

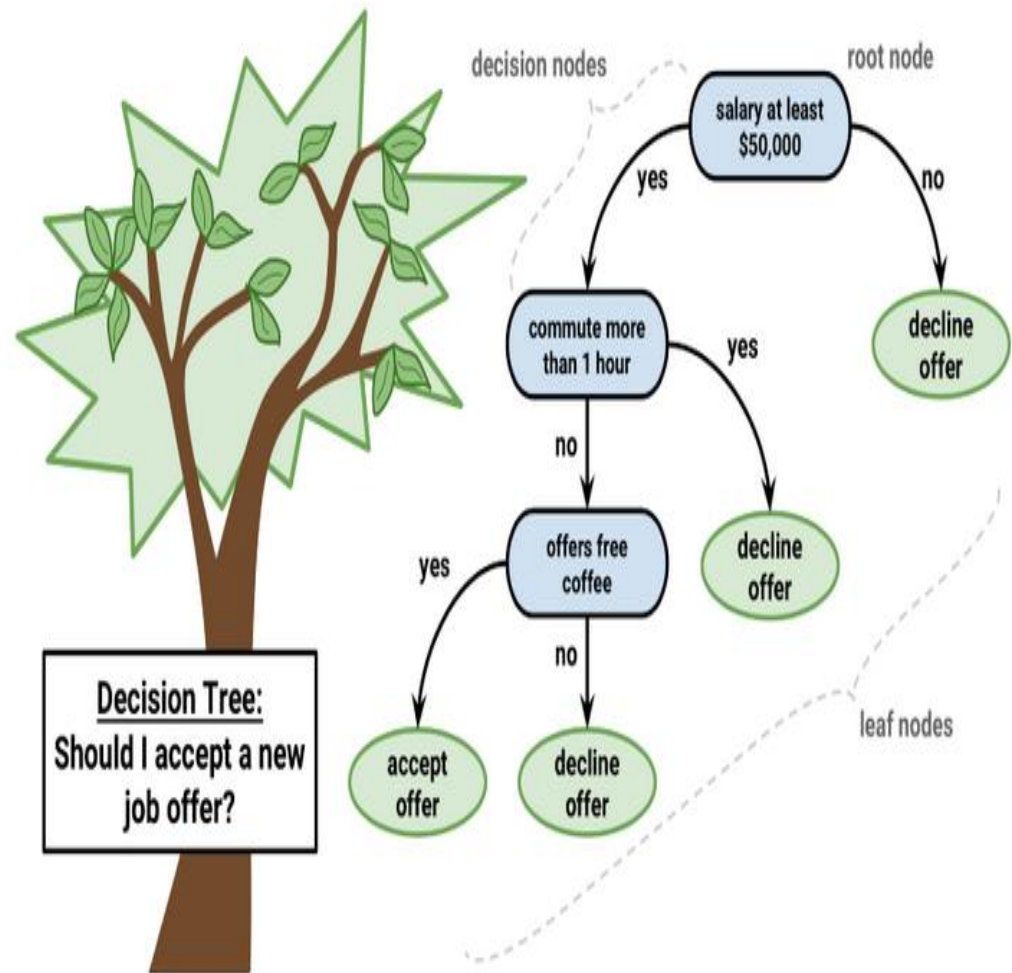
INT354

Machine Learning

Decision Trees and Random Forests

Decision Tree Learning

- **Breaking down data by making decisions based on asking a series of questions.**



Decision Tree Learning

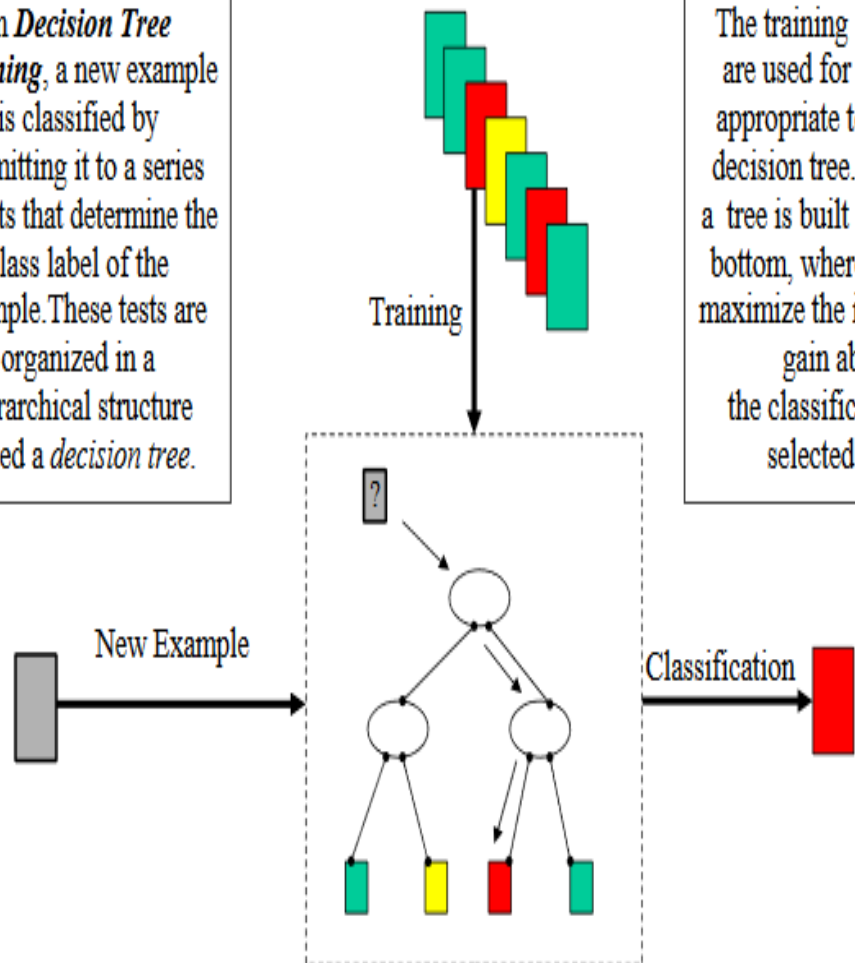
- A decision tree consists of
 - Nodes
 - Test for the value of a certain attribute.
 - Edges
 - Correspond to the outcome of a test.
 - Connect to the next node or leaf.
 - Leaves
 - Terminal nodes that predict the outcome.

Algorithm

1. Start at the root.
2. Perform the test.
3. Follow the edge corresponding to outcome.
4. Goto step 2 unless leaf.
5. Predict the outcome associated with the leaf.

In *Decision Tree Learning*, a new example is classified by submitting it to a series of tests that determine the class label of the example. These tests are organized in a hierarchical structure called a *decision tree*.

The training examples are used for choosing appropriate tests in the decision tree. Typically, a tree is built from top to bottom, where tests that maximize the information gain about the classification are selected first.



Design Decision Tree

| <i>Day</i> | <i>Temperature</i> | <i>Outlook</i> | <i>Humidity</i> | <i>Windy</i> | <i>Play Golf?</i> |
|------------|--------------------|----------------|-----------------|--------------|-------------------|
| 07-05 | hot | sunny | high | false | no |
| 07-06 | hot | sunny | high | true | no |
| 07-07 | hot | overcast | high | false | yes |
| 07-09 | cool | rain | normal | false | yes |
| 07-10 | cool | overcast | normal | true | yes |
| 07-12 | mild | sunny | high | false | no |
| 07-14 | cool | sunny | normal | false | yes |
| 07-15 | mild | rain | normal | false | yes |
| 07-20 | mild | sunny | normal | true | yes |
| 07-21 | mild | overcast | high | true | yes |
| 07-22 | hot | overcast | normal | false | yes |
| 07-23 | mild | rain | high | true | no |
| 07-26 | cool | rain | normal | true | no |
| 07-30 | mild | rain | high | false | yes |

Note: Consider “Outlook” as root node

Exercise

| | | | | | |
|-------|------|-------|--------|-------|---|
| today | cool | sunny | normal | false | ? |
|-------|------|-------|--------|-------|---|

| | | | | | |
|----------|------|-------|--------|-------|---|
| tomorrow | mild | sunny | normal | false | ? |
|----------|------|-------|--------|-------|---|

Good Attribute?

- **Prefers attributes that have a high degree of “order”.**
 - **Maximum Order: All examples are of the same class.**
 - **Minimum Order: All classes are equally likely.**

Entropy

Entropy is the measure of

- Impurity
- Disorder
- uncertainty

Entropy for two classes:

$$E(S) = -p_1 \cdot \log_2 p_1 - p_2 \cdot \log_2 p_2$$

S is the complete set,

p_1 is the proportion of examples in class 1 and

$p_2 = 1 - p_1$ is the proportion of examples in class 2.

Exercise

Compute entropy

- Outlook=sunny
- Outlook=overcast
- Outlook=rainy

Entropy for more classes

$$\begin{aligned} E(S) &= -p_1 \cdot \log p_1 - p_2 \cdot \log p_2 \dots - p_n \cdot \log p_n \\ &= - \sum_{i=1}^n p_i \cdot \log p_i \end{aligned}$$

Entropy Disadvantages

- Only computes the quality of a single subset of examples corresponds to a single value.

Average Entropy

- Computes the quality of the entire split corresponds to an entire attribute.

$$I(S, A) = \sum_i \frac{|s_i|}{|S|} \cdot E(Si)$$

S is the complete set.

A is Attribute that splits S into different subsets.

Properties of Entropy

- When node is pure, measure should be zero.
- When impurity is maximal, measure should be maximal.

Exercise

- **Compute the average entropy for attribute “Outlook”.**

Information Gain

$$\begin{aligned} \text{Gain}(S, A) &= E(S) - I(S, A) \\ &= E(S) - \sum_i \frac{|S_i|}{|S|} \cdot E(S_i) \end{aligned}$$

Where S is complete set and A is the attribute that splits the set S into subsets S_i .

Note: Maximizing information gain is equivalent to minimizing average entropy, because $E(S)$ is constant for all attributes A .

Exercise

- Compute the information gain for
 - $\text{Gain}(S, \text{Humidity})=?$
 - $\text{Gain}(S, \text{Wind})=?$
 - $\text{Gain}(S, \text{Outlook})=?$
 - $\text{Gain}(S, \text{Temperature})=?$

Note:

The attribute with **maximum** information gain is selected as root node.

Intrinsic Information of an attribute

- Amount of information need to tell which branch an instance belongs to

$$Int1(S, A) = - \sum_i \frac{|S_i|}{|S|} \log\left(\frac{|S_i|}{|S|}\right)$$

Note:

Attributes with higher intrinsic information are less useful.

Exercise

- **Compute intrinsic information of**
 - **Day**
 - **Temperature**
 - **Humidity**
 - **Windy**
 - **Outlook**

Gain Ratio

- **Modification of the information gain that reduces its bias towards multi-valued attributes.**

$$GR(S, A) = \frac{Gain(S, A)}{Int1(S, A)}$$

Exercise

- **Compute gain ratio of**
 - **Day**
 - **Temperature**
 - **Humidity**
 - **Windy**
 - **outlook**

Gini Index

- **Measure impurity**

$$Gini(S) = 1 - \sum_i p_i^2$$

- **Average Gini Index**

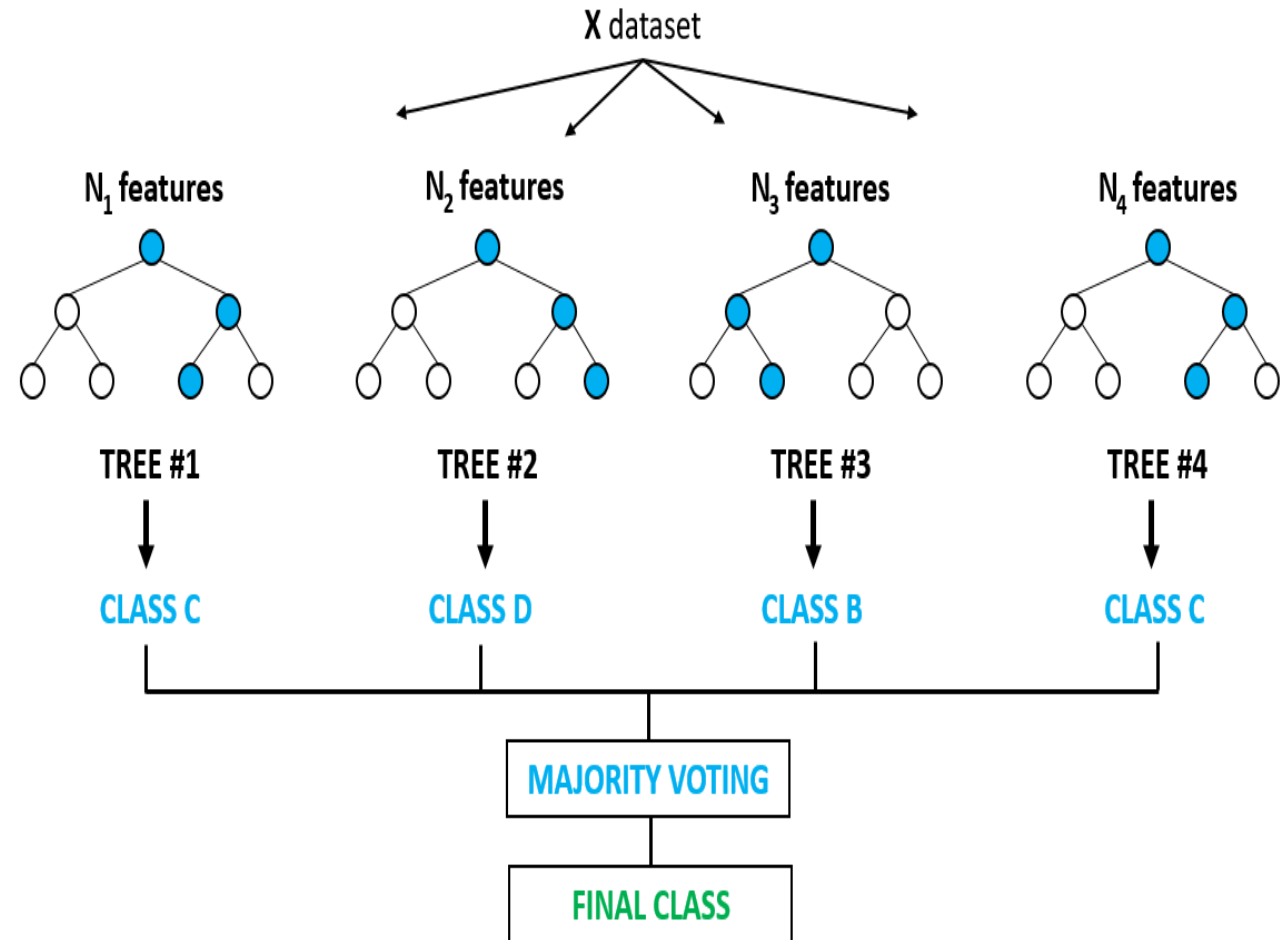
$$Gini(S, A) = \sum_i \frac{|S_i|}{|S|} \cdot Gini(S_i)$$

Pruning

- **Pre-pruning:**
 - Stop growing a branch when information becomes unreliable.
- **Post-pruning:**
 - Grow a decision tree that correctly classifies all training data.
 - Simplify it later by replacing some nodes with leafs.

Random Forest

- Builds multiple decision tree and merges them together to get a more accurate and stable prediction.



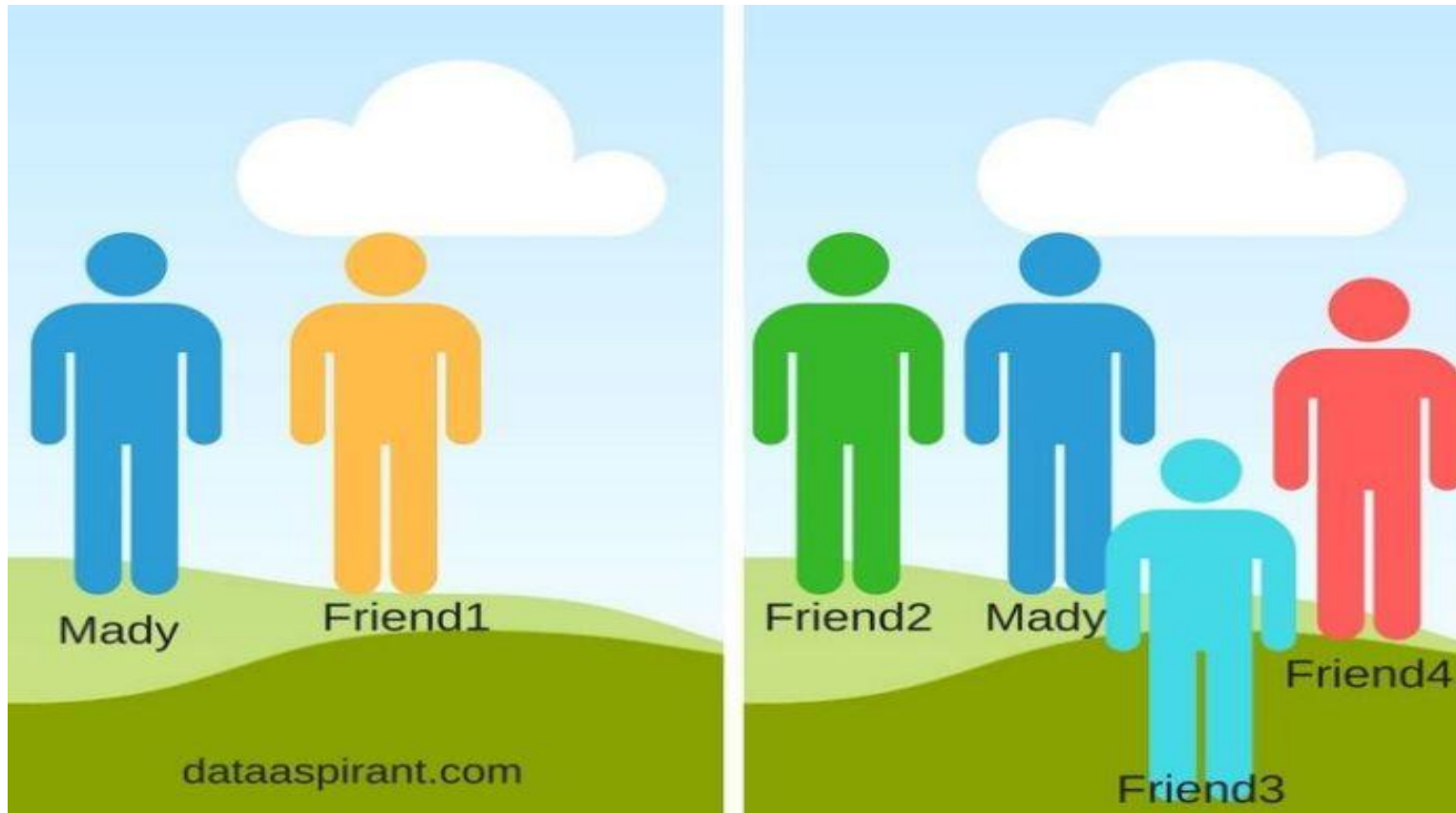
Random Forest Creation Algorithm

1. Randomly select “K” features from total “m” features.
 - Where $K \ll m$
2. Among the “K” features, calculate the node “d” using the best split point.
3. Split the node into daughter nodes using the best split.
4. Repeat 1 to 3 steps until “l” number of nodes has been reached.
5. Build forest by repeating steps 1 to 4 for “n” number of times to create “n” number of trees.

Random Forest Prediction Algorithm

1. Takes the **test features** and use the rules of each randomly created decision tree to predict the outcome and stores the predicted outcome.
2. Calculate the **vote** for each predicted target.
3. Consider the **high voted predicted target** as the final prediction from the random forest algorithm.

Random Forest Example

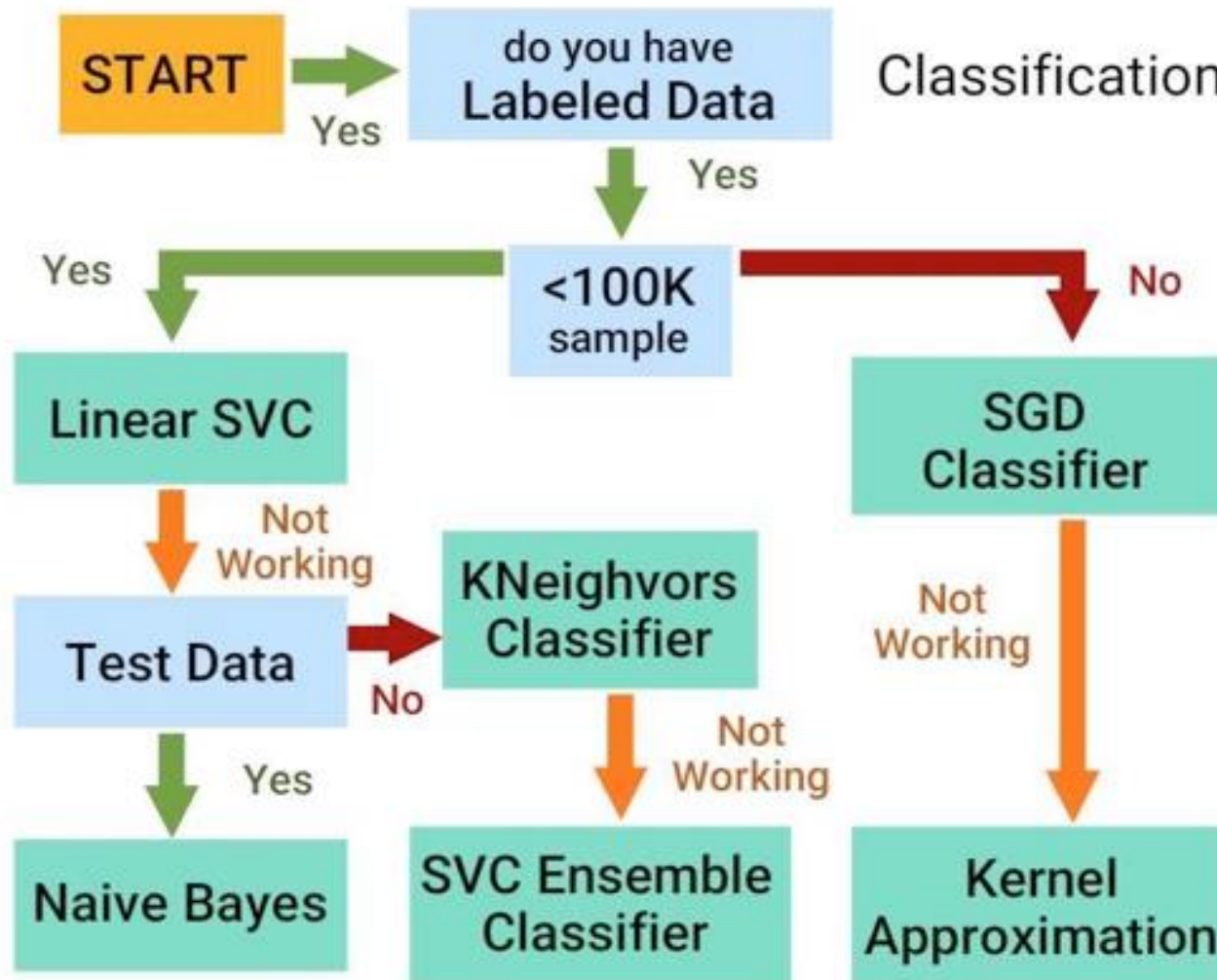


- Mady takes opinion from friends for some problem.

Why Random Forest Algorithm?

- Can be used for both classification and regression.
- Handles the missing value.
- Not over-fit the model.

Algorithm Selection



COMING UP
