https://docs.scipy.org/doc/scipy/reference/generated/scipy.interpolate.interp2d.html

This function won't work since it only works with 1D arrays for x and y and outputs a 2D array of interpolated values which would be easy to use if the grid was rectangular, but it isn't so it would take multiple nested for loops which will be slow and error prone. And even then we get an array of outputs that assumes a rectangular grid and would therefore be distorted.

scipy.ndimage.map_coordinates:

https://docs.scipy.org/doc/scipy/reference/generated/scipy.ndimage.map coordinates.html

This function is promising but currently yields some strange results which we do not yet fully understand and can't really be tested until the previous code works. In our implementation, the function only returns integer values and we are unsure what the cause of this is.

Documentation subpix_step

In MATLAB an array [~,a] was created to get the value and index of the largest entry in the d-array, in Python this had to be substituted with np.argmax() to get only the index.

Documentation SymCenter

In MATLAB, NaNs in the input array were first located using a find function. Subsequently, they were padded using the value *nanmean* of the input array. In Python, this can be done in a single step using *np.where*. This was done by using the truth statement *np.isnan*. If the statement is true for an array element, the value of that element was replaced with *np.nanmean* of the input array.

Documentation get_eval_coords

A function that takes in a 2D array of coordinates and returns a flattened 1D array of these coordinates. It is used in the function *track_xy*.

Documentation rebuild_grid

A function that takes in a 1D array of points and a shape. The function then builds a 2D array with the same dimensions as shape. It is used in the function *track_xy*.

Documentation QI_tracker

A small error was found in the __init__ function of Ql_Tracker. In the variable assignment of self.X0samplinggrid and self.Y0samplinggrid both arrays were not transposed, while they should be. This was fixed by adding .T at the end of both.

removeNoise

We suspect the long duration of the calculation can be attributed to the time the noise removal takes. We tried to speed this process up by replacing an iteration function (*next*) with a numpy *np.where* function, which is not iterative.

The following line was replaced:

xIhalf = next(x for x, val in enumerate(ilstflat_t)

with

xlhalf = np.where(ilstflat_t>lhalf)[0][0].

This had little influence on the speed of the process.

The following line was also replaced:

xmindist = next(x for x, val in enumerate(dist) if val == min(dist))

with

xmindist = np.argmin(dist)

This had a major impact on the speed, removeNoise now takes less time to run.

Trackpy

http://soft-matter.github.io/trackpy/v0.4.2/tutorial/walkthrough.html

Trackpy is a python package which is used for particle tracking. It proves to be easy in use and promises accurate results (article about accuracy:

https://www.cell.com/biophysj/fulltext/S0006-3495(05)73136-2).

Using this Python function instead of the complicated QI-tracking would potentially not only make a more compact and structured code, it also showed some promising results in comparison with the MATLAB code. For the 'Bead' data set that we were given, the MATLAB code fails to track the bead. This is a result of large jumps in space of the bead in the image which cannot be followed by the QI-tracker. The trackpy function, however, seems to have no trouble following the bead whatever the size of the 'jumps'.

Another advantage is that the trackpy function provides the error in position for each independent frame. Therefore, instead of guessing the error for the QI-tracker, exact error calculation can be performed.