## ex3

## January 10, 2023

[]: # Create a Toy dataset

```
[]: !pip install scikit-learn
    Collecting scikit-learn
      Downloading
    scikit_learn-1.2.0-cp39-cp39-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (9.5
                                9.5/9.5 MB
    1.4 MB/s eta 0:00:0000:0100:010m
    Collecting joblib>=1.1.1
      Using cached joblib-1.2.0-py3-none-any.whl (297 kB)
    Requirement already satisfied: scipy>=1.3.2 in
    /home/pranav/miniconda3/envs/gal/lib/python3.9/site-packages (from scikit-learn)
    (1.9.3)
    Requirement already satisfied: numpy>=1.17.3 in
    /home/pranav/miniconda3/envs/gal/lib/python3.9/site-packages (from scikit-learn)
    (1.24.1)
    Collecting threadpoolctl>=2.0.0
      Using cached threadpoolctl-3.1.0-py3-none-any.whl (14 kB)
    Installing collected packages: threadpoolctl, joblib, scikit-learn
    Successfully installed joblib-1.2.0 scikit-learn-1.2.0 threadpoolctl-3.1.0
[]: import numpy as np
     from scipy import sparse
     from sklearn.neighbors import kneighbors_graph
     from sklearn.cluster import KMeans
     from sklearn.metrics import adjusted_rand_score, homogeneity_score,_
      ⇔completeness_score, v_measure_score
     import networkx as nx
     # import make moons
     from sklearn.datasets import make_moons
[]: import matplotlib.pyplot as plt
     random_state = 213
     np.random.seed(random state)
     data_size = 150
```

```
features,y = make_moons(n_samples=data_size, noise=0.07, random_state=213)
[]: n_neighbors = 10
     knn_dist_graph = kneighbors_graph(X=features,
     n_neighbors=n_neighbors,
     mode='distance',
     metric='euclidean',
     n_jobs=6
[]: sigma = 1
[]: similarity_graph = sparse.csr_matrix(knn_dist_graph.shape)
     nonzeroindices = knn_dist_graph.nonzero()
     similarity_graph[nonzeroindices] = np.exp( -np.
     →asarray(knn_dist_graph[nonzeroindices])**2 / 2.0 * sigma**2)
     similarity_graph = 0.5 * (similarity_graph + similarity_graph.T)
     similarity graph.todense()[0]
    /home/pranav/miniconda3/envs/gal/lib/python3.9/site-
    packages/scipy/sparse/_index.py:146: SparseEfficiencyWarning: Changing the
    sparsity structure of a csr_matrix is expensive. lil_matrix is more efficient.
      self._set_arrayXarray(i, j, x)
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[]: degree_matrix = similarity_graph.sum(axis=1)
     diagonal_matrix =np.diag(np.asarray(degree_matrix).reshape(data_size,))
     L = diagonal_matrix - similarity_graph
[]: L
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[]: matrix([[ 9.88985997,
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[]:
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