

CS & IT ENGINEERING



Computer Network

Flow Control

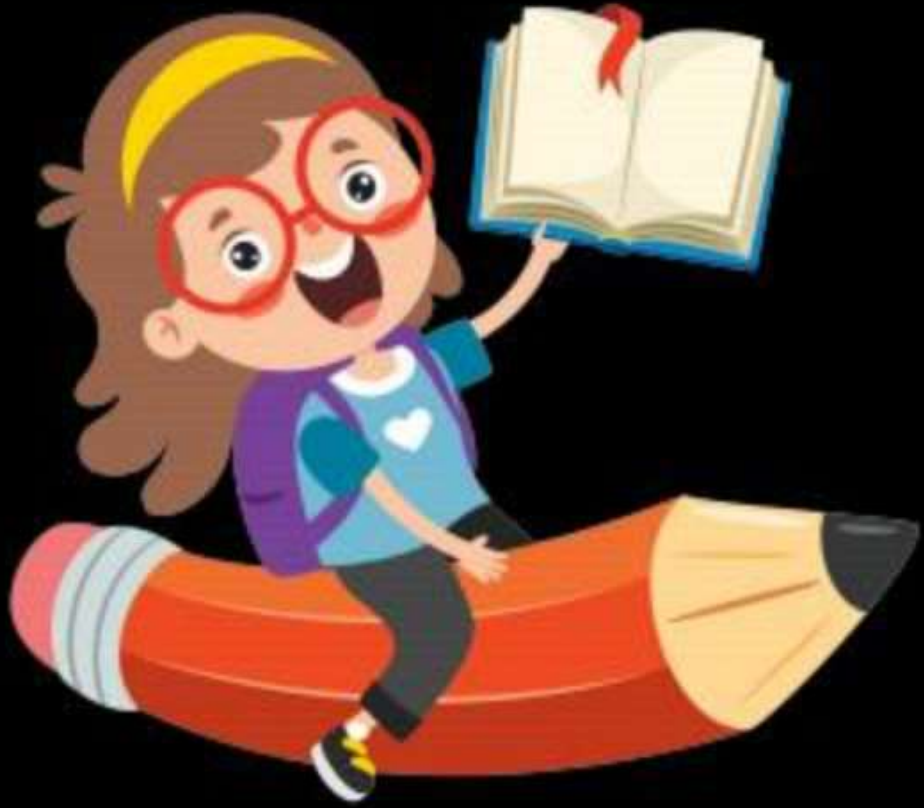
Lecture No. - 09



By - Abhishek Sir



Recap of Previous Lecture



Topic

Go Back N ARQ

Topic

Selective Repeat ARQ



Topics to be Covered



Topic

Selective Repeat ARQ



ABOUT ME



Hello, I'm **Abhishek**

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- 12 years of GATE CS teaching experience

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#Q. Station A needs to send a message consisting of 9 packets to Station B using a sliding window (window size 3) and go-back-n flow control strategy. All packets are ready and immediately available for transmission. If every 5th packet that A transmits gets lost (but no ACKs from B ever get lost), then what is the number of packets that A will transmit for sending the message to B?

[GATE 2006]

A 12

1 2 3 4 ⑤ 6 7 | 5 6 ⑦ 8 9
 ✓ ✓ ✓ ✓ discard ✓ ✓ discard

B 14

7 8 ⑨ | 9
 ✓ ✓ ✓

C 16

Ans: C

D 18

#Q. Consider a network connecting two systems located 8000 kilometers apart. The bandwidth of the network is 500×10^6 bits per second. The propagation speed of the media is 4×10^6 meters per second. It is needed to design a Go-Back-N sliding window protocol for this network. The average packet size is 10^7 bits. The network is to be used to its full capacity. Assume that processing delays at nodes are negligible. Then, the minimum size in bits of the sequence number field has to be _____.

[GATE 2015]

Solution:-

$$\text{Packet Size} = 10^7 \text{ bits}$$

$$\text{Bandwidth} = 500 * 10^6 \text{ bits / sec}$$

$$t_x = \frac{\text{Packet Size}}{\text{Bandwidth}} = \frac{10^7 \text{ bits}}{500 * 10^6 \text{ bits / sec}} = \frac{1}{50} \text{ sec}$$

$$\text{Distance} = 8000 \text{ Km} = 8 * 10^6 \text{ m}$$

$$\text{Signal Speed} = 4 * 10^6 \text{ m/s}$$

$$t_p = \frac{\text{Distance}}{\text{Signal Speed}} = \frac{8 * 10^6 \text{ m}}{4 * 10^6 \text{ m/s}} = 2 \text{ sec}$$

$$\text{Cycle Time} = (t_x + 2 * t_p) = \left(\frac{1}{50} + 2 * 2 \right) \text{ sec} = \left(\frac{201}{50} \right) \text{ sec}$$



$$\text{Optimal Window Size (N)} = \left\lceil \frac{\text{Cycle Time (RTT)}}{\text{Transmission delay}} \right\rceil = \left\lceil \frac{\frac{201}{50} \text{ sec}}{\frac{1}{50} \text{ sec}} \right\rceil = 201$$

For Go Back N ARQ : $N = 201$

$$\text{Total number of sequences} = (N + 1) = (201 + 1) = 202$$

Minimum number of bits required for sequence number field

$$= \lceil \log_2 [\text{Total number of sequences}] \rceil \text{ bits}$$
$$= \lceil \log_2(202) \rceil \text{ bits} = 8 \text{ bits}$$

$$\boxed{\text{Ans} = 8}$$

#Q. A 20 Kbps satellite link has a propagation delay of 400 ms. The transmitter employs the "go back n ARQ" scheme with n set to 10. Assuming that each frame is 100 bytes long, what is the maximum data rate possible?

Throughput

[GATE 2004]

(A) 5Kbps

✓ (B) 10Kbps

(C) 15Kbps

(D) 20Kbps

Ans: B

Solution:-

$$\underline{\text{Packet Size}} = \underline{100 \text{ bytes}} = \underline{8 * 10^2 \text{ bits}}$$

$$\underline{\text{Bandwidth}} = \underline{20 \text{ Kbps}} = \underline{2 * 10^4 \text{ bits / sec}}$$

$$t_x = \frac{\text{Packet Size}}{\text{Bandwidth}} = \frac{8 * 10^2 \text{ bits}}{2 * 10^4 \text{ bits / sec}} = \underline{40 \text{ ms}} = 40 * 10^{-3} \text{ sec}$$

$$t_p = 400 \text{ ms}$$

$$\begin{aligned} \text{Cycle time} &= (t_x + 2 * t_p) = \underline{840}^{\text{ms}} = 840 * 10^{-3} \text{ sec} \\ &= (40 + 2 * 400) \text{ ms} \end{aligned}$$

$$\underline{\text{Window Size}} = \underline{10}$$

$$\begin{aligned} \text{Throughput} &= \frac{\text{Window Size} * \text{Packet Size}}{\text{Cycle Time}} = \frac{10 * 8 * 10^2 \text{ bits}}{840 * 10^{-3} \text{ sec}} \\ &= \frac{8000}{840} * 10^3 \text{ bits/sec} \\ &= 9.52 \text{ Kbps} \end{aligned}$$

#Q. A 1Mbps satellite link connects two ground stations. The altitude of the satellite is 36,504 km and speed of the signal is 3×10^8 m/s. What should be the packet size for a channel utilization of 25% for a satellite link using go-back-127 sliding window protocol? Assume that the acknowledgment packets are negligible in size and that there are no errors during communication.

[GATE 2008]

11SC



Ans: A

- ✓ (A) 120 bytes
- (B) 60 bytes
- (C) 240 bytes
- (D) 90 bytes

Solution:-

$$\text{Packet Size} = ? \text{ (in bytes)}$$

$$\text{Bandwidth} = 1 \text{ Mbps} = 10^6 \text{ bits / sec}$$

$$\text{Distance} = 2 * 36504 \text{ Km} = 73008 * 10^3 \text{ m}$$

$$\text{Signal Speed} = 3 * 10^8 \text{ m/s}$$

$$t_p = \frac{\text{Distance}}{\text{Signal Speed}} = \frac{73008 * 10^3 \text{ m}}{3 * 10^8 \text{ m/s}} = 24336 * 10^{-5} \text{ Sec}$$

To achieve 25% utilization ($\eta = 1/4$) in Go Back 127 ARQ

$$N = 127$$

$$\text{Efficiency } (\eta) = \frac{N * \text{Transmission delay}}{\text{Cycle Time}}$$

$$\text{Cycle Time} = 4 * N * \text{Transmission delay}$$

$$(t_x + 2 * t_p) = 4 * 127 * t_x$$

$$t_x = 2 * t_p / 507$$

$$\begin{aligned} \text{Frame Size} &= (2 * t_p / 507) * \text{Bandwidth} \\ &= (2 * 24336 * 10^{-5} \text{ Sec} / 507) * 10^6 \text{ bits / sec} \\ &= \underline{960 \text{ bits}} = \underline{120 \text{ bytes}} \end{aligned}$$



Topic : Selective Repeat ARQ

→ Transmitter's transmitting window size = N

$(N > 1)$

→ Receiver's receiving window size = N

→ Total number of sequences = 2N [0 to (2N-1)]

0 (N-1)
N (2N-1)

Total number of sequences =

Transmitter's transmitting window size
+ Receiver's receiving window size

Sequence number \leftarrow (Frame number) mod (2N)



Topic : Selective Repeat ARQ



CASE I :

Suppose $N = 4$

Sequence Number = 0 to 7

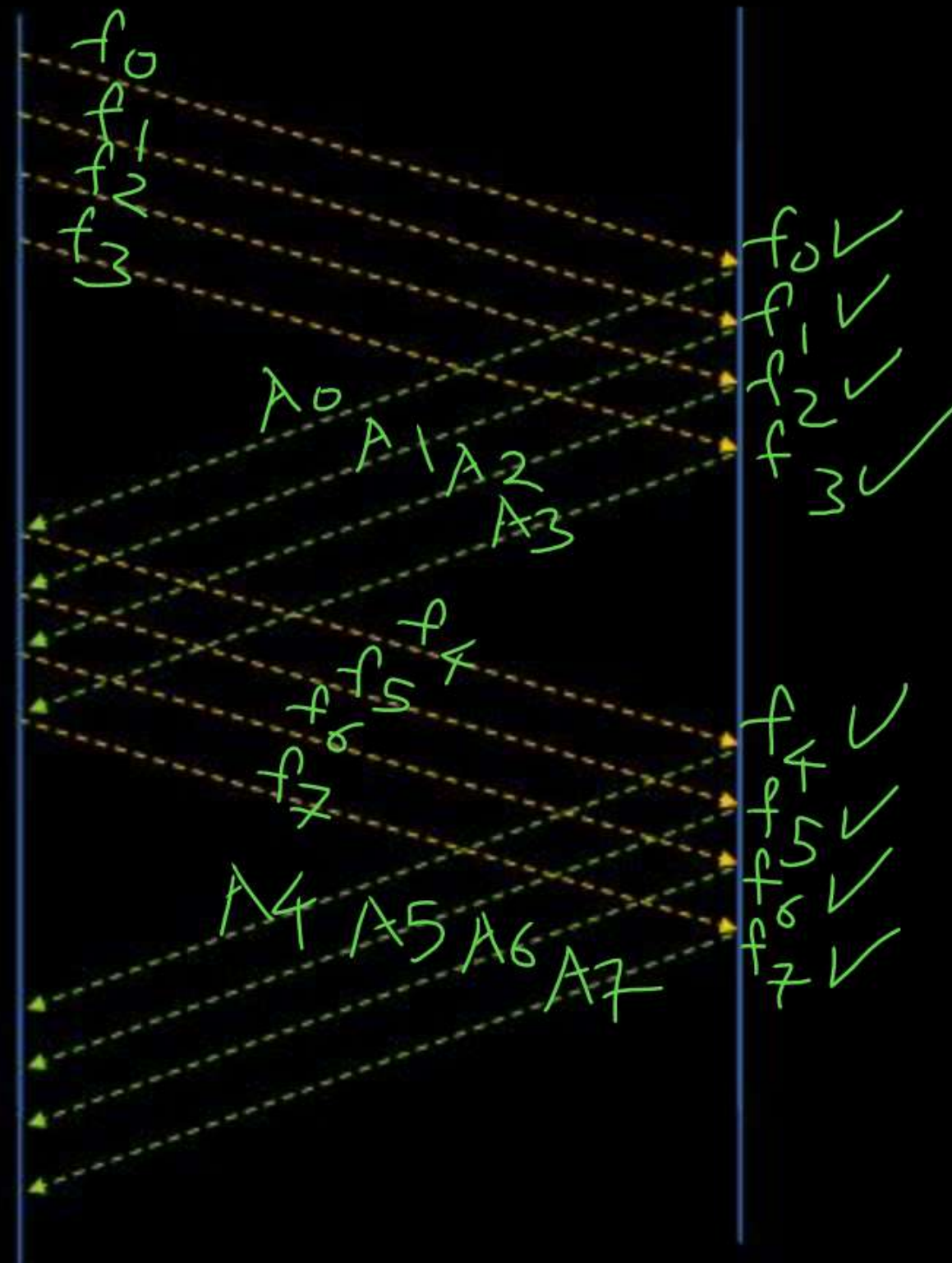
$F_0 F_1 F_2 F_3$
 $f_0 f_1 f_2 f_3$

$F_4 F_5 F_6 F_7$
 $f_4 f_5 f_6 f_7$

$F_8 F_9 F_{10} F_{11}$
 $f_0 f_1 f_2 f_3$

Transmitter

Receiver





Topic : Selective Repeat ARQ



Selective Repeat ARQ

CASE II :

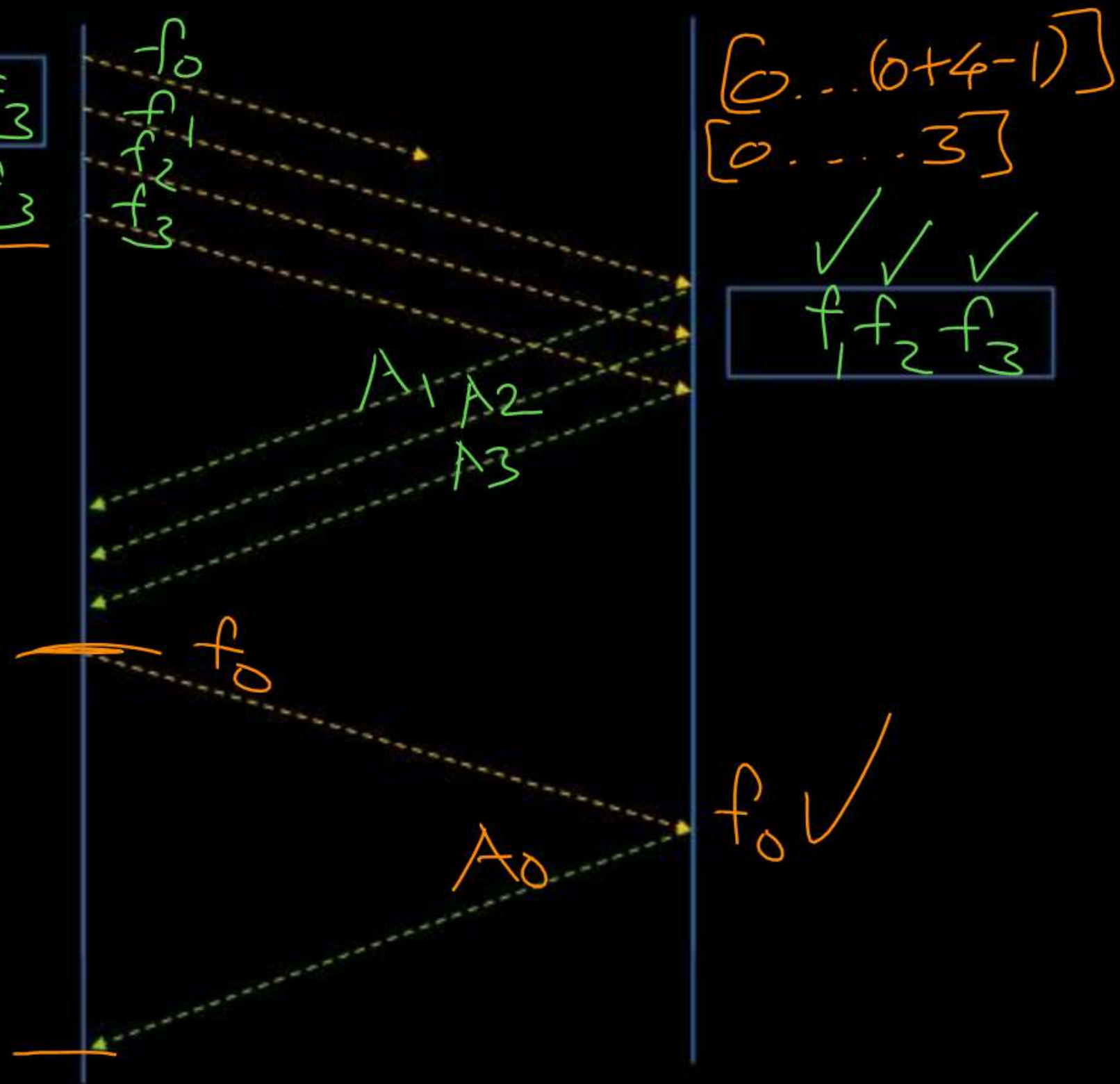
Suppose $N = 4$

Sequence Number = 0 to 7

$F_0 F_1 F_2 F_3$
 $f_0 f_1 f_2 f_3$

Transmitter

Receiver





Topic : Selective Repeat ARQ



CASE III :

Suppose $N = 4$

Sequence Number = 0 to 7

$F_0 F_1 F_2 F_3$
 $f_0 f_1 f_2 f_3$

T_0 f_0
 T_0 f_1
 T_0 f_2
 T_0 f_3

f_0
 f_1
 f_2
 f_3

A_0 A_1 A_2 A_3

Receiver

f_0 ✓
 f_1 ✓
 f_2 ✓
 f_3 ✓

$4-7$

f_0 (discard)
 f_1 - / / -
 f_2 - / / -
 f_3 - / / -

A_0 A_1 A_2 A_3



Topic : Selective Repeat ARQ



- ✓ → Transmitter transmit N frames without any acknowledgment
- ✓ → Receiver transmit "individual acknowledgment"
[for every successfully received frame]

→ "Cumulative (combine) acknowledgment" does not exist in this protocol



Topic : Selective Repeat ARQ



- Whenever transmitter gets time-out or received NACK, it retransmit that perticular frame only [mostly first frame, resides in transmitting window]
- Receiver buffer the frame which is out of order (expected sequence numbers) and send individual acknowledgment of that frame

Expected sequence no.
to $(\text{Expected seq no.} + N - 1)$

#Q. Consider a 128×10^3 bits/second satellite communication link with one-way propagation delay of 150 milliseconds. Selective retransmission (repeat) protocol is used on this link to send data with a frame size of 1 kilobyte. Neglect the transmission time of acknowledgment. The minimum number of bits required for the sequence number field to achieve 100% utilization is _____.

[GATE-2016, Set-2, 2-Mark]

11SC
H.W

#Q. Consider a selective repeat sliding window protocol that uses a frame size of 1 KB to send data on a 1.5 Mbps link with a one-way latency of 50 msec. To achieve a link utilization of 60%, the minimum number of bits required to represent the sequence number field is _____.

[GATE-2014, Set-1, 2-Mark]

IIT KGP
H.W.

#Q. In a sliding window ARQ scheme, the transmitter's window size is N and the receiver's window size is M . The minimum number of distinct sequence numbers required to ensure correct operation of the ARQ scheme is

[GATE 2004]

IIT-D

A $\min(M, N)$

B $\max(M, N)$

✓ **C** $(M + N)$

D MN

Ans: C

Solution :-

Transmitter's transmitting window size = N

Receiver's receiving window size = M

Total number of sequences = $(N + M)$

Total number of sequences =
Transmitter's transmitting window size
+ Receiver's receiving window size

Sliding Window ARQ
($M = N$)

No of seq. = N

Go Back N ARQ

$M = 1$

No. of seq. = $(N + M)$
= $(N + 1)$

Selective Repeat ARQ

$M = N$

No of seq. = $(N + M)$
= $2N$



Transmitter's transmitting window size = N

1. Sliding Window Protocol

Total number of sequences = N

2. Go Back N ARQ

Total number of sequences = $(N+1)$

3. Selective Repeat ARQ

Total number of sequences = $(N+N) = (2N)$

Minimum number of bits required for sequence number field

$$= \lceil \log_2(\text{Total number of sequences}) \rceil \text{ bits}$$

Number of bits in sequence number field = k

$$\text{Total number of sequences} = 2^k$$

Number of bits in sequence number field = k

1. Sliding Window Protocol

Transmitter's transmitting window size = 2^k

2. Go Back N ARQ

Transmitter's transmitting window size = $(2^k - 1)$

3. Selective Repeat ARQ

Transmitter's transmitting window size = $2^{(k-1)}$

$$= \binom{2^k}{2}$$

#Q. The maximum window size for data transmission using the selective reject protocol with n-bit frame sequence numbers is:

[GATE 2005]

11T-B

seq no. field \Rightarrow n bit
No of distinct seq. = 2^n

A 2^n

☒ **B** $2^{(n-1)}$

C $(2^n) - 1$

D $2^{(n-2)}$

max^m(sending) window size = $\left(\frac{2^n}{2}\right)$
 $= 2^{(n-1)}$

Ans: B



Topic : Bit Error Rate



=> Bit Error Rate (BER)

→ Number of bit errors per unit time

=> Bit Error Ratio or Bit Error Probability (P_b)

→ Probability that a bit is corrupted



Topic : Bit Error Rate



Suppose P_b = bit error probability

and Frame Length = L bits

What is the probability that a frame has received by receiver does not contain any error?

Answer : $(1 - P_b)^L$

$$(1 - P_b) * (1 - P_b) * \dots * (1 - P_b)$$

$$(1 - P_b)^L$$

#Q. In a communication network, a packet of length L bits takes link L1 with a probability of p_1 or link L2 with a probability of p_2 . Link L1 and L2 have bit error probability of b_1 and b_2 respectively. The probability that the packet will be received without error via either L1 or L2 is

[GATE 2005]

☒ **A** $(1 - b_1)^L p_1 + (1 - b_2)^L p_2$

☐ **B** $[1 - (b_1 + b_2)^L] p_1 p_2$

☐ **C** $(1 - b_1)^L (1 - b_2)^L p_1 p_2$

☐ **D** $1 - (b_1^L p_1 + b_2^L p_2)$

$$P_1 * (1 - b_1)^L + P_2 * (1 - b_2)^L$$

Ans: A



Topic : Bit Error Rate



Suppose P_b = bit error probability
and Frame Length = L bits

What is the probability that a frame has received by receiver contains some error(s)?

Answer : $1 - (1 - P_b)^L$



Topic : Packet Error Ratio

=> Packet Error Ratio or Packet Error Probability (P_p)

→ Probability that a packet ~~is corrupted~~ has corrupted bits

Suppose P_b = bit error probability

and Frame Length = L bits

$$\text{Packet error probability } (P_p) = 1 - (1 - P_b)^L$$

#Q. On a wireless link, the probability of packet error is 0.2. A stop-and-wait protocol is used to transfer data across the link. The channel condition is assumed to be independent from transmission to transmission. What is the average number of transmission attempts required to transfer 100 packets?

~~A~~ 100

☒ B 125

C 150

D 200

Ans: B

Packet Error Probability = $P = 0.2$ [GATE 2006]
No. of packets = $N = 100$

Total no of transmission attempts

$$= N + N * P + N * P^2 + N * P^3 + \dots$$

$$= N * [1 + P + P^2 + P^3 + \dots]$$

$$= N * \frac{1}{(1-P)} = \frac{N}{(1-P)} = \frac{100}{(1-0.2)} = \frac{100}{0.8} = 125$$



2 mins Summary



Topic

Selective Repeat ARQ

Packet Error Probability



THANK - YOU