

Mini Project - Different exact and approximation algorithms for Travelling-Sales-Person Problem

```
In [2]: # 1. Brute-Force Approach (Exact Algorithm)
# Python Implementation

import itertools
import sys
import time

def calculate_total_distance(route, distance_matrix):
    total = 0
    for i in range(len(route)):
        total += distance_matrix[route[i]][route[(i + 1) % len(route)]]
    return total

def brute_force_tsp(distance_matrix):
    n = len(distance_matrix)
    cities = list(range(n))
    min_distance = sys.maxsize
    best_route = []
    # Generate all possible permutations of cities
    for perm in itertools.permutations(cities):
        current_distance = calculate_total_distance(perm, distance_matrix)
        if current_distance < min_distance:
            min_distance = current_distance
            best_route = perm
    return best_route, min_distance

# Main execution
if __name__ == "__main__":
    # Example distance matrix (symmetric)
    distance_matrix = [
        [0, 10, 15, 20],
        [10, 0, 35, 25],
        [15, 35, 0, 30],
        [20, 25, 30, 0]
    ]
    start_time = time.time()
    route, distance = brute_force_tsp(distance_matrix)
    end_time = time.time()
    print("Optimal Route (Brute-Force):", route)
    print("Minimum Distance:", distance)
    print(f"Time taken: {end_time - start_time:.4f} seconds")
```

Optimal Route (Brute-Force): (0, 1, 3, 2)

Minimum Distance: 80

Time taken: 0.0000 seconds

```
In [3]: # 2. Nearest Neighbor Algorithm (Approximation Algorithm)
# Python Implementation

import time

def nearest_neighbor_tsp(distance_matrix, start=0):
    n = len(distance_matrix)
    unvisited = set(range(n))
    unvisited.remove(start)
    route = [start]
    total_distance = 0
```

```

    current = start
    while unvisited:
        next_city = min(unvisited, key=lambda city: distance_matrix[current][city])
        total_distance += distance_matrix[current][next_city]
        route.append(next_city)
        current = next_city
        unvisited.remove(next_city)
    # Return to start
    total_distance += distance_matrix[current][start]
    route.append(start)
    return route, total_distance
# Main execution
if __name__ == "__main__":
    # Example distance matrix (symmetric)
    distance_matrix = [
        [0, 10, 15, 20],
        [10, 0, 35, 25],
        [15, 35, 0, 30],
        [20, 25, 30, 0]
    ]

    start_time = time.time()
    route, distance = nearest_neighbor_tsp(distance_matrix)
    end_time = time.time()
    print("Route (Nearest Neighbor):", route)
    print("Total Distance:", distance)
    print(f"Time taken: {end_time - start_time:.6f} seconds")

```

Route (Nearest Neighbor): [0, 1, 3, 2, 0]

Total Distance: 80

Time taken: 0.000000 seconds