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Standard      Section      Roll No.

Subject AI LAB

**School / College**

S. No.	Date	Title	Page No.	Teacher's Sign
01	24.09.24	LAB - 01 Tic-tac-toe game	01	N, 24 SAH
02	01.10.24	LAB - 02 Vacuum Cleaner Problem	02 - 03	D 1/10/24
03	8.10.24	LAB - 03 8 puzzle problem - BFS	04 - 05	D 25/10/24
04	15.10.24	LAB 8 puzzle problem - A* algorithm	6 - 10	JW 15/10/24
05	22.10.24	LAB ① Iterative Deepening Search ② Hill climbing search	11 - 15	D 22/10/24

S. No.	Date	Title	Page No.	Teacher's Sign
	27.10.24	LAB - 6 Simulated Annealing		Do 29/10/24
	18.11.24	LAB Propositional logic - Truth Table Enumeration		b 12/11
	19.11.24	LAB - 7 First Order Logic - Unification		Ag-11
	26.11.24	LAB 8 First Order Logic - Forward Chaining		10 26/11
	2.12.24	LAB - 09. First Order Logic - Resolution		
	16.12.24	LAB-10 Alpha Beta Pruning		

implement Tic-tac-toe gameAlgorithm

- ① Create a  $3 \times 3$  board using a two dimensional array
- ② Display the empty board.
- ③ Define a function called evaluate() to check whether the board is filled or not.
- ④ Create a function called row-win() to check whether the rows are filled by winner.
- ⑤ Similarly, create column-win() and diag-win().
- ⑥ Randomly choose a player to begin playing
- ⑦ Display output (the board) after each move.
- ⑧ The player inputs the x coordinate and y-coordinate to move.
- ⑨ Repeatedly check if any of the winning arrangement returns true.
- ⑩ If the current player has won, the game, then print a winning game message and break the loop.
- ⑪ If the game is a draw, print draw message.

Ques 21-a-21

01/10/34

LAB-02

(Program - 4)

## Implement Vacuum Cleaner world

function REFLEX - VACUUM - AGENT ([location, status]) return an action

if status = Dirty then return Suck  
else if location = A then return Right  
else if location = B then return Left

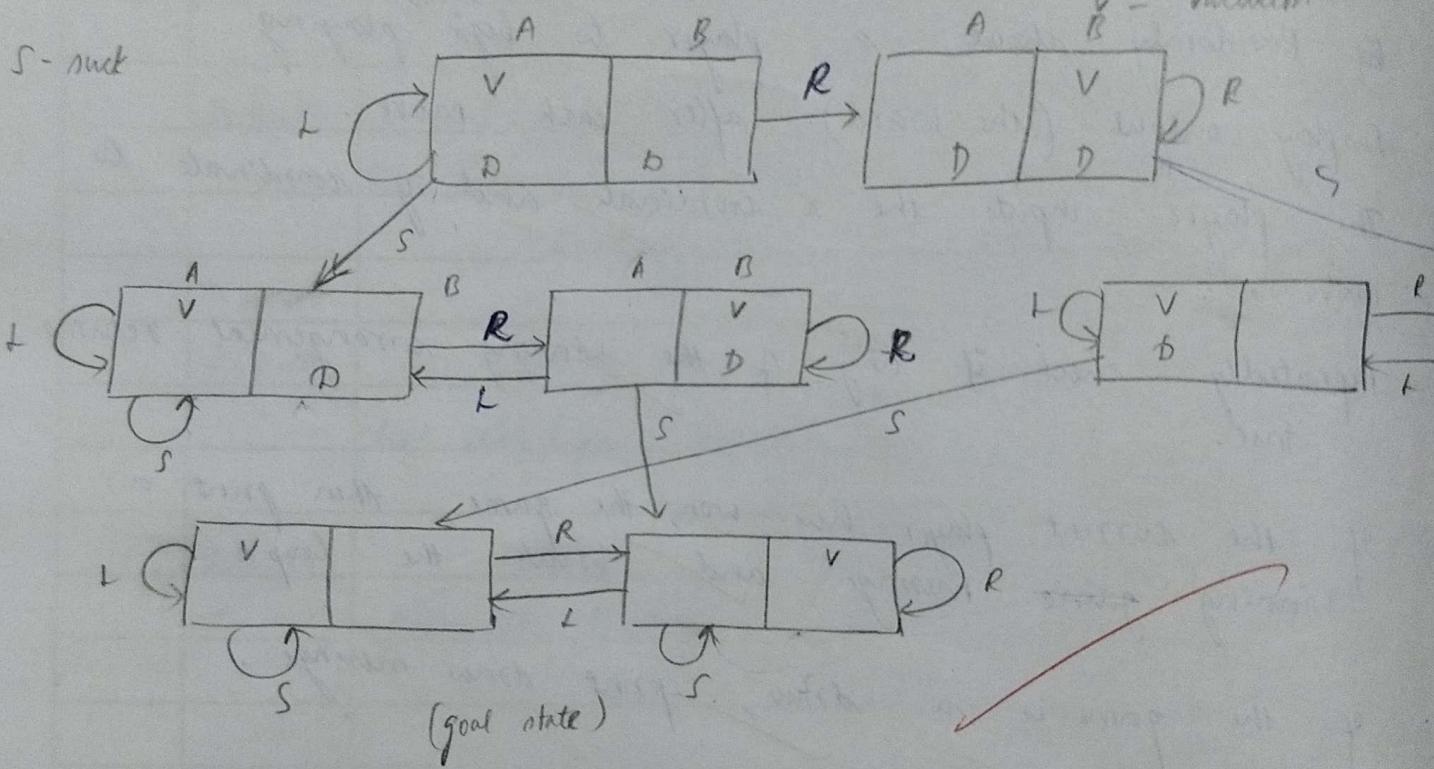
L - Left

R - Right

D - Dust

V - Vacuum

## State space for the vacuum world



Simple model

O's and S (input)

- ① Ask location
- ② Status
- ③ Is dust available in this room? // enter location
- ④ cost + everytime you suck)

enter status = 0/1

is dust available in room?

## ALGORITHM

- ① Define a function called `vacuum-world()` where user input of the location of the vacuum, the status of the room and status of other room.
- ② The goal state is defined as  $[A, 0, B, 0]$  and cost is initialized to 0.
- ③ Depending on the user's input, the following steps are followed -
  - (i) Location is specified as A/B and status is 0 when clean, 1 when room is dirty.
  - (ii) If the input location is A and the room is dirty, then vacuum has to suck and the goal state for room A is changed to zero.
  - (iii) Incrment the cost variable
  - (iv) If the other room's status is dirty, then the vacuum has to move right and suck. ~~and goal~~
  - (v) Goal of the input location is A and the room is clean, then depending on the other room's status the vacuum will remain in room A or move right to room B.

④ Goal state attained. and cost calculated.

Ques  
10/27

08/10

LAB - 03

AI - 8 puzzle problem using BFS and DFS

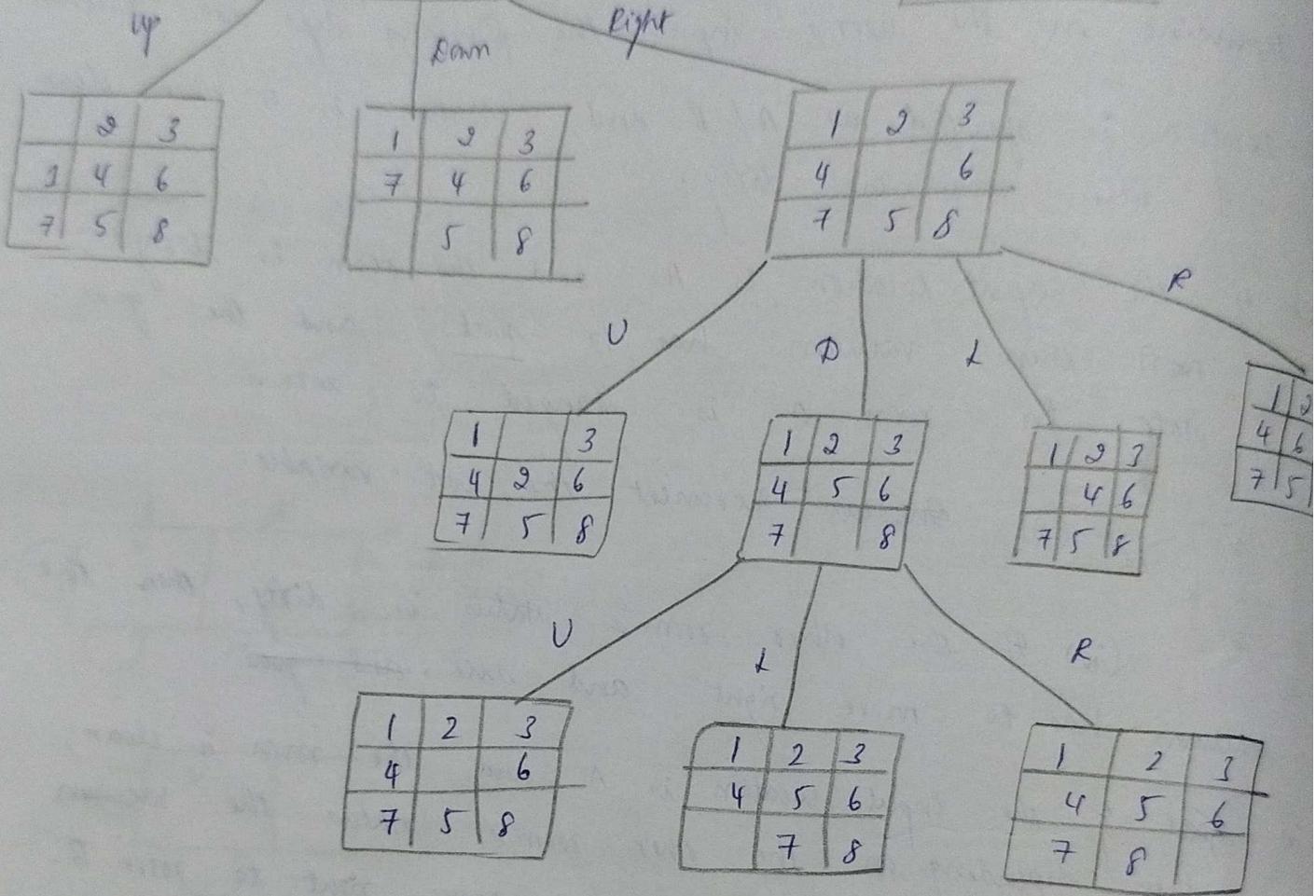
\* BFS - Non heuristic approach

Initial state -

1	2	3
4	6	
7	5	8

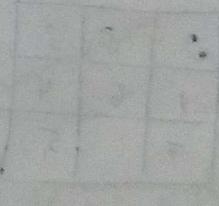
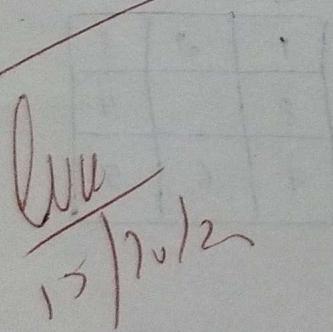
goal state -

1	2	3
4	5	6
7	8	



- ① Input : Initial state and fi goal state ✓
- ② Depending on blank space, check for possible actions - UP, DOWN, RIGHT, LEFT
- ③ Implement ^ function to locate blank tile in the current state.
- ④ Implement a function to check if the current state matches the goal state.

- ⑤ Create a function to check if the current state matches the goal state
- ⑥ Implement a function to generate a new board configuration by applying a move.
- ⑦ Initialize a queue and add starting state -
- Use a set to ~~not~~ track visited states to avoid cycles.
  - Each entry in the queue consists of current state and the path taken to reach it.
- ⑧ Implement a function to print the configuration once the goal state is reached.
- ⑨ Print the series of moves that moved from initial state to goal state :



For 8 puzzle problem using A\* implementation to calculate f(n) using -

a)  $g(n)$  = depth of a node

$h(n)$  = heuristic value  $\Rightarrow$  no. of misplaced tiles

$$f(n) = g(n) + h(n)$$

b)  $g(n)$  = depth

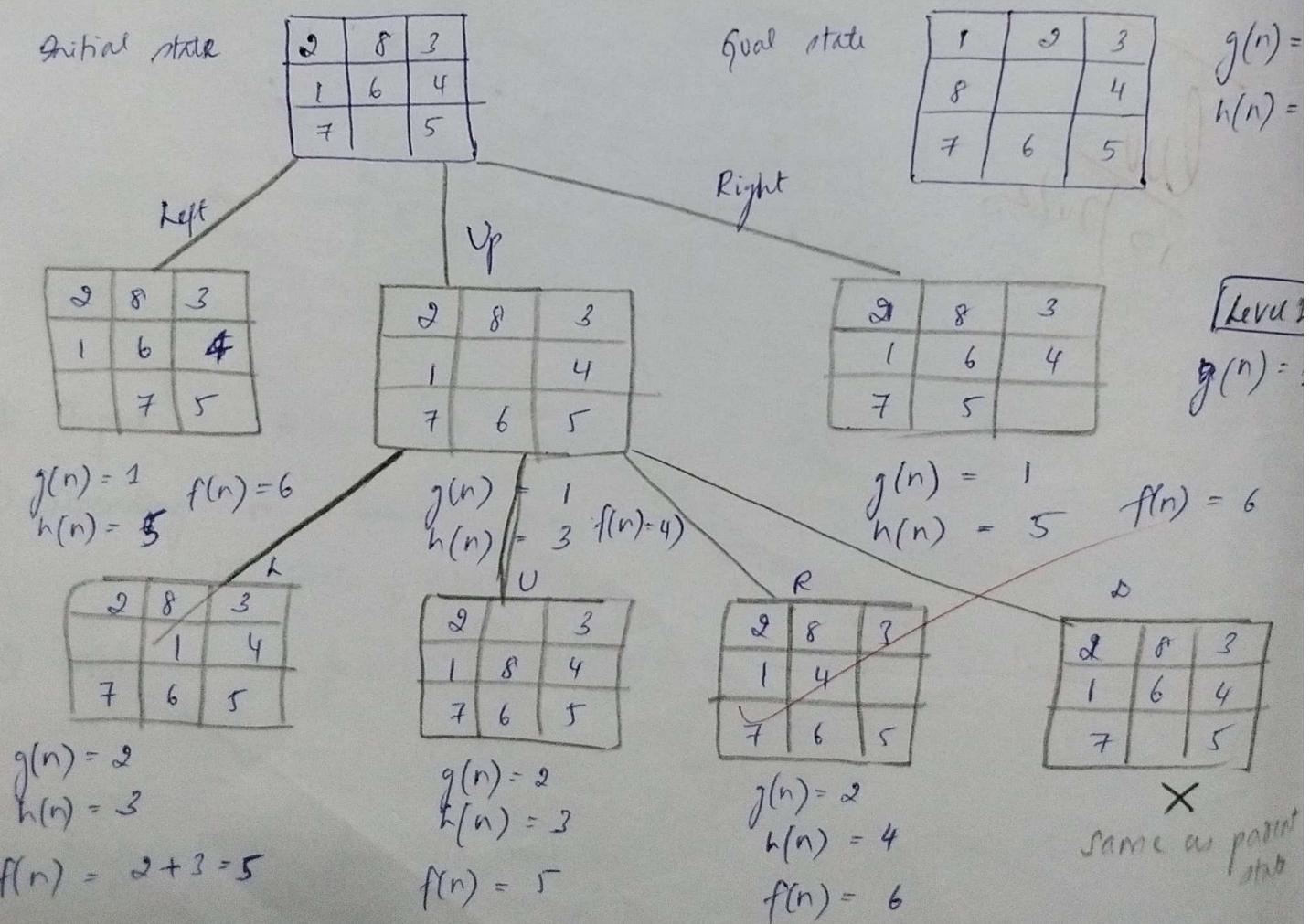
$h(n)$  = heuristic value  $\Rightarrow$  Manhattan distance

$$f(n) = g(n) + h(n)$$

a) NUMBER OF MISPLACED TILES

minimum no. of displaced tiles

Draw the state space diagram for -



left

2	8	3
1	4	
7	6	5

$$g(n) = 9$$

$$h(n) = 3$$

$$f(n) = 5$$

up

2	3	
1	8	4
7	6	5

V

2	8	3
1	4	
7	6	5

R

2	8	3
1	4	
7	6	5

D

2	8	3
1	4	
7	6	5

2	3	
1	8	4
7	6	5

2	3	
1	8	4
7	6	5

R

2	3	
1	8	4
7	6	5

$$g(n) = 3$$

$$h(n) = 3$$

$$f(n) = 6$$

X

$$g(n) = 7$$

$$h(n) = 4$$

$$f(n) = 7$$

$$f(n) = 7$$

$$h(n) = 2$$

$$f(n) = 5$$

$$g(n) = 7$$

$$h(n) = 3$$

$$f(n) = 6$$

$$g(n) = 3$$

$$h(n) = 3$$

$$f(n) = 6$$

$$g(n) = 4$$

$$h(n)$$

X

2	3	
1	8	4
7	6	5

$$g(n) = 4$$

$$h(n) = 1$$

$$f(n) = 5$$

2	3	
1	8	4
7	6	5

U

2	3	
1	8	4
7	6	5

$$g(n) = 5$$

Goal state

2	3	
1	8	4
7	6	5

2	3	
1	8	4
7	6	5

X

O

## \* Algorithm

- Step 1 : Place the starting node in the open list
- Step 2 : Check if the open list is empty or not if the list is empty then return failure and stops. // No input
- Step 3 : Select the node from the OPEN list which has the smallest value of evaluation function ( $g(n) + h(n)$ ) if node 'n' is goal node, then return success and stop the process.
- Step 4 : Expand node 'n' and generate all of its successors and add them into the closed list. For each successor 'n', check whether 'n' is already in the open or closed list. If not then complete the evaluation function for 'n' and place it in open list.
- Step 5 : Else if node 'n' is already in open and closed, then it should be attached to the back pointer which reflects the lowest  $f(n)$  value.

WU  
10/11h

b) MANHATTAN DISTANCE

Initial state

2	8	3
1	6	4
7	5	

$$g(n) = 0$$

Goal state

1	2	3
8		4
7	6	5

L

2	8	3
1	6	4
7	5	

$$g(n) = 1$$

$$h(n) = 6$$

$$f(n) = 7$$

V

2	8	3
1	4	6
7	5	6

$$g(n) = 1$$

$$h(n) = 4$$

$$f(n) = 5$$

R

2	8	3
1	6	4
7	5	

$$g(n) = 1$$

$$h(n) = 6$$

$$f(n) = 7$$

L

2	8	3
1	4	6
7	6	5

$$g(n) = 2$$

$$h(n) = 2 + 1 + 2 = 5$$

$$f(n) = 7$$

V

2	3	
1	8	4
7	6	5

$$g(n) = 2$$

$$h(n) = 1 + 1 + 1 = 3$$

R

2	3	
1	4	6
7	6	5

$$g(n) = 2$$

$$h(n) = 1 + 1 + 1 + 2 = 5$$

$$f(n) = 7$$

D

2	8	3
1	6	4
7	5	

X

L

2	3	
1	8	4
7	6	5

$$g(n) = 3$$

$$h(n) = 1 + 1 = 2$$

$$f(n) = 5$$

D

2	3	
1	4	6
7	6	5

$$g(n) = 3$$

$$h(n) = \text{X}$$

R

2	3	8
1	8	4
7	6	5

$$g(n) = 3$$

$$h(n) = 1 + 1 + 1 + 1 = 4$$

$$f(n) = 7$$

R

2	3	
1	8	4
7	6	5

X

1	2	3
8		4
7	6	5

$$g(n) = 4$$

$$h(n) = 1$$

$$f(n) = 5$$

R

1	2	3
8		4
7	6	5

✓

1	2	3
7	8	4
6	5	

$$g(n) = 5$$

$$h(n) = 0$$

$$f(n) = 5$$

Manhattan distance for  $g(n) = 1$

1	2	3	4	5	6	7	8
1	1	0	0	0	1	1	0

left

$$\text{Sum} = 1 + 1 + 1 + 1 + 2 = 6$$

1	2	3	4	5	6	7	8
1	1	0	0	0	0	0	0

up

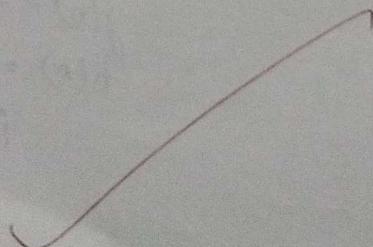
$$\text{Sum} = 4$$

1	2	3	4	5	6	7	8
1	1	0	0	1	1	0	0

right

$$\text{Sum} = 6$$

Manhattan distance for  $g(n) = 2$



QW  
13710/m

Implement iterative deepening search algorithm — (DFS)

Algorithm —

1. For each child of the current node .
2. If it is the target node, return the node .
3. If the current maximum depth is reached, return .
4. Set the current node to this node and go back to 1 .
5. After having gone all through all children, go to the next child of the parent (the next sibling)
6. After having gone through all children of the start node , increase the maximum depth and go back to 1 .
7. If we have reached all leaf (bottom) nodes, the goal node doesn't exist .

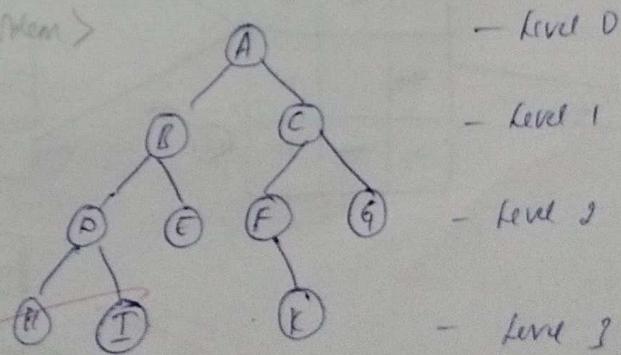
function ITERATIVE-DEEPENING-SEARCH (problem) returns a solution or failure

for depth = 0 to  $\infty$  do

result  $\leftarrow$  DEPTH-LIMITED-SEARCH (problem, depth)

if result  $\neq$  cutoff then return result .

<Explore with 8 puzzle problem>



1st iteration  $\rightarrow$  A

2nd iteration  $\rightarrow$  A, B, C

3rd  $\rightarrow$  A, B, D, E, C, F, G

4th  $\rightarrow$  A, B, D, H, I, E, C, F, K, G .

Initial state:

9	8	3
1	6	4
7		5

$$\text{limit} = 0$$

Goal state:

1	2	3
8		4
7	6	5

R

A

L

V

9	8	3
1	6	4
7		5

9	8	3
1	6	4
7	6	5

B

V

R

9	8	3
1	6	4
7	5	

P

V

U

$$\text{limit} = 2$$

$$\text{limit} = 1$$

$$\text{limit} = 0$$

9	8	3
1	6	4
7	5	

G

H

I

9	8	3
1	6	4
7	5	

J

9	8	3
1	6	4
7	6	5

K

9	8	3
1	6	4
7	6	5

L

9	8	3
1	6	4
7	6	5

M

9	8	3
1	6	4
7	7	5

N

Return Failure

- 1st iteration - A
- 2nd iteration - A, B, C, D,
- 3rd iteration - A, B, E, F, C, G, H, I, J, D, K, L

UV  
2<sup>nd</sup> tut.

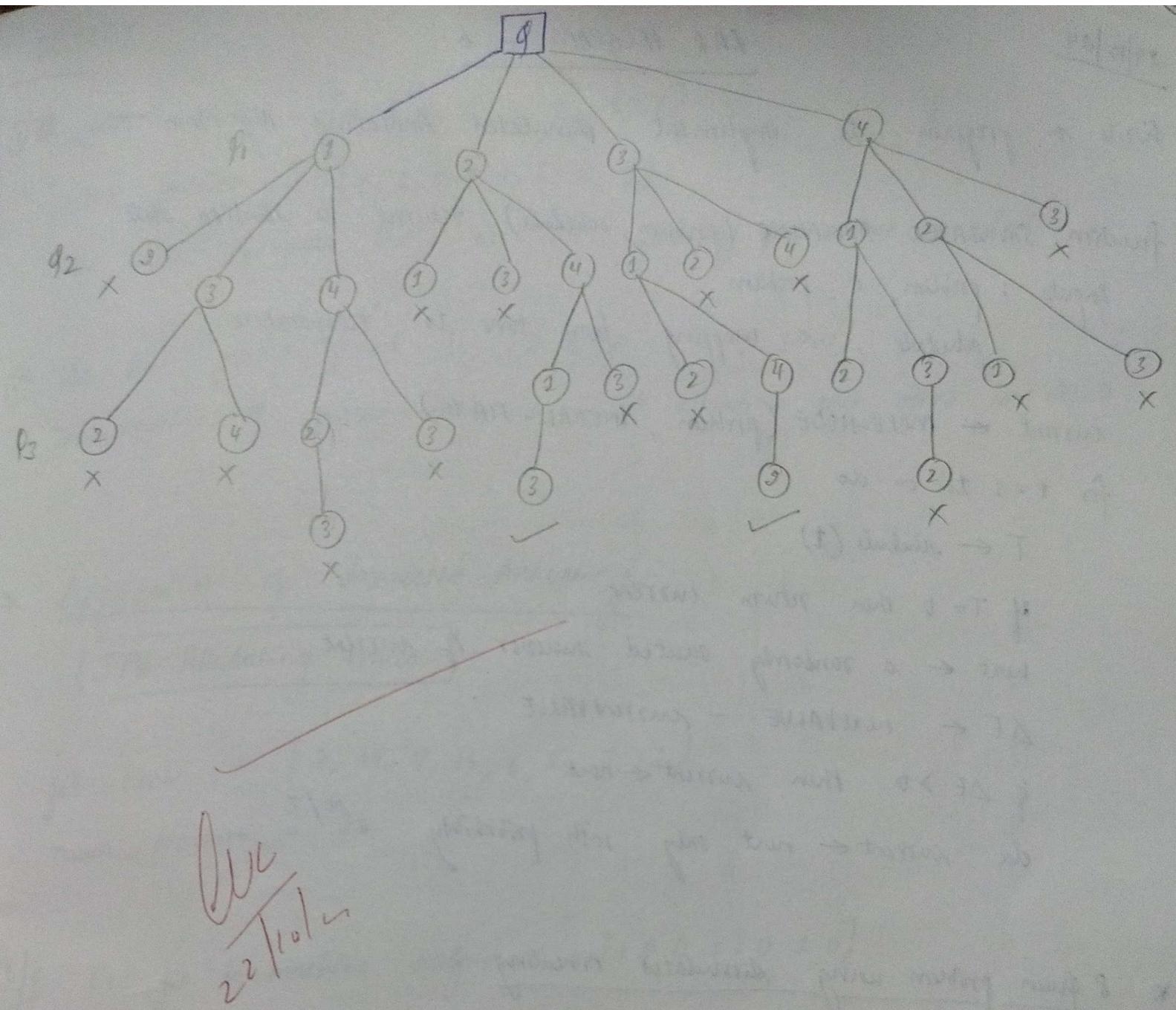
Implement hill climbing search algorithm to solve N-queens problem

### Algorithm -

function HILL-CLIMBING (problem) returns a state that is a local maximum  
current  $\leftarrow$  MAKE-NODE (problem, INITIAL-STATE)  
loop do  
    neighbour  $\leftarrow$  a highest valued successor of current  
    if neighbour.VALUE  $\leq$  current.VALUE then return current.STATE  
    current  $\leftarrow$  neighbour

### Problem Formulation -

- State : 4 queens on the board. One queen per column.
  - Variables :  $x_0, x_1, x_2, x_3$  where  $x_i$  is the position row position of the queen in column  $i$ .
    - : Assume that there is one queen per column.
  - Domain for each variable :  $x_i \in \{0, 1, 2, 3\}, \forall i$
- Initial state - a random state
- Goal state - 4 queens on the board. No pair of queens are attacking each other.
- Neighbour relation - Swap the row positions of two queen.
- Cost function - The number of pairs of queens attacking each other, directly or indirectly.



29/10/24

## LAB PROGRAM - b

Write a program to implement Simulated Annealing Algorithm -

function SIMULATED-ANNEALING (problem, schedule) returns a solution state

inputs : problem, a problem

schedule , a mapping from time to "temperature"

current  $\leftarrow$  MAKE-NODE (problem, INITIAL-STATE)

for  $t = 1$  to  $\infty$  do

$T \leftarrow$  schedule ( $t$ )

if  $T = 0$  then return current

next  $\leftarrow$  a randomly selected successor of current

$\Delta E \leftarrow$  nextVALUE - currentVALUE

if  $\Delta E > 0$  then current  $\leftarrow$  next

else current  $\leftarrow$  next only with probability  $e^{\Delta E/T}$

\* 8 Queen problem using Simulated Annealing

mlrose - Python package

mlrose for simulated annealing

① Import the mlrose and numpy libraries

②

$$P(x, x_j, T) = \begin{cases} 1 & F(x_j) \geq F(x) \\ e^{\frac{F(x_j) - F(x)}{T}} & F(x_j) < F(x) \end{cases}$$

## OUTPUT

① initial position =  $[4, 6, 1, 5, 2, 0, 3, 7]$

best position =  $[0, 6, 4, 7, 1, 3, 5, 2]$

The number of queens that are not attacking each other is 8.0.

② The best position found is  $[2, 5, 7, 1, 3, 0, 6, 4]$

The number of queens that are not attacking each other is: 8.0

## \* Application of Simulated Annealing

### Job Scheduling Problems

job-time =  $[2, 14, 4, 16, 6, 5, 3, 12]$

num-machine = 3

O/P Best job-to-machine assignment =  $[1 \ 2 \ 0 \ 1 \ 2 \ 0 \ 1 \ 0]$

minimum makespan : 21.0

Machine 1 jobs :  $[(2, 4), (5, 5), (7, 12)]$  Total time : 21

Machine 2 jobs :  $[(0, 2), (3, 16), (6, 3)]$  Total time : 21

Machine 3 jobs :  $[(1, 14), (4, 6)]$  Total time : 20

WAT  
29-10-22

WEEK - 07

12/11

Create a knowledge base using propositional logic and show that the query entails the knowledge base or not =

Algorithm :

function  $\text{TT-ENTAILS?}(\text{KB}, \alpha)$  returns true or false

inputs :  $\text{KB}$ , - the knowledge base, a sentence in propositional logic  
 $\alpha$  - the query, a sentence in propositional logic

$\text{symbols} \leftarrow$  a list of the proposition symbols in  $\text{KB}$  and  $\alpha$

return  $\text{TT-CHECK-ALL}(\text{KB}, \alpha, \text{symbols}, \{\})$

function  $\text{TT-CHECK-ALL}(\text{KB}, \alpha, \text{symbols}, \text{model})$  returns true or false

if  $\text{EMPTY?}(\text{symbols})$  then

    if  $\text{PL-TRUE?}(\text{KB}, \text{model})$  then return  $\text{PL-TRUE?}(\alpha, \text{model})$   
 else return true // when KB is false, always return true

else do

$P \leftarrow \text{FIRST}(\text{symbols})$

$\text{rest} \leftarrow \text{REST}(\text{symbols})$

    return  $(\text{TT-CHECK-ALL}(\text{KB}, \alpha, \text{rest}, \text{model}) \vee \{P=\text{true}\})$   
 and

$\text{TT-CHECK-ALL}(\text{KB}, \alpha, \text{rest}, \text{model}) \vee \{P=\text{false}\})$

Truth table

$P$	$Q$	$\neg P$	$P \wedge Q$	$P \vee Q$	$P \Leftrightarrow Q$	$P \Rightarrow Q$
false	false	true	false	false	true	true
false	true	true	false	true	false	true
true	false	false	false	true	false	true
true	true	false	true	true	true	false

$\wedge$  - and      $\Rightarrow$  implies if  $P$  then  $Q$

$\vee$  - or

Example

$$\alpha = A \vee B$$

$$KB = (A \vee C) \wedge (\neg B \vee \neg C)$$

Checking  $KB \neq \alpha$

A	B	C	$A \vee C$	$\neg B \vee \neg C$	$KB$	$\alpha$
F	F	F	F	T	F	F
F	F	T	T	F	F	F
F	T	F	F	T	F	T
F	T	T	T	T	T	T
T	F	F	T	T	T	T
T	F	T	T	F	F	T
T	T	F	T	T	T	T
T	T	T	T	T	T	T

OP See<sup>n</sup>  
 See  
 12/11/2021

# LAB PROGRAM - 7

19/11/24

## Implement unification in First Order Logic

Algorithm : Unify ( $\psi_1, \psi_2$ )

Step 1 : If  $\psi_1$  or  $\psi_2$  is a variable or constant, then :

a) If  $\psi_1$  or  $\psi_2$  are identical, then return NIL.

b) Else if  $\psi_1$  is a variable,

a. then if  $\psi_1$  occurs in  $\psi_2$ , then return FAILURE.

b. Else return  $\{(\psi_2 / \psi_1)\}$ .

c) Else if  $\psi_2$  is a variable,

a. If  $\psi_2$  occurs in  $\psi_1$ , then return FAILURE,

b. Else return  $\{(\psi_1 / \psi_2)\}$ .

d) Else return FAILURE.

Step 2 : If the initial predicate symbol in  $\psi_1$  and  $\psi_2$  are not same, then return FAILURE.

Step 3 : If  $\psi_1$  and  $\psi_2$  have a different number of arguments, then return FAILURE.

Step 4 : Set substitution set (SUBST) to NIL.

Step 5 : For  $i=1$  to the number of elements in  $\psi_1$ ,

a) Call Unify function with the  $i$ th element of  $\psi_2$  and put the result into  $s$ .

b) If  $s = \text{failure}$ , then return failure.

c) If  $s \neq \text{NIL}$ , then do -

a. Apply  $s$  to the remainder of both L1 and L2.

b. SUBST = APPEND ( $s$ , SUBST).

Step 6 : Return SUBST.

$$\text{Ex: I } P(x, F(y)) \rightarrow \textcircled{1} \quad \textcircled{1} \text{ predicate}$$

$$P(a, F(g(x))) \rightarrow \textcircled{2} \quad \textcircled{2} \text{ no. of arguments}$$

$\textcircled{1}$  and  $\textcircled{2}$  are identical if  $x$  is replaced with 'a' in  $\textcircled{1}$

$$P(a, F(y))$$

if  $y$  is replaced with  $g(z)$ .

$$P(a, F(g(z)))$$

$$\text{II } Q(a, g(z, a), f(y)) \rightarrow \textcircled{1}$$

$$Q(a, g(f(b), a), z) \rightarrow \textcircled{2}.$$

Replace  $z$  in  $\textcircled{1}$  with  $f(b) \Rightarrow Q(a, g(f(b), a), f(y))$

Replace  $f(y)$  in  $\textcircled{1}$  with  $z \Rightarrow \underline{Q(a, g(f(b), a), z)}$

$$\varphi_1) \quad \Psi_1 = P(f(a), g(x))$$

$$\Psi_2 = P(x, x)$$

fact As the predicates  $f$  and  $g$  are distinct and not same, they cannot be substituted as the same variable  $x$ .

Unification fail

$$\varphi_2) \quad \Psi_1 = P(b, z, f(g(z))) \rightarrow \textcircled{1}$$

$$\Psi_2 = P(z, f(y), f(y)) \rightarrow \textcircled{2}.$$

Replace  $b$  with  $z$  in  $\textcircled{1}$   $P(z, z, f(g(z)))$

$z$  with  $f(y)$  in  $\textcircled{1}$   $P(z, f(y), f(g(z)))$

$g(z)$  with  $y$   $P(z, f(y), f(y))$

## OUTPUT

Case 1 :  $P(f(a), f(b))$  and  $P(z, x)$ .

Unification unsuccessful!

Case 2 :  $P(t, x, f(g(z)))$  and  $P(z, f(y), f(y))$

Replace  $b$  with  $z$

Replace  $x$  with  $f(y)$

Replace  $y$  with  $g(z)$

Unification successful.

A  
/ Q 11.15

For a given case study you should  
create a knowledge base consisting of first order logic statements and  
prove the given query using forward reasoning.

Algorithm : FORWARDREASONING

function FOL-FC-ASK (KB,  $\alpha$ ) returns a substitution or false

inputs : KB , the knowledge base , a set of first order definite clauses.

$\alpha$  , the query, an atomic sequence

local variable : new, the new sentences inferred on each iteration

repeat until new is empty

new  $\leftarrow \{\}$

for each rule in KB do

$(p_1 \wedge \dots \wedge p_n \Rightarrow q) \leftarrow \text{STANDARDIZE-VARIABLES}(\text{rule})$

for each  $\theta$  such that  $\text{SUBST}(\theta, p_1 \wedge \dots \wedge p_n) =$   
 $\text{SUBST}(\theta, p'_1 \wedge \dots \wedge p'_n)$

for some  $p'_1, \dots, p'_n$  in KB

$q' \leftarrow \text{SUBST}(\theta, q)$

if  $q'$  does not unify with some sentence already in  
KB or new then

add  $q'$  to new

$\phi \leftarrow \text{UNIFY}(q', \alpha)$

if  $\phi$  is not fail then return  $\phi$

add new to KB

return false.

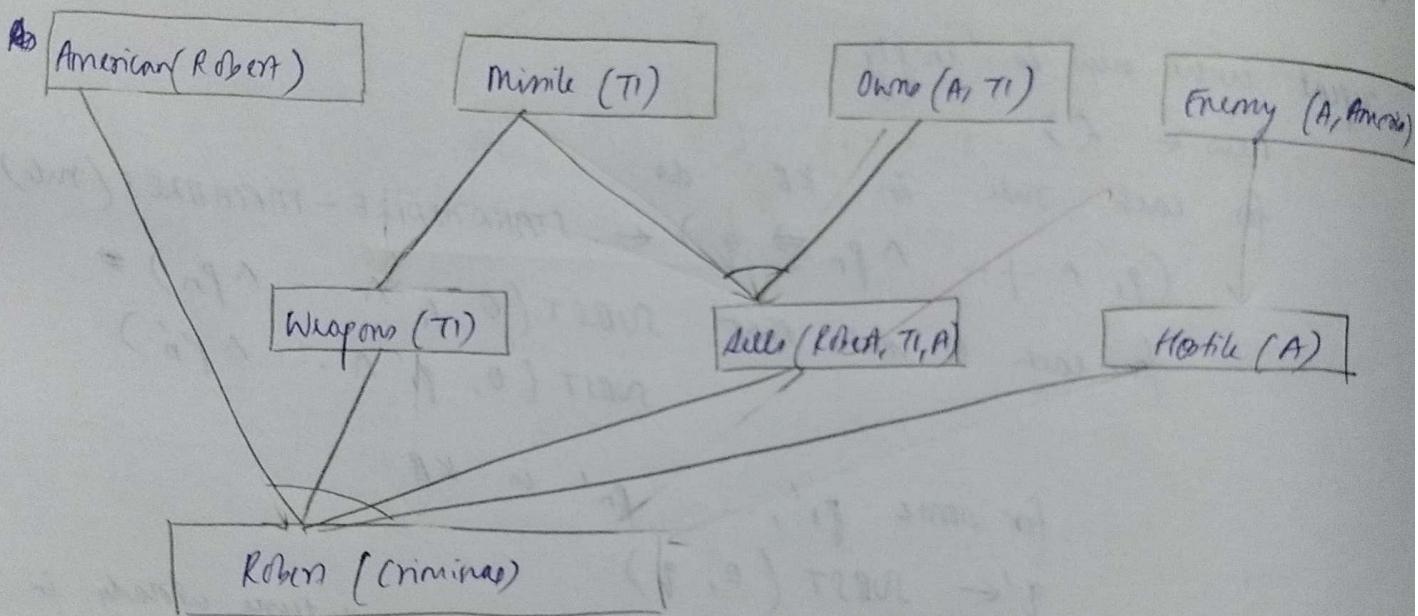
o/p

Query  $\{C\}$ : 'John' } is TRUE with substitution of 'C': 'John'

KB = [ $\{L(A) : "x"\}, \{L(B) : "x"\}, L(C) : "x\}$ , #  $A(?)$  and  $B(?)$ ,  
 $(A : "John")$ , # Fact:  $A(John)$   
 $(B : "John")$ , # Fact:  $B(John)$ ]  
]

query  $\{C\}$ : "John".

Off



- It is a crime for an American to use weapons to hostile nation.

Let's say p, q, r are variable.  
Rule 1

American(p)  $\wedge$  weapon(q)  $\wedge$  sells(p, q, r)  $\wedge$  Hostile(r)  $\Rightarrow$  Criminal(p)

- Country A has some missile.

$\exists x \text{ owns}(A, x) \wedge \text{missile}(x)$

owns(A, T1)

missile(T1)

• All of the missiles were sold to country A by Robert  
~~rule<sup>2</sup>~~  $\forall x \text{ missile}(x) \cdot A \text{ owns}(A, x) \Rightarrow \text{sell}(\text{Robert}, x, A)$ .

• missiles are weapons.

~~rule<sup>3</sup>~~ missile( $x$ )  $\Rightarrow$  weapon( $x$ )

• Enemy of America is known as hostile

~~rule<sup>4</sup>~~  $\forall x \text{ Enemy}(x, \text{America}) \Rightarrow \text{hostile}(x)$

To prove : Robert is criminal

**Facts**

- ① Robert is an American.
- ② Country A is an enemy of America.

~~date~~  
26-11-22

## LAB PROGRAM - 9

Convert a given first order logic statement into resolution -

Basic steps for proving a conclusion  $S$  given premises -

Premise, ... premise  $n$

(all expressed in FOL)

1. Convert all sentences to CNF.
2. Negate conclusion  $S$  and convert result to CNF.
3. Add negated conclusion  $\neg S$  to the premise clauses.
4. Repeat until contradiction or no progress is made -
  - a) Select 2 clauses (call them parent clauses)
  - b) Resolve them together, performing all required unifications.
  - c) If resultant is the empty clause, a contradiction has been found (i.e.)  $S$  follows from the premises
  - d) If not, add resultant to the premises.

If we succeed in step 4, we have proved the conclusion.

Hyp : Tom eats fruit

Example

given the KB or premises :

- ① John likes all kind of food.
- ② Apple and vegetables are food.
- ③ Anything anyone eats and not killed is food.
- ④ Anil eats peanuts and still alive.
- ⑤ Harry eats everything that Anil eats.
- ⑥ Anyone who is alive implies not killed.
- ⑦ Anyone who is not killed implies alive.

Prove by resolution that - ⑧ John likes peanut.

prove by resolution that

- ①  $\forall x : \text{food}(x) \rightarrow \text{like}(\text{John}, x)$
- ②  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetable})$
- ③  $\forall x \forall y : \text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$
- ④  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
- ⑤  $\forall x : \text{eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Harry}, x)$
- ⑥  $\forall x : \neg \text{killed}(x) \rightarrow \text{alive}(x)$
- ⑦  $\forall x : \text{alive}(x) \rightarrow \neg \text{killed}(x)$
- ⑧  $\text{like}(\text{John}, \text{Peanuts})$

Rules      ①  $\alpha \Rightarrow \beta$       with       $\neg \alpha \vee \beta$

