QUANTITATIVE RISK MANAGEMENT IN PYTHON

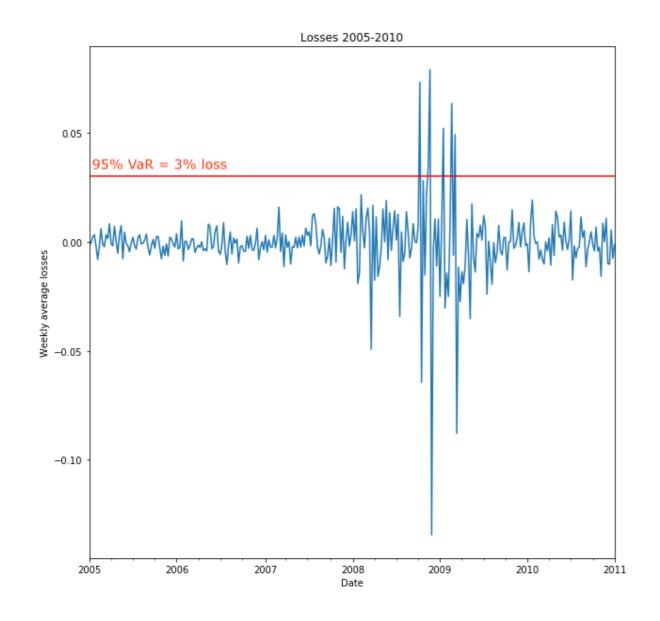


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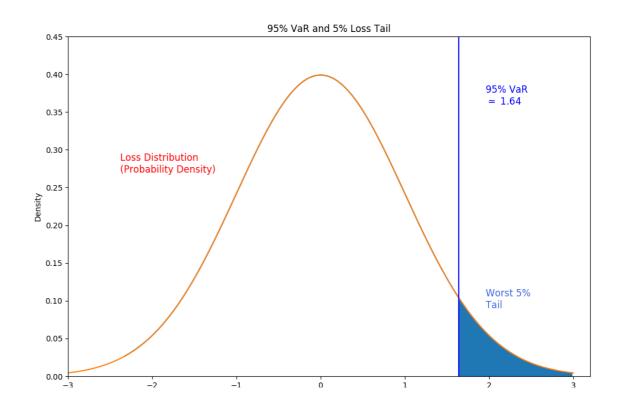


#### Extreme values

Portfolio losses: extreme values

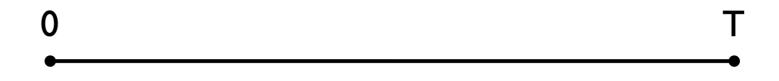


- Extreme values: from tail of distribution
  - Tail losses: losses exceeding some value
  - Model tail losses => better risk
     management

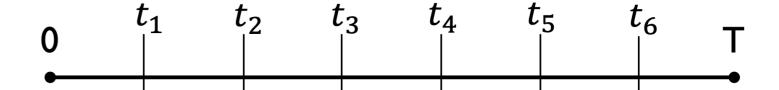


• Extreme value theory: statistical distribution of extreme values

Block maxima



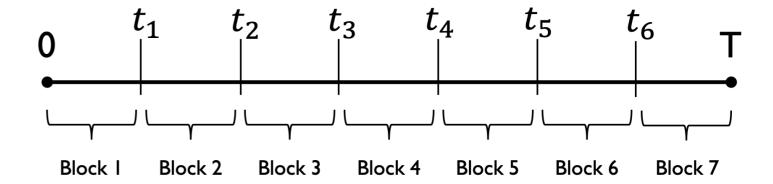
• Extreme value theory: statistical distribution of extreme values



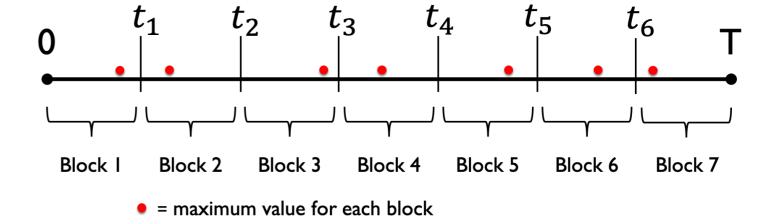
- Block maxima:
  - Break period into sub-periods



- Extreme value theory: statistical distribution of extreme values
- Block maxima:
  - Break period into sub-periods
  - Form block from each sub-period



- Extreme value theory: statistical distribution of extreme values
- Block maxima:
  - Break period into sub-periods
  - Form blocks from each sub-period
  - Set of block maxima = dataset
- Peak over threshold (POT):
  - Find all losses over given level
  - Set of such losses = dataset



#### **Generalized Extreme Value Distribution**

- Example: Block maxima for 2007 2009
  - Resample losses with desired period (e.g. weekly)

```
maxima = losses.resample("W").max()
```

- Generalized Extreme Value Distribution (GEV)
  - Distribution of maxima of data
  - Example: parametric estimation using scipy.stats.genextreme

```
from scipy.stats import genextreme
params = genextreme.fit(maxima)
```

#### VaR and CVaR from GEV distribution

- 99% VaR from GEV distribution
  - Use .ppf() percent point function to find 99% VaR
  - Requires params from fitted GEV distribution
  - Finds maximum loss over one week period at 99% confidence
- 99% CVaR from GEV distribution
  - CVaR is conditional expectation of loss given VaR as minimum loss
  - Use .expect() method to find expected value

```
VaR_99 = genextreme.ppf(0.99, *params)
```

```
CVar_{99} = (1 / (1 - 0.99)) * genextreme.expect(lambda x: x, *params, lb = VaR_{99})
```

# Covering losses

- Risk management: covering losses
  - Regulatory requirement (banks, insurance)
  - Reserves must be available to cover losses
    - For a specified period (e.g. one week)
    - At a specified confidence level (e.g. 99%)
- VaR from GEV distribution:
  - estimates maximum loss
    - given period
    - given confidence level

#### Covering losses

- **Example**: Initial portfolio value = \$1,000,000
- One week reserve requirement at 99% confidence
  - $\circ$  Va $R_{99}$  from GEV distribution: maximum loss over one week at 99% confidence
- Reserve requirement: Portfolio value x  $VaR_{99}$ 
  - $\circ$  Suppose  $VaR_{99}$  = 0.10, i.e. 10% maximum loss
  - Reserve requirement = \$100,000
- Portfolio value changes => reserve requirement changes
- Regulation sets frequency of reserve requirement updating

# Let's practice!

QUANTITATIVE RISK MANAGEMENT IN PYTHON



# Kernel density estimation

QUANTITATIVE RISK MANAGEMENT IN PYTHON

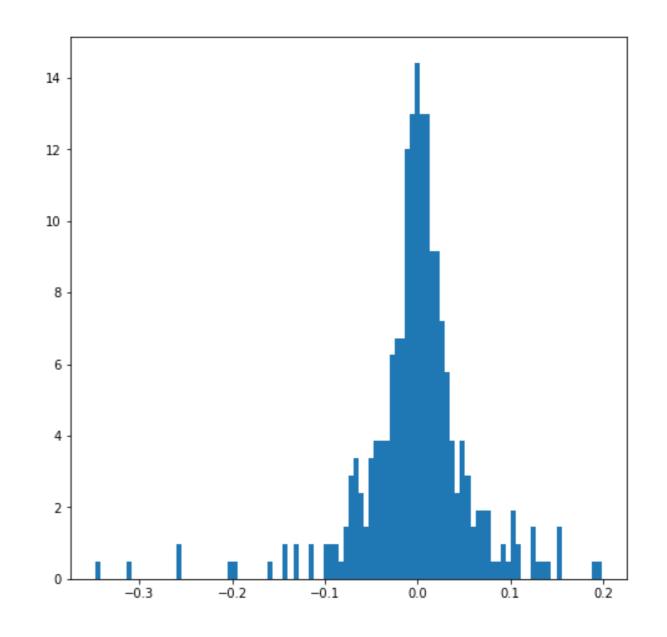


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# The histogram revisited

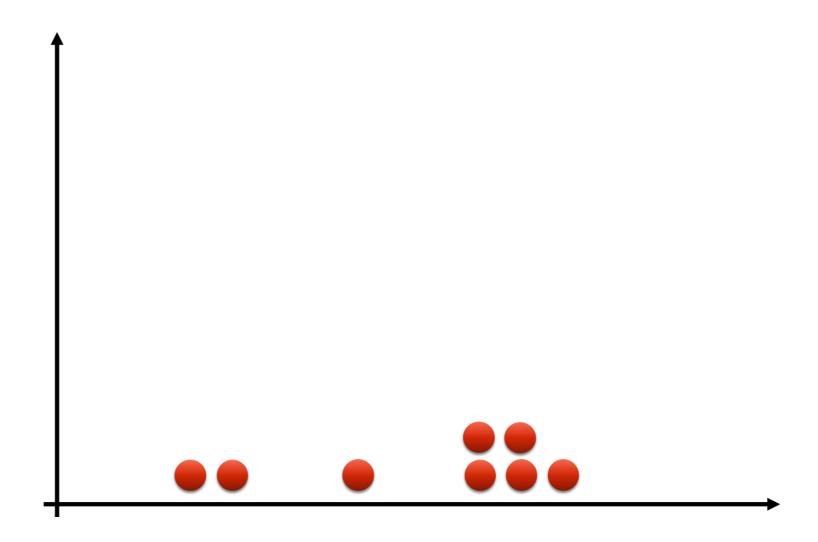
- Risk factor distributions
  - Assumed (e.g. Normal, T, etc.)
  - Fitted (parametric estimation, Monte Carlo simulation)
  - Ignored (historical simulation)
- Actual data: histogram
- How to represent histogram by probability distribution?
  - Smooth data using filtering
  - Non-parametric estimation



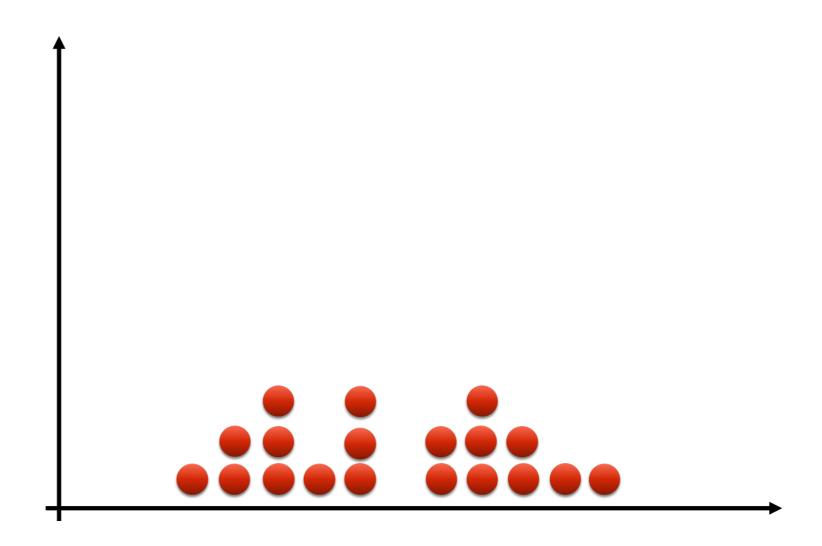
• Filter: smoothen out 'bumps' of histogram



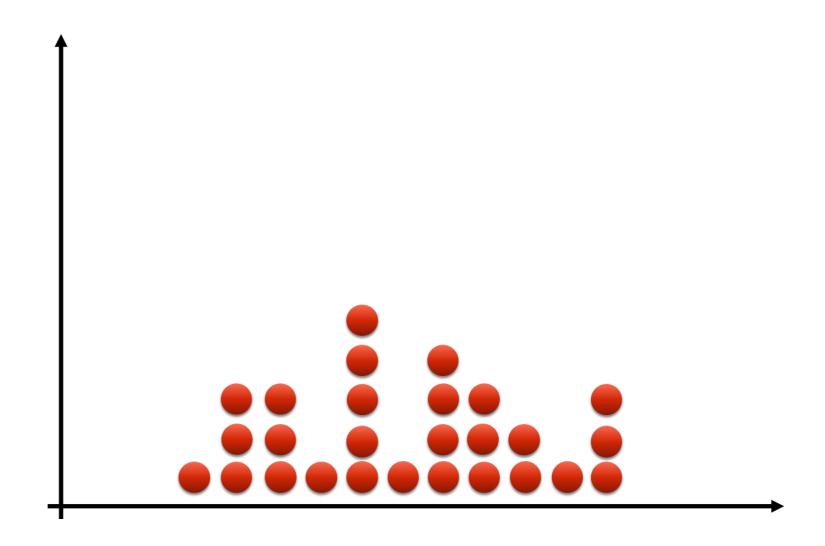
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time



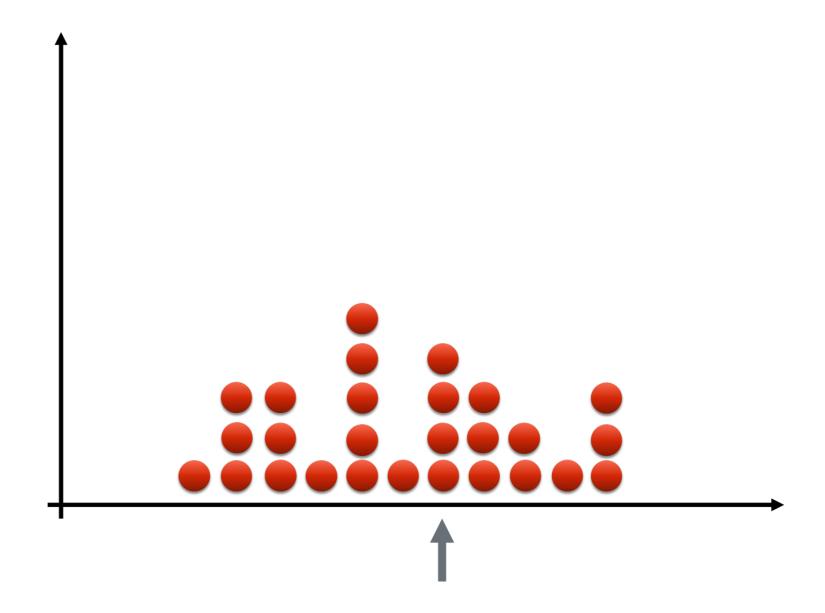
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time



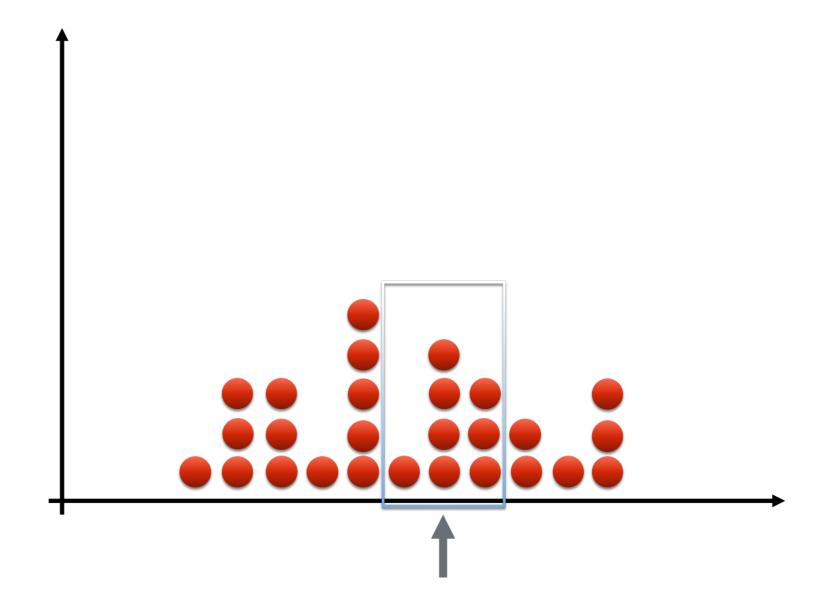
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time



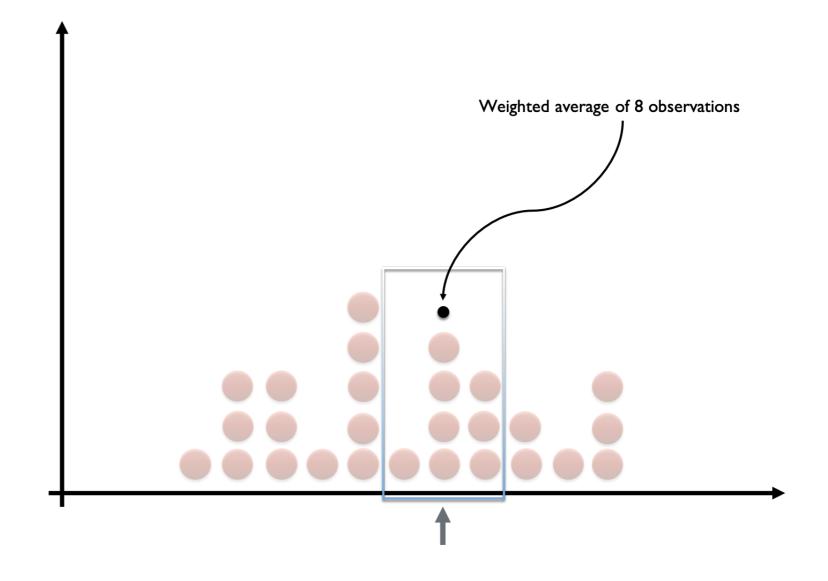
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time
- Pick particular portfolio loss



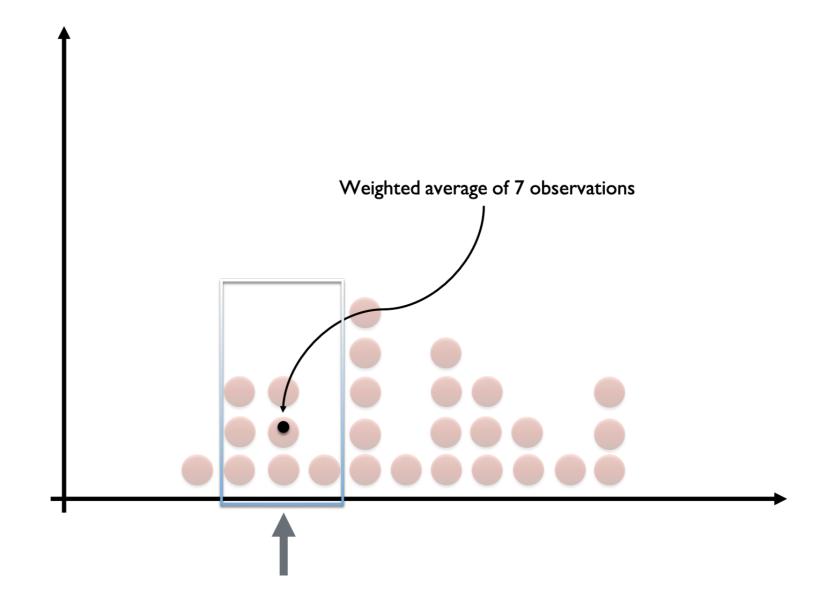
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time
- Pick particular portfolio loss
  - Examine nearby losses



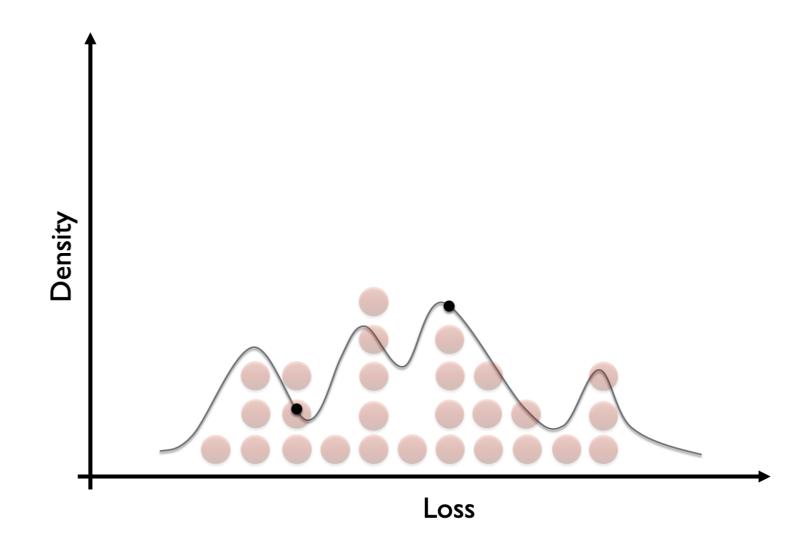
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time
- Pick particular portfolio loss
  - Examine nearby losses
  - Form "weighted average" of losses
- Kernel: filter choice; determines "window"



- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time
- Pick particular portfolio loss
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  - Form "weighted average" of losses
- Kernel: filter choice; determines "window"
  - Move window to another loss

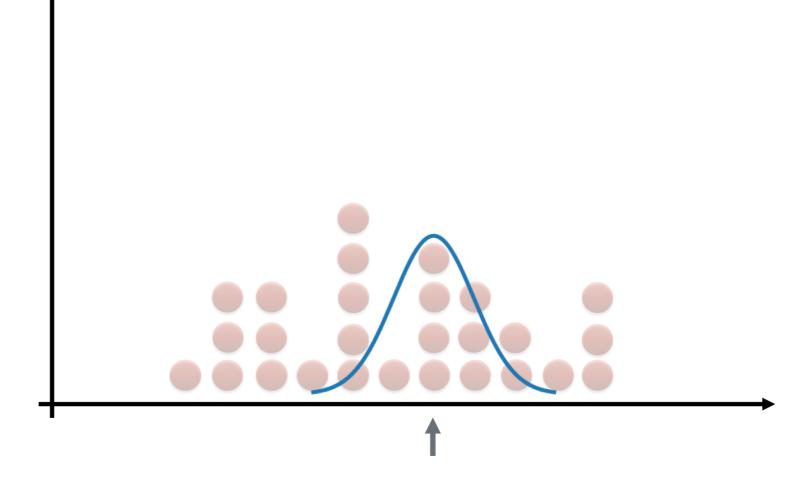


- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time
- Pick particular portfolio loss
  - Examine nearby losses
  - Form "weighted average" of losses
- Kernel: filter choice; determines "window"
  - Move window to another loss
- Kernel density estimate: probability density



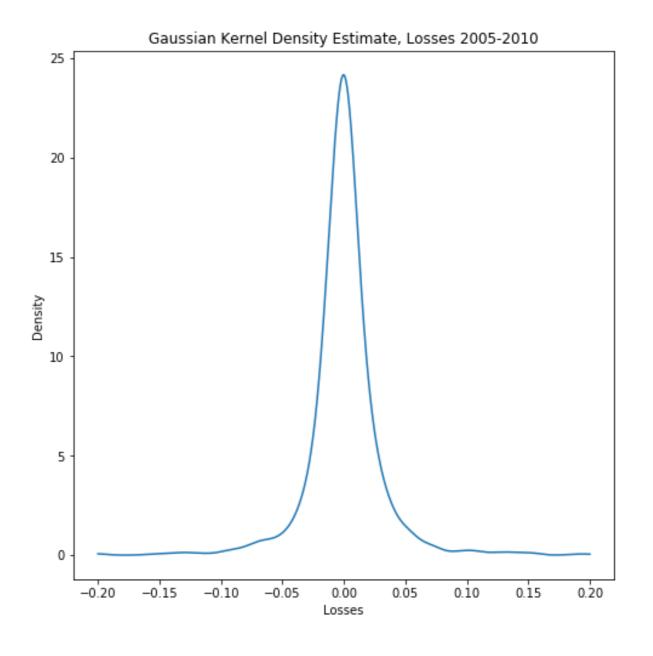
#### The Gaussian kernel

- Continuous kernel
- Weights all observations by distance from center
- **Generally**: many different kernels are available
  - Used in time series analysis
  - Used in signal processing



# **KDE in Python**

• Visualization: probability density function from KDE fit



# Finding VaR using KDE

- VaR: use gaussian\_kde .resample() method
- Find quantile of resulting sample
- CVaR: expected value as previously encountered, but
  - o gaussian\_kde has no .expect() method => compute integral manually
  - special .expect() method written for exercise

```
sample = kde.resample(size = 1000)
VaR_99 = np.quantile(sample, 0.99)
print("VaR_99 from KDE: ", VaR_99)
```

```
VaR_99 from KDE: 0.08796423698448601
```

# Let's practice!

QUANTITATIVE RISK MANAGEMENT IN PYTHON



# Neural network risk management

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# Real-time portfolio updating

- Risk management
  - Defined risk measures (VaR, CVaR)
  - Estimated risk measures (parameteric, historical, Monte Carlo)
  - Optimized portfolio (e.g. Modern Portfolio Theory)
- New market information => update portfolio weights
  - Problem: portfolio optimization costly
  - $\circ$  Solution: weights  $= f( ext{prices})$
  - $\circ$  Evaluate f in real-time
  - $\circ$  Update f only occasionally

#### Neural networks

- Neural Network: output = f(input)
  - Neuron: interconnected processing node in function
- Initially developed 1940s-1950s
- Early 2000s: application of neural networks to "big data"
  - Image recognition, processing
  - Financial data
  - Search engine data
- Deep Learning: neural networks as part of Machine Learning
  - 2015: Google releases open-source Tensorflow deep learning library for Python

- Layers: connected processing neurons
  - Input layer

Layers

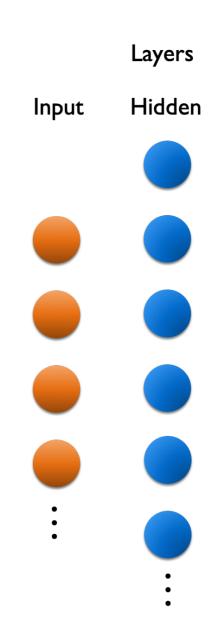




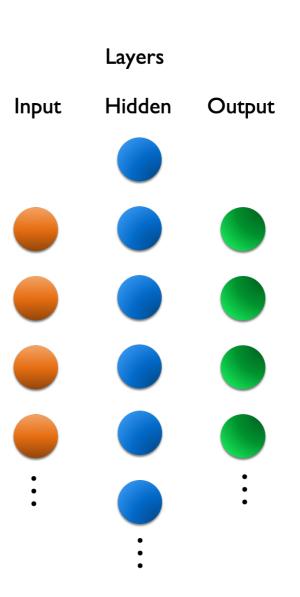




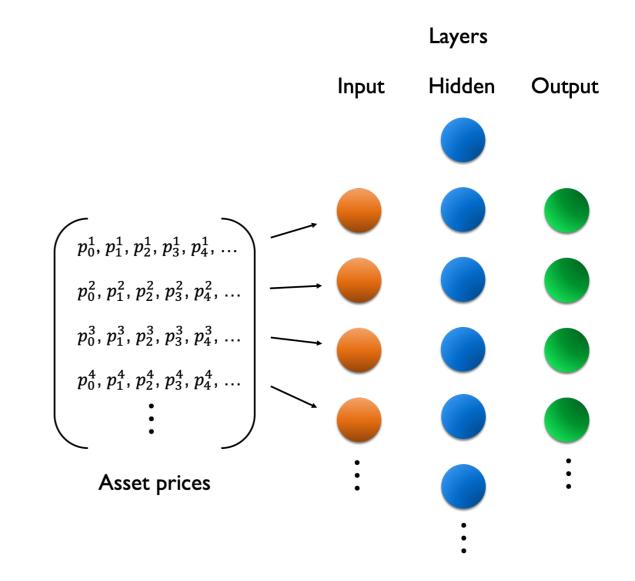
- Neural network structure
  - Input layer
  - Hidden layer



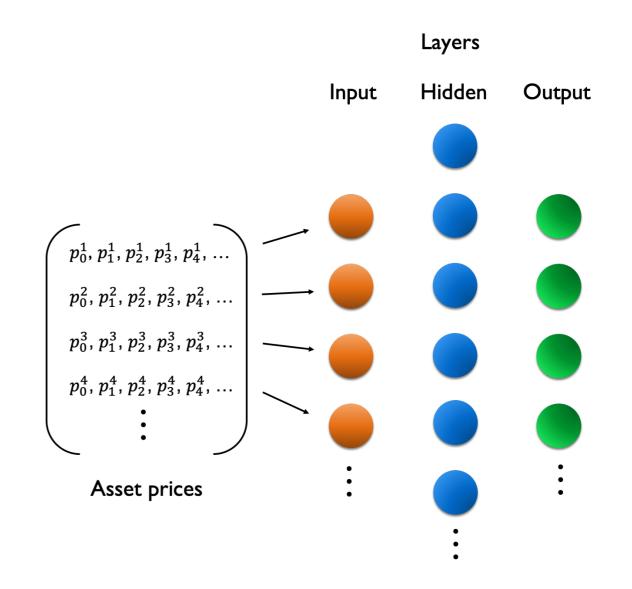
- Neural network structure
  - Input layer
  - Hidden layer
  - Output layer
- **Training**: learn relationship between input and output



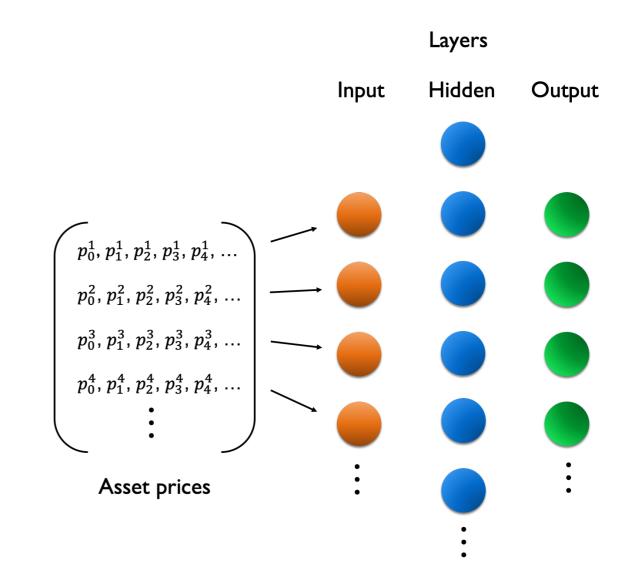
- Neural network structure
  - Input layer
  - Hidden layer
  - Output layer
- Training: learn relationship between input and output
  - Asset prices => Input layer



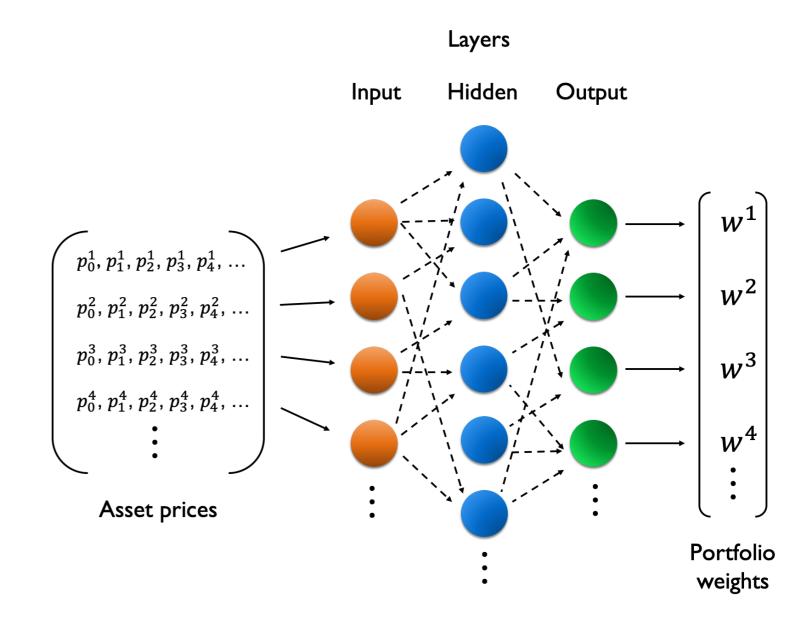
- Neural network structure
  - Input layer
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  - Output layer
- Training: learn relationship between input and output
  - Asset prices => Input layer
  - Input + hidden layer processing



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- Neural network structure
  - Input layer
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  - Output layer
- Training: learn relationship between input and output
  - Asset prices => Input layer
  - Input + hidden layer processing
  - Hidden + output layer processing
  - Output => portfolio weights



#### Using neural networks for portfolio optimization

#### Training

- Compare output and pre-existing "best" portfolio weights
- Goal: minimize "error" between output and weights
- Small error => network is trained

#### Usage

- Input: new, unseen asset prices
- Output: predicted "best" portfolio weights for new asset prices
- Best weights = risk management

### Creating neural networks in Python

- Keras: high-level Python library for neural networks/deep learning
- Further info: Introduction to Deep Learning with Keras

```
from keras.models import Sequential

from keras.layers import Dense

model = Sequential()

model.add(Dense(10, input_dim=4, activation='sigmoid'))

model.add(Dense(4))
```

#### Training the network in Python

- Historical asset prices: training\_input matrix
- Historical portfolio weights: training\_output vector
- Compile model with:
  - given error minimization ('loss')
  - given optimization algorithm ('optimizer')
- Fit model to training data
  - epochs: number of training loops to update internal parameters

```
model.compile(loss='mean_squared_error', optimizer='rmsprop')
model.fit(training_input, training_output, epochs=100)
```

### Risk management in Python

- Usage: provide new (e.g. real-time) asset pricing data
  - New vector new\_asset\_prices given to input layer
- Evaluate network using model.predict() on new prices
  - Result: predicted portfolio weights
- Accumulate enough data over time => re-train network
  - Test network on previous data => backtesting

```
# new asset prices are in the vector new_asset_prices
predicted = model.predict(new_asset_prices)
```



## Let's practice!

QUANTITATIVE RISK MANAGEMENT IN PYTHON



# Wrap-up and Future Steps

QUANTITATIVE RISK MANAGEMENT IN PYTHON



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Chapter I

Risk and Return Recap

**Return Distribution** 

**Risk Factors** 

Volatility & Covariance

Modern Portfolio Theory

Efficient Portfolio & Efficient Frontier



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**Extreme Value Theory** 

Kernel Density Estimation

**Neural Networks** 

Real-time risk management

### Tools in your toolkit

Scipy	Statsmodels	PyPortfolioOpt	Keras
scipy.stats	statsmodels.api	pypfopt	keras
norm()	OLS()	risk_models	models
skewnorm()	add_constant()	cla	layers
t()	.fit()	expected_returns	Sequential()
genextreme()		efficient_frontier	Dense()
<pre>gaussian_kde()</pre>		objective_functions	.add()
anderson()		EfficientFrontier()	.fit()
skewtest()		<pre>mean_historical_return()</pre>	.predict()
.pdf()		CovarianceShrinkage()	
.ppf()		<pre>.negative_cvar()</pre>	
.fit()		.CLA()	
.rvs()		<pre>.ledoit_wolf()</pre>	

#### Future steps and reference

- Upcoming DataCamp courses
  - Credit Risk Modeling in Python
  - Financial Forecasting in Python
  - Machine Learning for Finance in Python
  - GARCH Models for Finance in Python
- Quantitative Risk Management: Concepts, Techniques and Tools, McNeil, Frey & Embrechts, Princeton UP, 2015.

# Best of luck on your data science journey!

QUANTITATIVE RISK MANAGEMENT IN PYTHON

