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Ans to the ques no 1

a) Unicycle Model

- State Variables: x, y, θ
- Control Variables: v, ω (angular velocity)

Equations:

- $dx/dt = v * \cos(\theta)$
- $dy/dt = v * \sin(\theta)$
- $d\theta/dt = \omega$

b) Differential Drive Robot

- State Variables: x, y, θ
- Control Variables: ω_r (right wheel angular velocity), ω_l (left wheel angular velocity)
- Constant Variables: r (wheel radius), L (distance between wheels)

Equations:

- $dx/dt = (r / 2) * (\omega_r + \omega_l) * \cos(\theta)$

- $dy/dt = (r / 2) * (\omega_r + \omega_l) * \sin(\theta)$
- $d\theta/dt = (r / L) * (\omega_r - \omega_l)$

c) Simplified Car Model

- State Variables: x, y, θ
- Control Variables: v (linear velocity), ϕ (steering angle)
- Constant Variables: L (wheelbase)

Equations:

- $dx/dt = v * \cos(\theta)$
- $dy/dt = v * \sin(\theta)$
- $d\theta/dt = (v / L) * \tan(\phi)$

d) Planar Quadrotor

- State Variables: $x, y, \theta, \dot{x}, \dot{y}, \omega$
- Control Variables: T_1, T_2
- Constant Variables: m (mass), g (gravity), I_{zz} (moment of inertia)

Equations:

- $\dot{x} = dx$
- $\dot{y} = dy$
- $\dot{\theta} = \omega$

- $d^2x/dt^2 = -(T_1 / m) \times \sin(\theta)$
- $d^2y/dt^2 = (T_1 / m) \times \cos(\theta) - g$
- $d\omega/dt = T_2 / I_{zz}$

1(ii)

The Unicycle model moves forward and turns using two controls: speed and turning rate. The Differential Drive robot moves using two wheels. The Simplified Car model moves like a normal car.