

Week Number 1 problem N8

Find the domain of the function:

1)  $g(x) = 2\sqrt{x-4}$  assume that  $g(x)$  is  $y$   
So that  $y = 2\sqrt{x-4}$

$$y = 2\sqrt{x-4} \quad y \cdot \frac{1}{2} = \sqrt{x-4}$$

$$\left(\frac{y}{2}\right)^2 + 4 = x \quad \frac{y^2}{4} + 4 = x \quad \frac{y^2}{4} + \frac{16}{4} = x$$

$$\frac{y^2 + 16}{4} = x \quad \frac{y^2 + 4^2}{4} = x$$

2) assume that  $x = 1$

$$f(1) = 2\sqrt{1-4} = 2\sqrt{-3} \text{ Not.}$$

$$f(4) = 2\sqrt{4-4} = 2 \cdot 0 = 0.$$

$$f(6) = 2\sqrt{6-4} = 4$$

$$f(8) = 2\sqrt{8-4} = 2\sqrt{4} = 4$$

$$f(5) = 2\sqrt{5-4} = 2.$$

$$\sqrt{\quad}$$

$z$

$$z \geq 0$$
$$x \geq 0$$

$$z-4 \geq 0$$
$$x \geq 4$$

4 was taken as the  
smallest number  
value.

So it means the following  $D: [4, \infty)$   
 $R: [0, \infty)$ .

Week 1. problem 9.

$$h(x) = -2x^2 + 4x - 9 \quad \text{lets assume } x=2$$

$$h(2) = -2 \cdot (2)^2 + 4 \cdot 2 - 9 = -2(4) + 8 - 9 = -7$$

$$h(2) = -7$$

lets assume  $x=4$

$$h(4) = -2(4)^2 + 4 \cdot 4 - 9 = -32 + 16 - 9 = -25$$

$$h(4) = -25$$

only numbers could be written.  
so  $(-\infty; \infty)$ .

$$\text{the vertex is } -\frac{b}{2a}; f\left(-\frac{b}{2a}\right) \quad \begin{matrix} a=2 \\ b=4 \end{matrix}$$

$$\left(-\frac{4}{2 \cdot 2}; f\left(-\frac{4}{2 \cdot 2}\right)\right) \quad \begin{matrix} a=2 \\ b=4 \end{matrix} \quad \begin{matrix} \text{the vertex is } (-1; f(-1)) \\ \text{which is } (-1, 2 \cdot (-1)^2 - 9) \\ \text{or } (-1, -7); \end{matrix}$$

the range will be started at  $-7$ .

parabola opens ~~up~~ upward  $R: [-7, \infty)$ .

Week 1. problem 10.

$$x^2 - 2x - 15 \geq 1$$

$$x^2 - 2x \geq 1 + 15$$

$$x^2 - 2x \geq 16$$

$$x^2 - 2x - 15 = 0$$

$$(x-5)(x+3) = 0$$

$$x-5 = 0 \quad x=5$$

$$x+3 = 0 \quad x=-3$$

$$f(x) = x^2 - 2x - 15 \quad \text{the domain will be:}$$

$$(-\infty; -3) \cup (-3; -5) \cup (-5; \infty).$$



Week 1 problem 11.

$$f(x) = -2x + 1 \quad -1 \leq x < 0 \quad \text{points could be } (1, -1)$$

$$f(x) = x^2 + 2 \quad 1 \leq x < 3$$

$$f(x) = -2x + 1$$

$$x = 1$$

$$f(1) = -2 \cdot (-1) + 1 = -2 + 1 = -1$$

$$x = -1.$$

cannot be used.

then let's see next equation.

$$f(x) = x^2 + 2$$

$$x = 1$$

$$f(1) = 1^2 + 2 = 3.$$

$$x = 3$$

points could be  $(1, 3)$

let's count left side ( $x = -1$ ):  $f(-1) = 3$   $(-1, 3)$

let's count right side ( $x = 1$ ):  $f(1) = -2(0) + 1 = 1$ .  $(0)$

doesn't include 0.  $(0, 1)$

between two points it is possible to create line on the graph.

let's find points for the second function.

$$f(x) = x^2 + 2 \quad \text{where } 0 \leq x \leq 2.$$

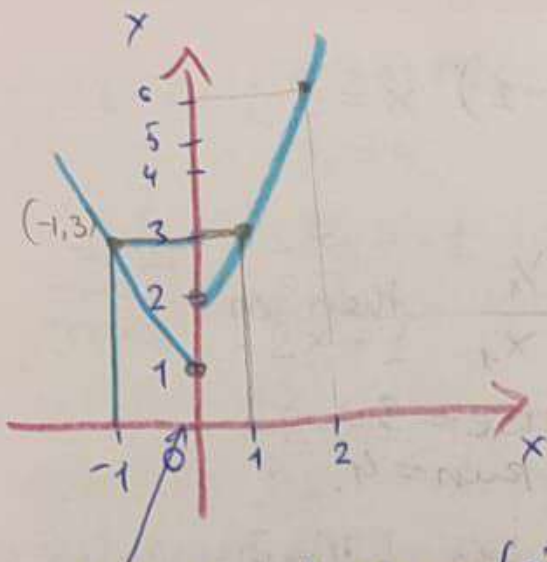
from  $x = 0$  to  $x = 2$ . (including).

let's count left side ( $x = 0$ ):  $f(0) = 0^2 + 2 = 2$   $(0, 2)$

let's count middle ( $x = 1$ ):  $f(1) = 1^2 + 2 = 3$   $(1, 3)$

let's count right side ( $x = 2$ ):  $f(2) = 2^2 + 2 = 6$   $(2, 6)$

let's create a graph:



$$2x+1 \quad [-1; 0]$$

$$x = -1 \quad y = 3 \quad (-1, 3)$$

$$x = 0 \quad y = 1 \quad (0, 1)$$

$$x^2+2 \quad [0, 2]$$

$$x = 0 \quad y = 2 \quad (0, 2)$$

$$x = 1 \quad y = 3 \quad (1, 3)$$

$$x = 2 \quad y = 6 \quad (2, 6)$$

here is not zero(0), but 0,5.

x	-1	-0,5	0	1	2
f(x)	3	2	2	3	6

$$x = -1; \quad f(-1) = -2 \cdot (-1) + 1 = 3$$

$$x = -0,5; \quad f(-0,5) = -2(-0,5) + 1 = 2$$

$$x = 0; \quad f(0) = 2$$

$$x = 1; \quad f(1) = 1^2 + 2 = 3$$

$$x = 2; \quad f(2) = 2^2 + 2 = 6$$

second function.

three points because of parabola.

Week 1 problem 12.

the slope of the line passes through the points  $(-1, 2)$  and  $(3, -4)$  point and graph will be following:

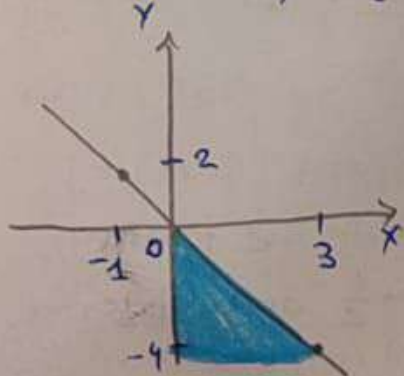
$$x_1 = -1; \quad y_1 = 2$$

$$x_2 = 3; \quad y_2 = -4$$

$$m(\text{slope}) = \frac{y_2 - y_1}{x_2 - x_1} = \frac{(-4) - 2}{3 - (-1)} = \frac{-6}{3 + 1} =$$

$$= -\frac{6}{4} = -\frac{3}{2}. \quad \text{the slope is } = -\frac{3}{2}.$$

$$\text{also range} = \frac{x_1}{y_1}; \quad \frac{x_2}{y_2}.$$





# Week 1, problem 13

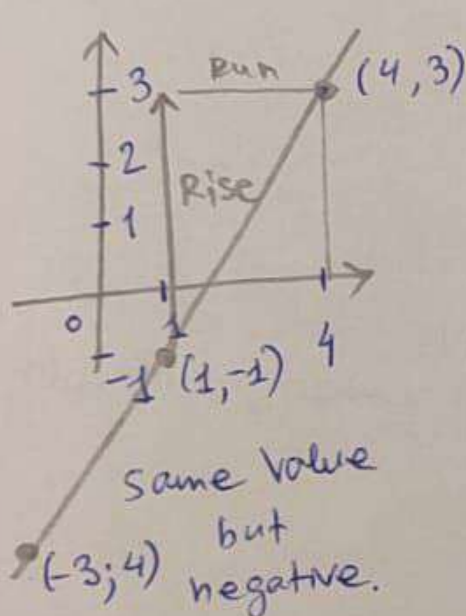
the line is passing the point  $(1, -1)$   $x=1$ ;  $y=-1$ .  
whose slope is  $m = \frac{3}{4}$ ;

if we have formula  $m = \frac{y_2 - y_1}{x_2 - x_1}$  then  $m = \frac{\text{Rise}}{\text{Run}}$ ,

so  $m = \frac{3}{4}$  equals  $\frac{\text{Rise}}{\text{Run}} = \frac{3}{4}$  or  $\text{Rise} = 3$   
 $\text{Run} = 4$ .

also it could be negative with the following value:

$y = -3$   $\text{Rise} = -3$   
 $x = -4$   $\text{Run} = -4$  } we can consider this as a  
third point.



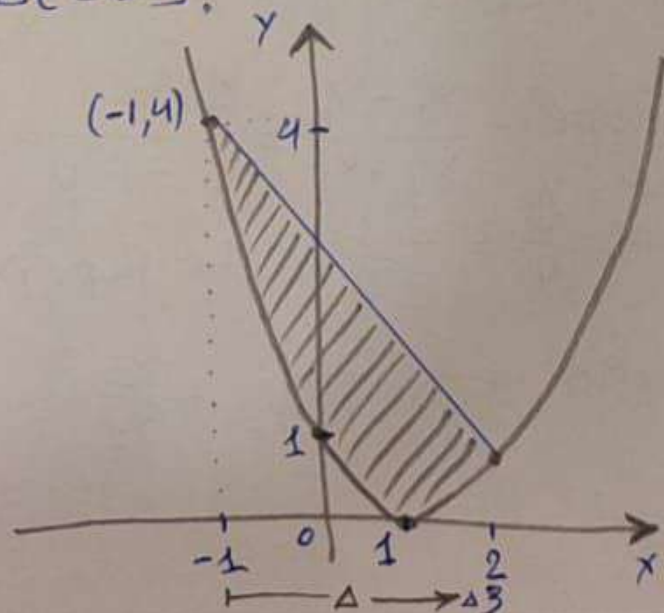
## problem 14

find average rate of change on the  
interval function  $g(t)$

$$\begin{aligned} x_1 &= -1 & \text{if } t &= -1 \\ x_2 &= 2 & g(t) &= g(-1) = 4 \\ & & t=2 & g(2) = 1. \end{aligned}$$

So the point on the parabola will be  
 $(-1, 4)$  and  $(2, 1)$  shown in  $g(t)$

and the horizontal change  $\Delta t = 3$ . vertical and  
also  $\Delta t = -3$ .



$$\begin{aligned} \text{the average rate of} \\ \text{change} &= \frac{f(4) - f(2)}{4 - 2} = \\ &= \frac{\frac{31}{2} - \frac{7}{2}}{2}; \text{ let's simplify:} \end{aligned}$$

$= \frac{12}{2} = 6$ . So this is an  
average speed (Rate) of  
change with the function.  
to  $f(x) = x^2 - \frac{1}{2}$  on the interval  
( $x=2$   $x=4$ ) or  $(2, 3, 5)$  and  $(4, 15, 9)$

Week 1 Problem 14.

continue.

$$y_2 = 1 \quad y_1 = 4$$

$$y_1 = 2 \quad x_1 = -1$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 4}{2 - (-1)} = \frac{-3}{3} = -1.$$

Problem 15.

Complete the average rate of  $f(x) = x^2 - \frac{1}{x}$  on the interval  $[2, 4]$ . the average rate of change is

$$\text{equals } ARC = \frac{f(b) - f(a)}{b - a}$$

$[a, b]$  is an interval, then  $f(x) = x^2 - \frac{1}{x}$   $[2, 4]$ .

$$a = 2 \quad b = 4$$

$$f(x) = x^2 - \frac{1}{x} \quad [2, 4] \quad f(x) = f(2) = 2^2 - \frac{1}{2} = 4 - \frac{1}{2} = \frac{8 - 1}{2} = \frac{7}{2}$$

$$\cancel{f(4) = 4^2 - \frac{1}{2} = 16 - \frac{1}{2} = \frac{32}{2} - \frac{1}{2} = \frac{31}{2}}$$

~~Problem 15.~~

$$f(x) = x^2 - \frac{1}{x} \quad \begin{matrix} x = 2 \\ x = 4 \end{matrix} \quad \text{Range.}$$

$$\cancel{f(2) = 2^2 - \frac{1}{2}} \quad f(4) = 4^2 - \frac{1}{2} = 16 - \frac{1}{2} = \frac{63}{2}$$

$$ARC = \frac{f(4) - f(2)}{4 - 2} = \frac{\frac{63}{2} - \frac{7}{2}}{4 - 2} = \frac{\frac{49}{2}}{2} = \frac{49}{4}$$

Problem 16.

we need to evaluate  $f(h(1))$

$$f(t) = t^2 - t \quad h(x) = 3x + 2 \quad x = 1$$

$$h(1) = 1 \cdot 3 + 2 = 5 \quad h(1) = 5.$$

$$f(h(1)) = 5^2 - 5 = 25 - 5 = 20.$$

$$f(h(1)) = 20.$$



Problem 17. Week 1

$$(g-f)(x) = g(x) - f(x) \quad \text{so} \quad \left(\frac{g}{f}\right)(x) = \frac{g(x)}{f(x)}$$

$$f(x) = x-1 \quad x^2-1 - (x-1) = x^2-x = x(x-1)$$

$$g(x) = x^2-1 \quad (g-f)(x) = x(x-1)$$

$$\frac{g(x)}{f(x)} = \frac{x^2-1}{x-1} = \frac{x+1}{1} = x+1.$$

$$x+1 \neq x(x-1) \quad \text{No the same :)}$$

it also necessary that we should have  $x \neq 1$ , because  
the denominator must be not  $x=0$ .