

## Principles of Compiler Design

\* Compiler is an intermediate which is used to convert a high level language into low level language (or) machine understandable code (i.e., 0's and 1's).

### Translators:

1) Compiler:



2) Assembler:

Pseudocode is converted to low level language.

3) Interpreter:

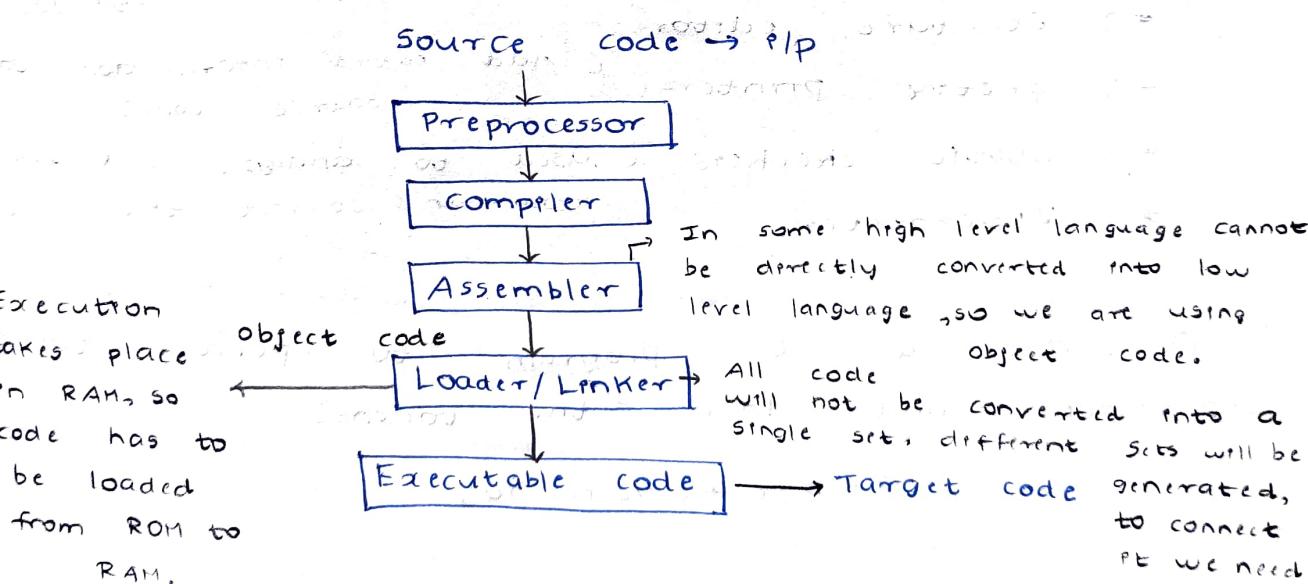
( $c = a + b$ ,  $\rightarrow$  ADD a,b) generates target language.

Compiler → converts into object code → generates an executable code. It also leads to additional memory.

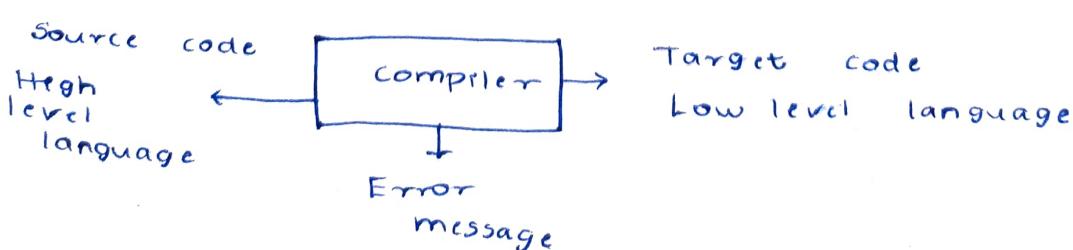
Interpreter → will not create a object code (or) generates an executable code. It does not require an additional memory.

Language Processing System:

~~Processor~~ ~~and other components:~~



### Model of compiler:

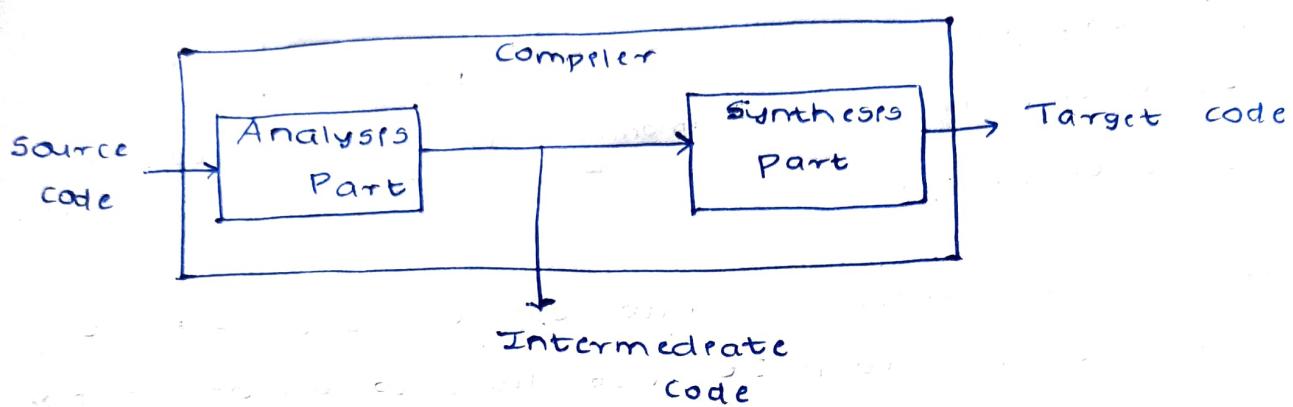


# Process of compilation:

\*.) Analysis Part.

\*) Synthesis Part.

source program is read down into small segments called tokens in analysis part.



Token → identifiers, Keywords, Operators, separators, constants.

Tools for manipulating source program and analyze the code:  
(uses command to build source program)

\*) Structure editor.

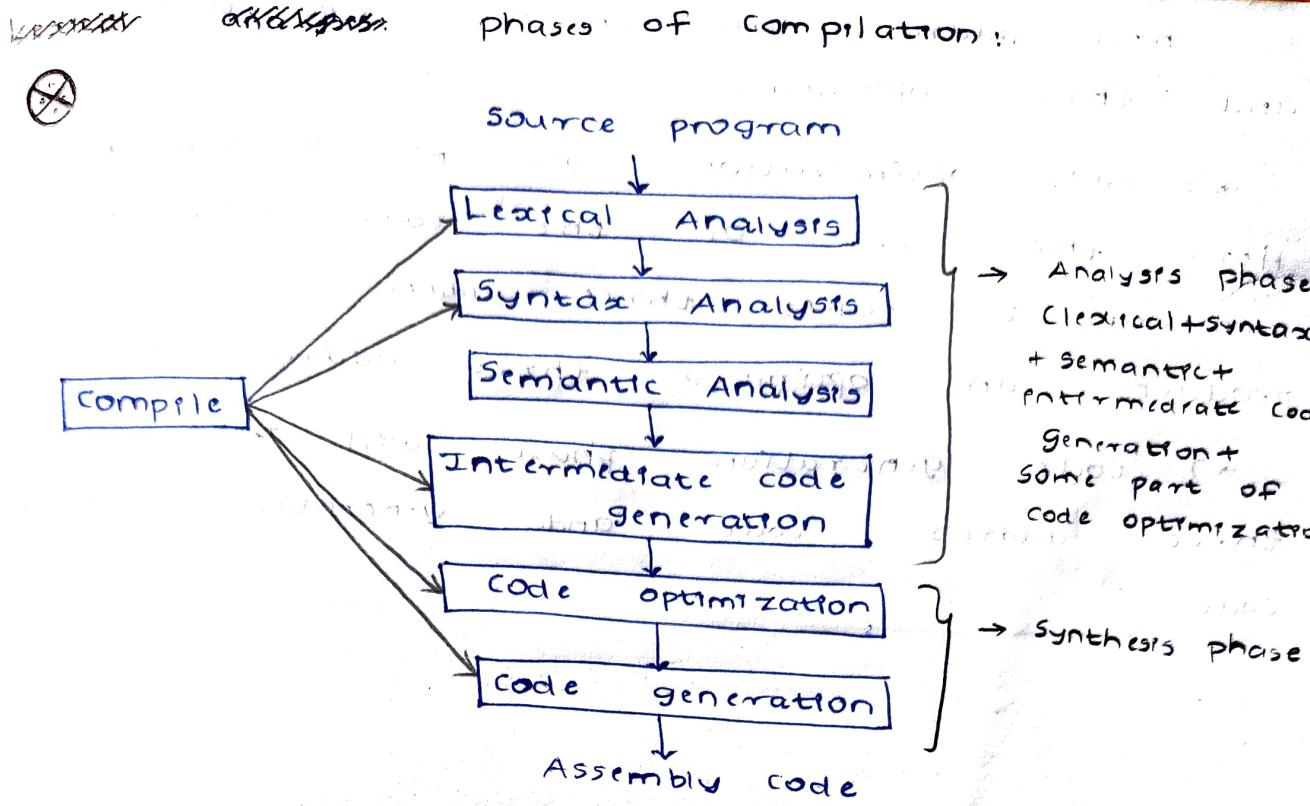
\*) pretty printers. (Add extra information to source code)

\*) static checkers. (Used to analyze and find errors & correct the code)

\*) Interpreter.

1) Write a C program to perform token separation and label the tokens?

$x = a + b / c * e \% h - 50;$



Compile will mainly have two phases (i) Analysis phase (ii) synthesis. There are other details datatype of variable, memory allocated.

(i) Symbol Table  
+ contains  
details datatype of variable, memory  
+  
used in lexical analysis  
→ token generation phase

\*.) Lexical analysis phase generates a set of tokens (Keywords, identifiers, constants, operators, delimiters). Once tokens are generated, then it'll be moved to next stage. → skipping of whitespaces, newlines.

\*.) Syntax analysis collects the tokens generated in the previous stage and create a tree called as syntax tree based on hierarchy.

\*.) Semantic analysis checks the meaning of Syntax (i.e., implicit or explicit type conversion).

\*.) Intermediate code generation goes through the tree and produces three address code.

$a + b \times c$   
 $t_1 = b \times c$   
 $t_2 = a + t_1$

This will be the intermediate code generation.

Three address code  $\rightarrow$  consists two operators  
and three operands.

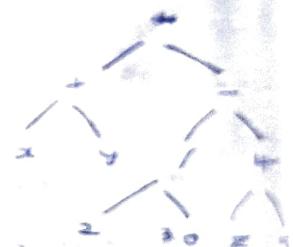
\* code optimization will be optional phase.  
Here the size of the code will be reduced. It takes three address code and produces an optimised three address code.

\* code generation phase, will take three address code and generates assembly code.

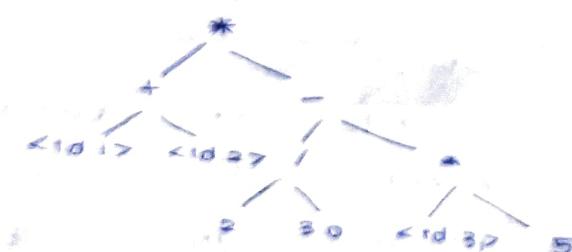
Lexical Analysis:  
 $x + y * z / 30 - 2 * 5$  where  $x, y$  are real.

Lexical analysis

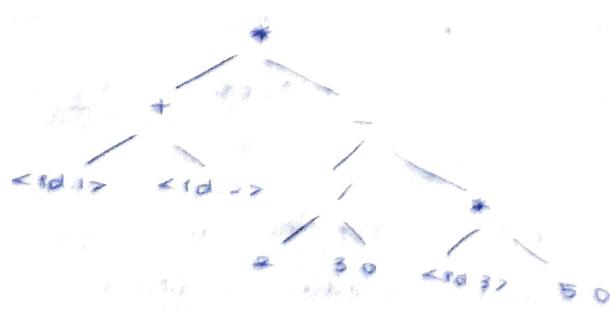
$<\text{id } 1> <\text{id } 2> <\text{id } 3> <\text{id } 4> <\text{id } 5>$



Syntax analysis



Semantic analysis



Intermediate code generation

$$\begin{aligned}
 t_1 &= \langle \text{rd1} \rangle + \langle \text{rd2} \rangle \\
 t_2 &= \text{Float}(2) \\
 t_3 &= t_2 / 3.0 \\
 t_4 &= \text{Float}(5) \\
 t_5 &= \langle \text{rd3} \rangle * t_4 \\
 t_6 &= t_3 - t_5 \\
 t_7 &= t_1 * t_6
 \end{aligned}$$

### Code optimization

$$\begin{aligned}
 t_1 &= \langle \text{rd1} \rangle \gg + \langle \text{rd2} \rangle \\
 t_2 &= 2.0 / 3.0 \\
 t_3 &= \langle \text{rd3} \rangle * 5.0 \\
 t_4 &= t_2 - t_3 \\
 t_5 &= t_1 * t_4
 \end{aligned}$$

### Code generation

LDF	$R_1, \text{rd}_1$
LDF	$R_2, \text{rd}_2$
ADDF	$R_1, R_1, R_2$
DIVF	$R_3, \#2.0, \#3.0$
LDF	$R_4, \text{rd}_3$
MULF	$R_4, R_4, \#5.0$
SUBF	$R_3, R_3, R_4$
MULF	$R_1, R_1, R_3$

### Reasons for separation of lexical phase and

- \* Compiler simplicity. (or) simplicity in design.

- \* Compiler portability.

- \* Compiler efficiency.

Three important terms:

- \* Token.  $\rightarrow$  pair  $\rightarrow$  token, symbol table entry.

- \* Pattern.  $\rightarrow$  Rule or structure for framing a token.

- \* Lexeme.  $\rightarrow$  sequence of characters that matches a pattern to form a token.

abstract symbol which  
represents lexical unit.  
optional.

## Error in lexical analysis:

- \*) Lexical analysis will show an error if any of the character that doesn't matches any of the pattern.
- \*) Error handler will try to delete a character, insert a character, replace characters (replace ~~one~~ one character with other), transposing two adjacent character.

## Panic error recovery mode:

- Delete a character.
- Insert a character.
- Replace a character with other character.
- Transposing two adjacent characters.

→ used to store characters while scanning.

## ~~Input~~ Buffering:

- \*) In order to process a sequence of characters, an input buffer is used to store the sequence of characters. (One character matread pani token generate panna mudriyaathusso we are using input buffer).

- \*) It is a buffer which is divided into two of size 4096 bytes.

N	N
a=b* EOF	c EOF

It consists of two pointers

- Lexeme binary → current beginning of lexeme.
- forward → to more forward.

- For every character we have to check whether it is EOF. If EOF is <sup>read</sup> in first buffer, reload the second buffer and if End of Buffer (EOB) is read in second buffer, reload the first buffer.

\*) It takes more time for checking this.

\*) To reduce this time, we are using sentinels which uses the concept of EOF. Only EOF can be checked.

String = "Kongu";

Prefix E, K, Ko, Kon, Kong, Kongu

proper prefix K, Ko, Kon, Kong

Suffix E, u, gu, ngu, ongu, Kongu

proper suffix u, gu, ngu, ongu

Substring continuous sequence (K, o, n, g, u, Ko, on, ng, gu, Kon, ong, ngu, Kong, ongu, Kongu)

Subsequence characters may not be in sequence.

What will the prefix, proper prefix and substring when a string of length  $n$  is given?

Soln: Prefix  $\Rightarrow n+1$  Suffix  $\Rightarrow n+1$

Proper prefix  $\Rightarrow n-1$  Subsequence  $= 2^n$

Substring  $\Rightarrow \frac{n(n+1)}{2} + 1$  if we include empty substring  
used to describe the pattern.

Regular Expression:

Regular expression has only three operators.

(i) closure (\*)

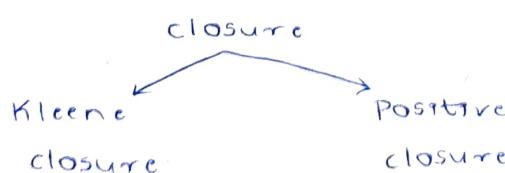
Priority,

(ii) Concatenation (.)

$* > . > / \text{ or } +$

(iii) Union (/ or +).

\*) closure is of two types.



\*) String is a set of alphabets which

is represented by  $\Sigma$ . (sigma)

consider,

$$\Sigma = \{a, b\}$$

→ Denotes create a string of length 0 from the above string.

$$\Sigma^0 = \{\epsilon\} \rightarrow$$
 since it is zero, nothing so epsilon will be used.

$$\Sigma^1 = \{a\}$$

$$\Sigma^2 = \{ab, ba\}$$

\*.)  $L = \{\text{collection of strings}\}$

$$L = a^* \rightarrow L = a^+ (\geq 1 \text{ or more})$$
 Erla venaaalu varalgaam but 'a' atleast one time varanum.

$$L = a^* \leftarrow L = \{\epsilon, a, aa, aaa, aaaa, \dots\}$$
 (Kleene closure)

$$L = a^+ \leftarrow L = \{a, aa, aaa, aaaa, \dots\}$$
 (positive closure)

\* → includes epsilon

+ → does not includes epsilon.

convention

for naming a ranable  $\Rightarrow L \cdot (L/d)^*$   
variable + ↓ ↴ variable (or) any no. of digit times

Rough notes      Definitions

\* → 0 or more

+ → 1 or more

? → 0 or 1

$$L = a^*$$

$$L = \{\epsilon, a, aa, \dots\}$$

$$L = L^0 \cup L^1 \cup L^2 \dots$$

$$\cancel{\text{defn}} \quad L^* = \bigcup_{i=0}^{\infty} L^i$$

$$L^+ = \bigcup_{i=1}^{\infty} L^i$$

$$L^? = L^0 \cup L^1$$

$$L^* = L^+ + \epsilon$$

$$L^+ = L^* - \epsilon$$

\*.) If Regular Expression is taken as RE and set of strings that can be formed (or language) is taken as L.

(i)  $RE = \{\epsilon\} \Rightarrow L = \{\epsilon\}$

(ii)  $RE = \{a\} \Rightarrow L = \{a\}$

(iii)  $RE = \{a/b\} \Rightarrow L = \{a, b\}$

(iv)  $RE = a \cdot (a/b) \Rightarrow L = \{aa, ab\}$

(v)  $RE = a \cdot (a/b)^* \Rightarrow L = \{a, aa, aaa, ab, abb, abba, \dots\}$

(vi)  $RE = (a/b) \cdot (a/b) \Rightarrow L = \{aa, ab, ba, bb\}$

\*.) Given a set of all possible strings, find the Regular expression.

(i)  $L$  = set of all strings that starts with '0' over  $\{0, 1\}$ .

$$L = \{0, 0000^*, 00, 01, 0111, \dots\}$$

$$RE = 0 \cdot (0/1)^*$$

(ii)  $L$  = set of all strings having odd number of 1's over  $\{0, 1\}$ .

$$L = \{1, 11, 111, \dots\}$$

$$RE = 0^* \cdot 1 \cdot (00)^* \cdot (11)^* \cdot (00)^*$$

(iii)  $L$  = set of all strings with '01' as substring over  $\{0, 1\}$ .

$$RE = (0/1)^* \cdot 01 \cdot (0/1)^*$$

(iv)  $L$  = set of all strings that ends with 'bb' over  $\{a, b\}$ .

$$RE = (a/b)^* bb$$

Regular expressions are recognized by finite automata.

Regular definition:

letter ~~is~~ → [A-Z a-z]

digit → [0-9]

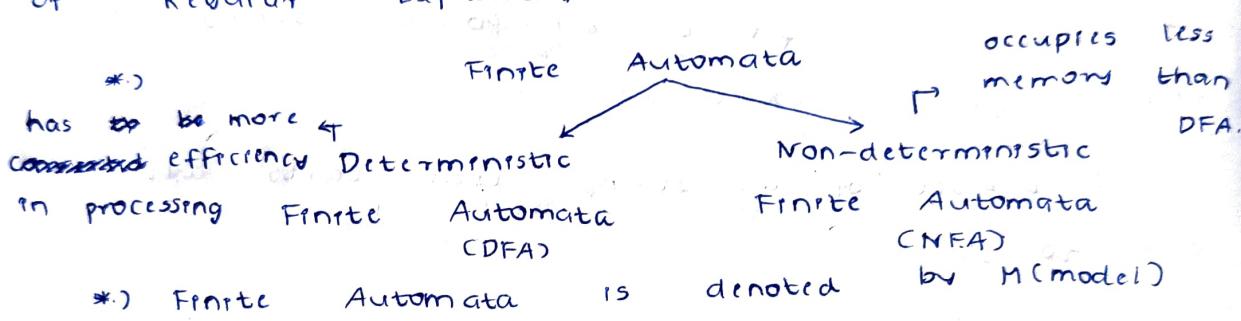
Id → letter (letter/digit)\*

digits → [0-9] + (or) [0-9][0-9]\*

Float number → [0-9] +, [0-9]\*

Finite Automata: (If n is given, the no. of states will be  $n+1$ )

\*) Simple transition model that accepts string of Regular Expression.



\*) Finite Automata is denoted by  $M$  (model)

$$M = (Q, \Sigma, \delta, q_0, F)$$

where,

$Q$  → set of all states of finite automata.

$\Sigma$  → set of input alphabets.

$\delta$  → transition function.

$q_0$  → initial state of automata.

$F$  → final state of automata.

DFA ⇒ If a finite automata model has only one input on a transition to other state. Every symbol of finite automata should have only one transition.

In  
NFA ⇒ If a finite automata models, if an input symbol having more than one transition is present to more than one state called as non-deterministic.

Regular expression defines a pattern for lexical analysis.

Example of DFA,

$$L = \{ay\}$$

$$RE = a^*y$$



Transition

diagram

Set of all states	input values	a
$q_0$	$q_0$	$q_1$
$q_1$	-	-

$$M = (Q, \Sigma, \delta, q_0, F)$$

$$Q = \{q_0, q_1\}$$

$$\Sigma = \{a, y\}$$

$$\delta(q_0, a) = q_1$$

$$q_0 = q_0$$

$$F = q_1$$

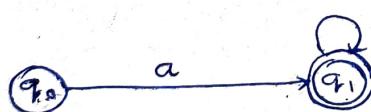
$\circ$  → initial state

$\bullet$  → Final state

(ii)  $L = \{a, aa, aaa, \dots\}$

$$RE = a^+$$

Whenever an finite automata model is drawn, it should be drawn for minimal string.



$$RE = a^*$$

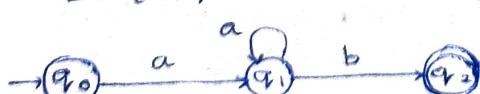


(iii)  $L = \{ab\}$

$$RE = ab$$



(iv)  $L = \{ab, aab, aaab, \dots\}$ ,  $RE = a^+b$



Set of all states	input values	a	b
$q_0$		$q_1$	-
$q_1$		$q_1$	$q_2$
$q_2$		-	-

1)  $L = \text{set of all strings with odd number of } 1's \text{ over } \{0,1\}$

$$L = \{1, 111, 1111, \dots\}$$

$$RE = 0^*, 1 \cdot (0)^*, (11)^*, (0)^*$$



0	1
q0	q0
q1	q1

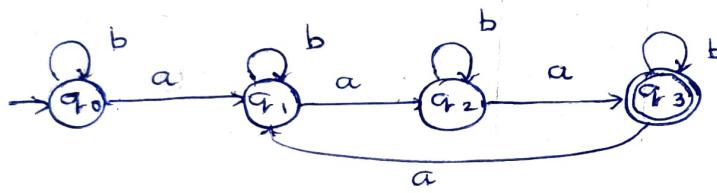
2)  $L = \text{set of all strings over } \{a,b\} \text{ that accepts string with number of } 'a' \text{ is divisible by 3.}$

3.

Soln:

$$RE = b^* (aaa)^*$$

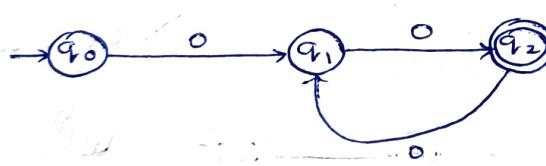
$$b^* (ab^*ab^*a)^+ b^*$$



3)  $L = \{00, 0000, 000000, \dots\}$

Soln:

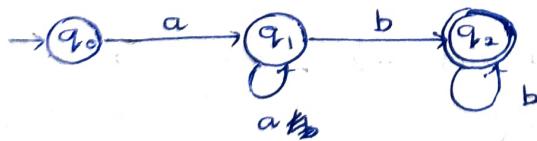
$$RE = (00)^+$$



4)  $RE = (a/b)^* ab$

$$L = \{ab, aab, aabb, \dots\}$$

Soln:



5)  $L = \{01, 00111, 000100, \dots\}$

Soln:

$$RE = (00)^* 01$$

\*.) NFA can have  $\epsilon$  as input (i.e., It can make transition from one state to another state without reading any input).

\*.) NFA occupies less memory than DFA.

\*.) DFA is more efficient in processing. So, NFA should be converted into DFA while processing.

\*.) DFA cannot have  $\epsilon$  as input.

Rules for converting Regular expression into

$\epsilon$ -NFA:

1)  $\epsilon$

Regular Expression

$\epsilon$ -NFA



2) a

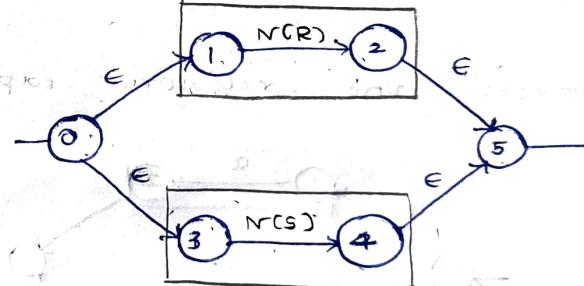


3)  $R_5 \rightarrow R/S$

(or)

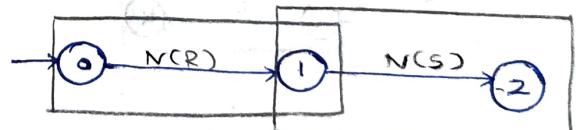
$R+S$

a/b concat b

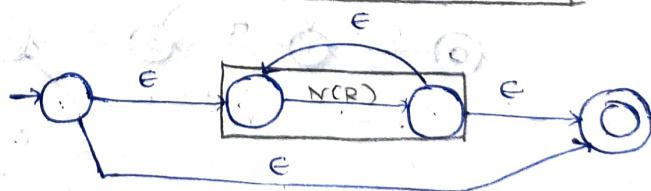


4) R.S

a.b



5)  $R^*$  or  $a^*$

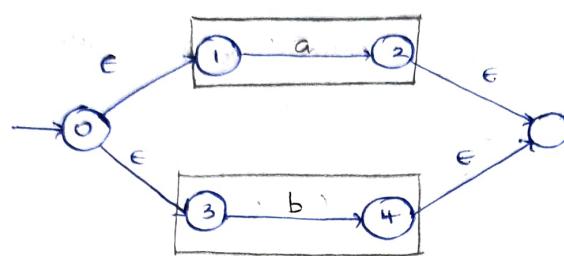


The process of converting a regular expression into  $\epsilon$ -NFA is called as

Thomson's construction method.

1) convert the regular expression  $a/b$  to  $\epsilon$ -NFA.

Soln:



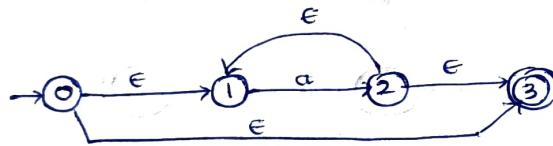
2) convert the regular expression  $a.b$  to  $\epsilon$ -NFA.

Soln:



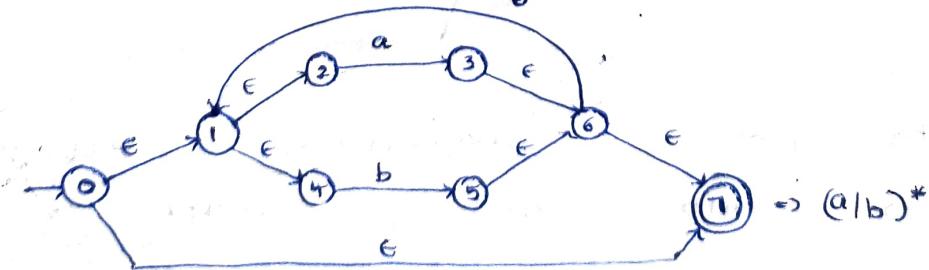
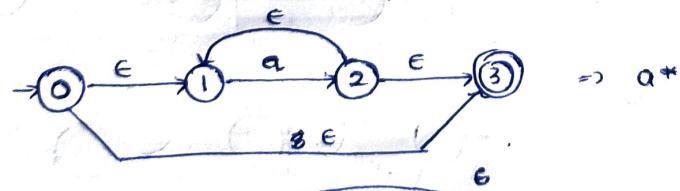
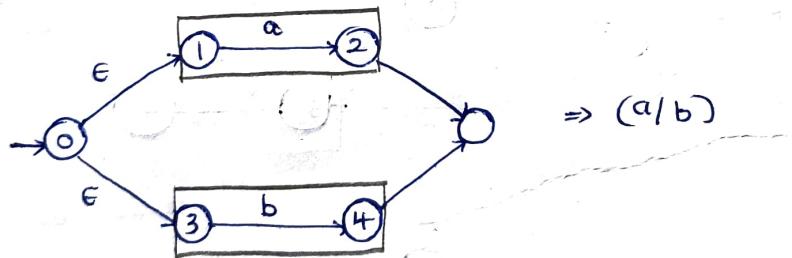
3) convert the regular expression  $a^*$  to  $\epsilon$ -NFA.

Soln:



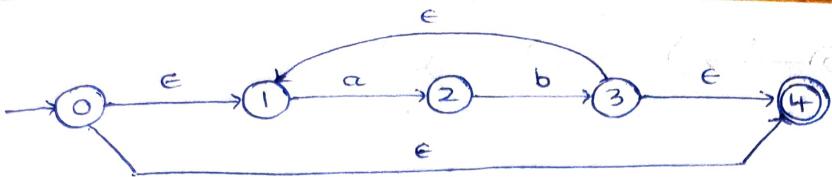
4) convert the regular expression  $(a/b)^*$  to  $\epsilon$ -NFA.

Soln:



5) convert the regular expression  $(a.b)^*$  to  $\epsilon$ -NFA.

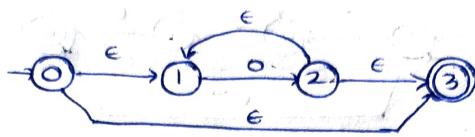
Soln:



6) Convert the regular expression  $01/0^*$  into  $\epsilon$ -NFA.

Soln:

$$0^* \Rightarrow$$

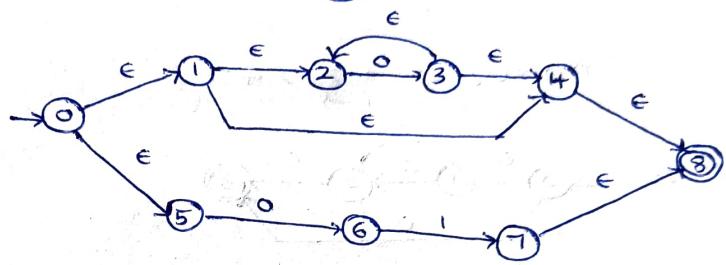


$$0.1/0^*$$

$$01 \Rightarrow$$



$$01/0^* \Rightarrow$$

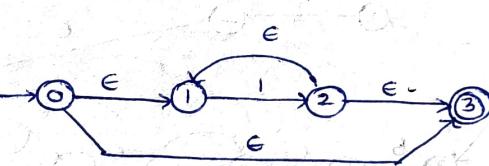


7) Convert the regular expression into  $\epsilon$ -NFA  
 (i)  $1^*/0^*$       (ii)  $1^*.0^*$

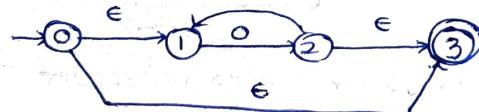
Soln:

$$(i) 1^*/0^*$$

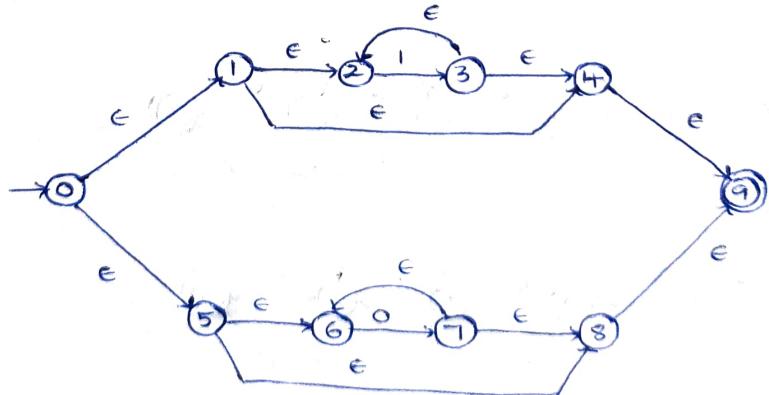
$$1^* \Rightarrow$$



$$0^* \Rightarrow$$

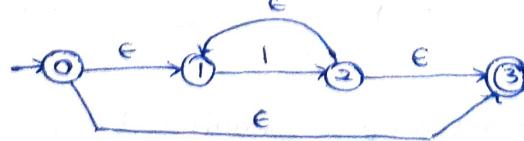


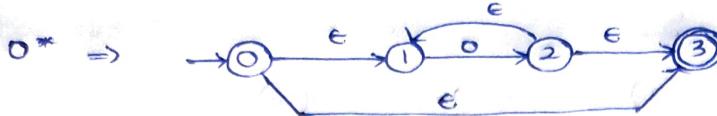
$$1^*/0^* \Rightarrow$$



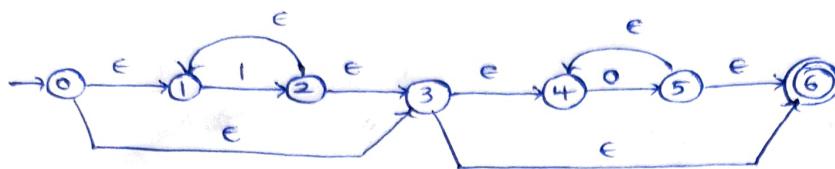
$$(ii) 1^*.0^*$$

$$1^* \Rightarrow$$





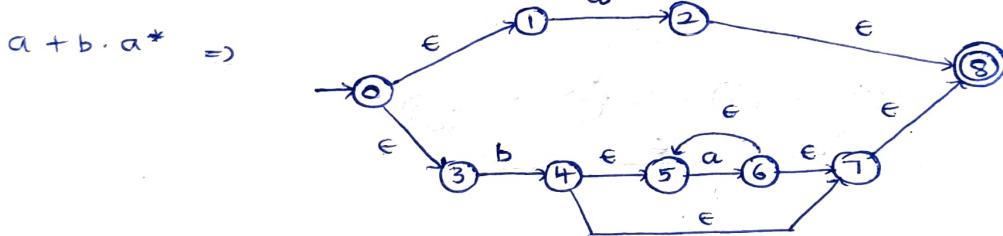
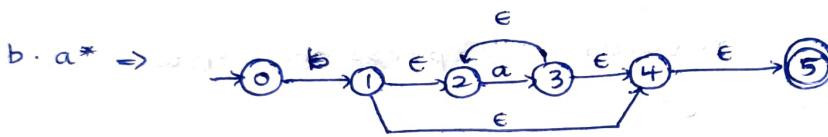
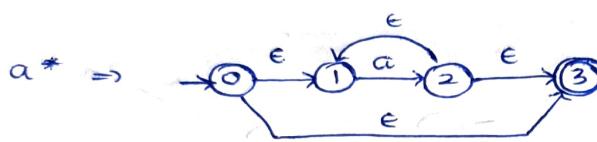
$1^*, 0^* \Rightarrow$



8) convert the regular expression  $a+b \cdot a^*$  into  $\epsilon$ -NFA.

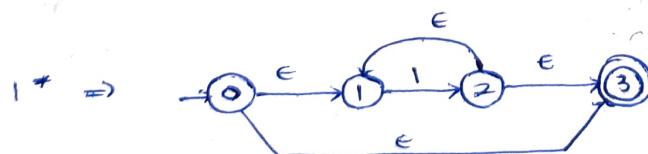
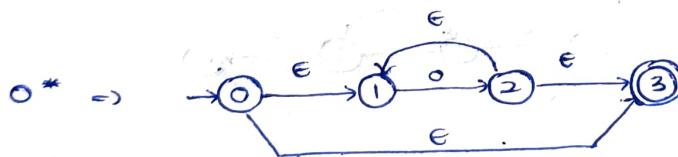
Soln:

Priorities  $\Rightarrow * > . > +$



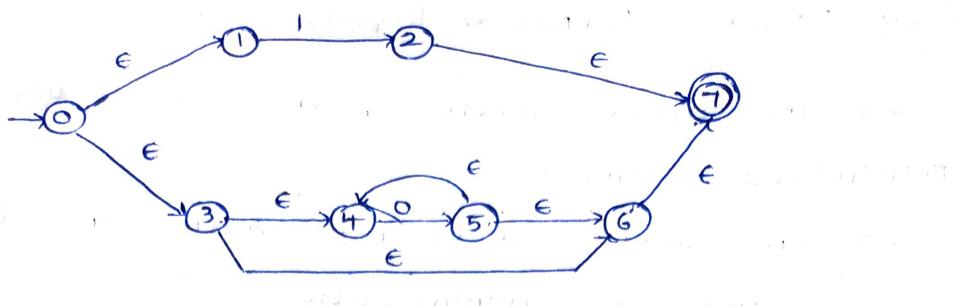
9) convert the regular expression  $1/0^*/1^*$  into  $\epsilon$ -NFA.

Soln:

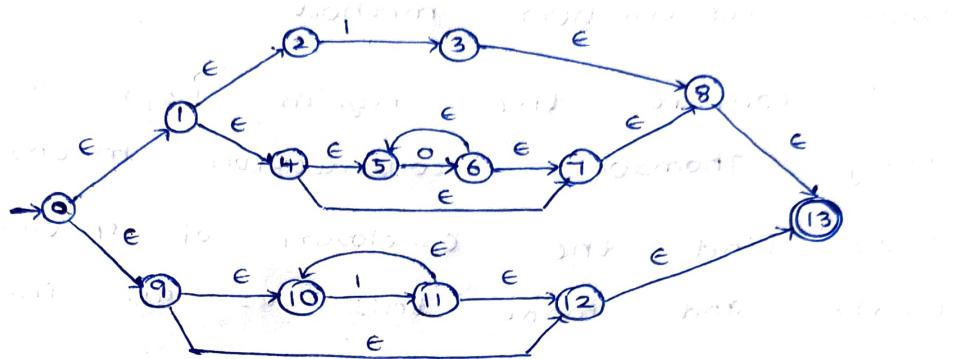


$1/0^*/1^* \Rightarrow$  Associativity from Left to Right.

$1/\varnothing^* \Rightarrow$



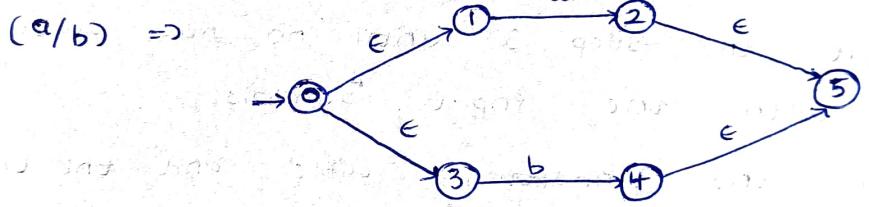
$1/\varnothing^*/1^* \Rightarrow$



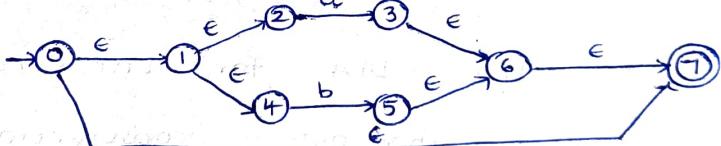
10) Convert the following regular expression

$(a/b)^* abb \text{ into } \epsilon\text{-NFA}.$

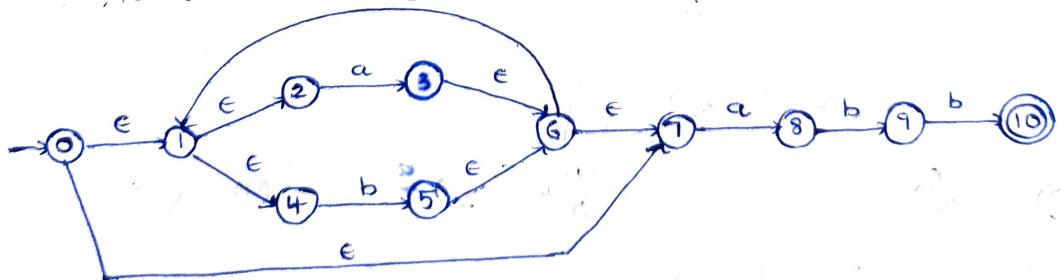
Soln:



$(a/b)^* \Rightarrow$



$(a/b)^* abb \Rightarrow$



Regular Expression	to	NFA	to	DFA
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Two ways to convert regular expression

into DFA

(i) subset construction

Method  $\Rightarrow$  Regular expression

to  $\epsilon\text{-NFA}$  - then to DFA.

(ii) Direct Method  $\Rightarrow$  Regular Expression - DFA

\*.) In direct method, the DFA obtained is minimized (optimal).

\*) In subset construction method, the DFA obtained must undergo minimization.

Subset construction method:

1) Convert the regular expression to  $\epsilon$ -NFA using Thomson's construction method.

2) Find the  $\epsilon$ -closure of initial state of  $\epsilon$ -NFA and make this as an initial state of DFA.

3) Find the moves on the input symbols in the regular expression.

4) Repeat the step 3 until no new state is obtained with the input symbols.

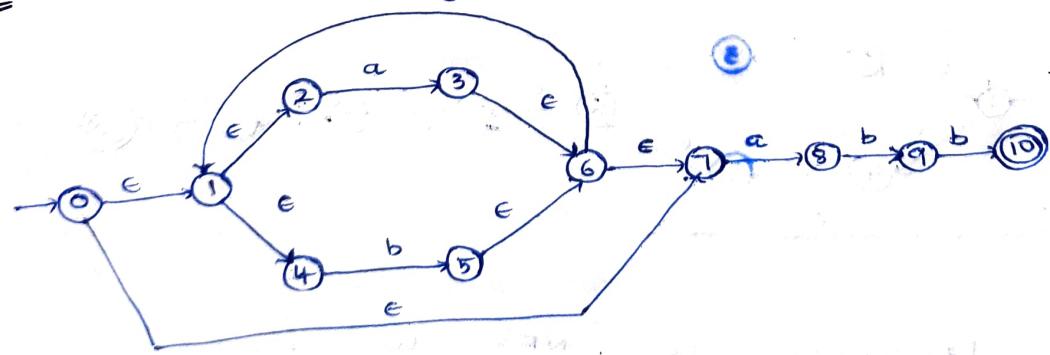
5) Draw the transition table and the transition diagram which is the required DFA.

1) construct the DFA for the regular expression

Thomson's construction method.

(a|b)\* abb using

Soln: (i)  $\epsilon$ -NFA for the regular expression



(ii)  $\epsilon$ -closure of initial state

set of all states reached by ~~reading~~ reading  $\epsilon \Rightarrow \epsilon$ -closure

$$\epsilon\text{-closure}(0) = \{0, 1, 2, 4, 7\}$$

Make this as initial state of DFA,

$$\epsilon\text{-closure}(0) = \{0, 1, 2, 4, 7\} \rightarrow A$$

(iii)  $\rightarrow \epsilon\text{-closure}$  la inukku valis la ethu  
\*)  $\text{Move}(A, a) = \{3, 8\}$  a, vch input ah eduthu enna,  
↳ Regular expression la inukku state ku pothun eluthanum.  
 $\epsilon\text{-closure}(\text{Move}(A, a)) = \epsilon\text{-closure}(\{3, 8\})$  ella input  
 $= \epsilon\text{-closure}(3) \cup \epsilon\text{-closure}(8)$  state kum  
 $= \{3, 6, 7, 1, 2, 4\} \cup \{8\}$  Podanum  
 $= \{1, 2, 3, 4, 6, 7, 8\} \rightarrow$  compare thrs with  
on state A, which is different so assign it as  
a new state B.

$$B = \{1, 2, 3, 4, 6, 7, 8\}$$

$$\text{Move}(A, b) = \{5\} = \emptyset$$

$$\epsilon\text{-closure}(\text{Move}(A, b)) = \epsilon\text{-closure}(5) \\ = \{5, 6, 7, 1, 2, 4\} \rightarrow C$$

$$*) \text{Move}(B, a) = \{3, 8\}$$

$$\therefore = \{1, 2, 3, 4, 6, 7, 8\} \rightarrow B$$

$$\text{Move}(B, b) = \{5, 9\}$$

$$\epsilon\text{-closure}(\text{Move}(B, b)) = \epsilon\text{-closure}(\{5, 9\}) \\ = \epsilon\text{-closure}(5) \cup \epsilon\text{-closure}(9) \\ = \{5, 6, 7, 1, 2, 4\} \cup \{9\} \\ = \{1, 2, 4, 5, 6, 7, 9\} \rightarrow D$$

$$*) \text{Move}(C, a) = \{3, 8\}$$

$$\epsilon\text{-closure}(\text{Move}(C, a)) = \epsilon\text{-closure}(\{3, 8\}) \\ = \epsilon\text{-closure}(3) \cup \epsilon\text{-closure}(8) \\ = \{3, 6, 7, 1, 2, 4\} \cup \{8\} \\ = \{1, 2, 3, 4, 6, 7, 8\} \rightarrow B$$

$$\text{Move}(C, b) = \{5\}$$

$$\epsilon\text{-closure}(\text{Move}(C, b)) = \epsilon\text{-closure}(5) \\ = \{5, 6, 7, 1, 2, 4\} \rightarrow C$$

$$*) \text{ Move}(D, a) = \{3, 8\}$$

$$\epsilon\text{-closure}(\{3, 8\}) = \{1, 2, 3, 4, 6, 7, 8\}$$

$$\text{Move}(D, b) = \{5, 10\}$$

$$\epsilon\text{-closure}(\text{Move}(D, b)) = \epsilon\text{-closure}(\{5, 10\})$$

$$= \epsilon\text{-closure}(5) \cup \epsilon\text{-closure}(10)$$

$$= \{5, 6, 7, 1, 2, 4\} \cup \{10\}$$

$$= \{1, 2, 4, 5, 6, 7, 10\} \rightarrow E$$

$$*) \text{ Move}(E, a) = \{3, 8\}$$

$$\epsilon\text{-closure}(\{3, 8\}) = \{1, 2, 3, 4, 6, 7, 8\}$$

$$\text{Move}(E, b) = \{5\}$$

$$\epsilon\text{-closure}(\{5\}) = \{5, 6, 7, 1, 2, 4\}$$

$\text{Move}(A, a) \rightarrow B$ ,  $\text{Move}(A, b) \rightarrow C$ ,  $\text{Move}(B, a) \rightarrow B$ ,  $\text{Move}(B, b) \rightarrow D$ ,

$\text{Move}(C, a) \rightarrow B$ ,  $\text{Move}(C, b) \rightarrow C$ ,  $\text{Move}(D, a) \rightarrow B$ ,  $\text{Move}(D, b) \rightarrow E$ ,

$\text{Move}(E, a) \rightarrow B$ ,  $\text{Move}(E, b) \rightarrow C$

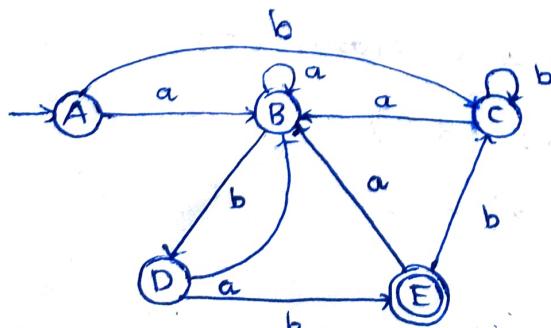
Transition Table

(iv)

	input	symbol
states	a	b
A	B	C
B	B	D
C	B	C
D	B	E
E	B	C

Transition Diagram

(v)



Initial state  $\rightarrow A$

Final state  $\rightarrow E$

E-NFA last value of state is final state, if it is present in move to one, all will be final states.

2) Construct the DFA for the regular expression

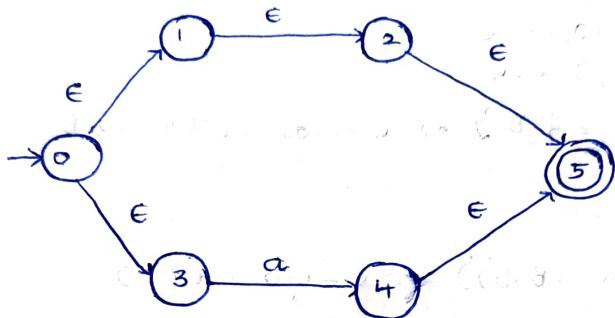
$$((\epsilon/a) \cdot b^*)^* \quad \text{or} \quad a^*/b^* \cdot a/b.$$

$$(1) ((\epsilon/a) \cdot b^*)^*$$

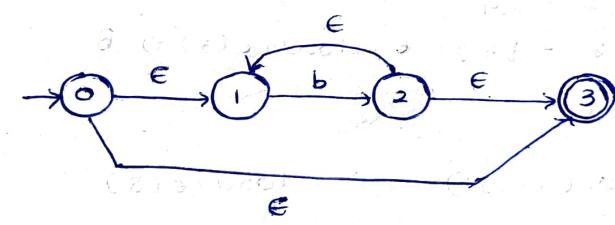
Step 1:  $\epsilon$ -NFA for the regular expression.



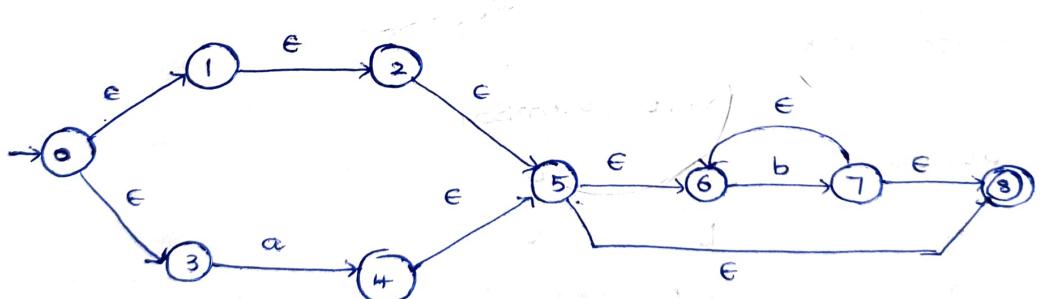
$(\epsilon/a)$



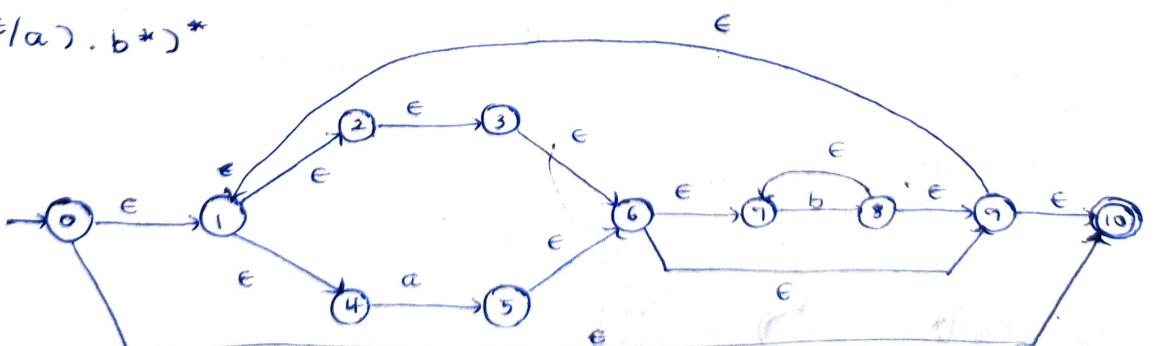
$b^*$



$(\epsilon/a) \cdot b^* \Rightarrow$



$((\epsilon/a) \cdot b^*)^*$



Step 2:  $\epsilon$ -closure of initial state

$$\epsilon\text{-closure}(0) = \{0, 1, 2, 3, 6, 7, 4, 9, 10\}$$

Make this as initial state of DFA.

$$\epsilon\text{-closure}(0) = \{0, 1, 2, 3, 4, 6, 7, 9, 10\} \rightarrow A$$

Step 3:

$$\text{More}(A, a) = \{5\}$$

$$\begin{aligned} *.) \quad \epsilon\text{-closure}(\text{More}(A, a)) &\Rightarrow \epsilon\text{-closure}(5) \\ &= \{5, 6, 7, 9, 10\} \rightarrow B \\ &\quad 1, 2, 3, 4 \end{aligned}$$

$$\text{More}(A, b) = \{8\}$$

$$\begin{aligned} *.) \quad \epsilon\text{-closure}(\text{More}(A, b)) &\Rightarrow \epsilon\text{-closure}(8) \\ &= \{8, 7, 9, 10\} \rightarrow C \\ &\quad 1, 2, 3, 6, 4 \end{aligned}$$

$$\text{More}(B, a) = \{5\} = \{5\} \Rightarrow \epsilon\text{-closure}(5) \Rightarrow B$$

$$\text{More}(B, b) = \{8\}$$

$$\begin{aligned} *.) \quad \epsilon\text{-closure}(\text{More}(B, b)) &\Rightarrow \epsilon\text{-closure}(8) \\ &= \{8, 7, 9, 10\} \rightarrow C \\ &\quad 1, 2, 3, 6, 4 \end{aligned}$$

$$\text{More}(C, a) = \{5\} = \{5\} \Rightarrow \epsilon\text{-closure}(5) \Rightarrow B$$

$$\text{More}(C, b) = \{8\}$$

$$\begin{aligned} *.) \quad \epsilon\text{-closure}(\text{More}(C, b)) &\Rightarrow \epsilon\text{-closure}(8) \\ &= \{8, 7, 9, 10\} \rightarrow C \\ &\quad 1, 2, 3, 6, 4 \end{aligned}$$

Step 4:

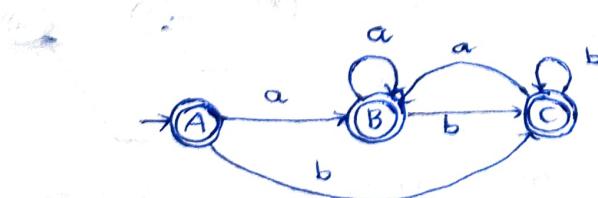
Transition table

(input symbol)

states	a	b
A	B	C
B	B	C
C	B	C

Step 5:

Transition diagram



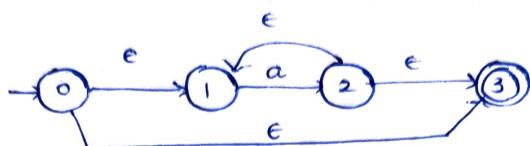
(iii)  $a^*/b^*. a/b$

Soln:

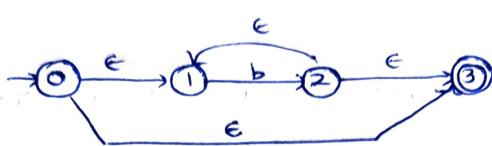
\* > . > + (or) /

Step 1:

$a^* \Rightarrow$



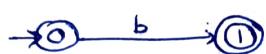
$b^* \Rightarrow$



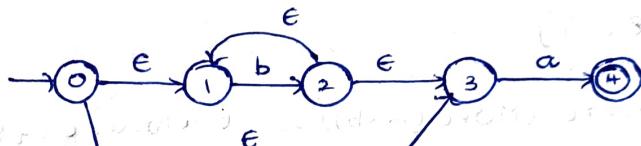
~~a~~  $\Rightarrow$



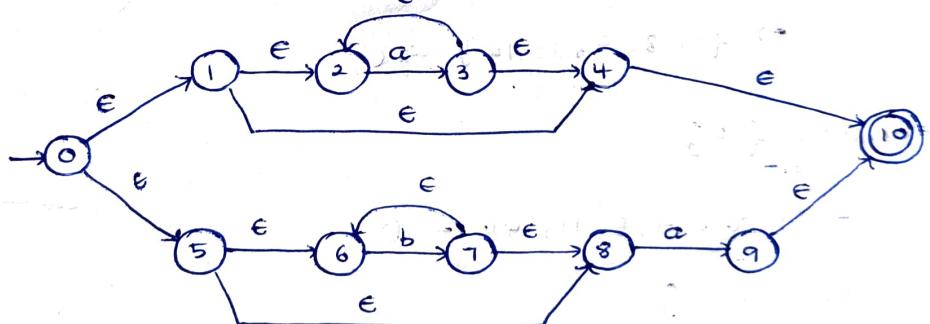
$b \Rightarrow$



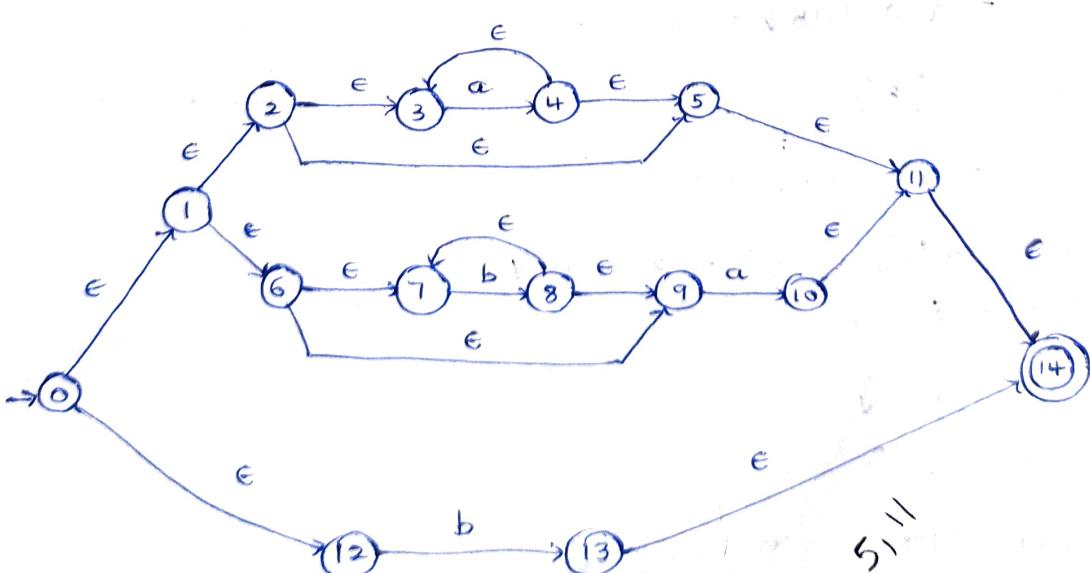
$b^*, a \Rightarrow$



$a^*/b^*a \Rightarrow$



$a^*/b^*a/b \Rightarrow$



0112131511

Step 2:

$$\epsilon\text{-closure}(0) = \{0, 1, 2, 3, 5, 11, 14, 6, 7, 9, 12\}$$

$$A = \{0, 1, 2, 3, 5, 6, 7, 9, 11, 12, 14\}$$

Step 3:

$$\text{Move}(A, a) = \{4, 10\}$$

$$\star \cdot \epsilon\text{-closure}(\text{Move}(A, a)) \Rightarrow \epsilon\text{-closure}(\{4, 10\})$$

$$\Rightarrow \epsilon\text{-closure}(4) \cup \epsilon\text{-closure}(10)$$

$$\Rightarrow \{3, 4, 5, 11, 14\} \cup \{10, 11, 14\}$$

$$\Rightarrow \{3, 4, 5, 10, 11, 14\} \rightarrow B$$

$$\text{Move}(A, b) = \{8, 13\}$$

$$\star \cdot \epsilon\text{-closure}(\text{Move}(A, b)) \Rightarrow \epsilon\text{-closure}(\{8, 13\})$$

$$\Rightarrow \epsilon\text{-closure}(8) \cup \epsilon\text{-closure}(13)$$

$$\Rightarrow \{8, 7, 9\} \cup \{13, 14\}$$

$$\Rightarrow \{7, 8, 9, 13, 14\} \rightarrow C$$

$$\text{Move}(B, a) = \{4\}$$

$$\Rightarrow \{3, 4, 5, 11, 14\} \rightarrow D$$

$$\text{Move}(B, b) = \{\}$$

$$\text{Move}(C, a) = \{10\}$$

$$= \{10, 11, 14\} \rightarrow E$$

$$\text{Move}(C, b) = \{8\}$$

$$= \{8, 7, 9\} \rightarrow F$$

$$\text{Move}(D, a) = \{4\} \Rightarrow \{3, 4, 5, 11, 14\} \rightarrow D$$

$$\text{Move}(D, b) = \{\}$$

$$\text{Move}(E, a) = \{\}$$

$$\text{Move}(E, b) = \{\}$$

$$\text{Move}(F, a) = \{10\} \Rightarrow \{10, 11, 14\} \rightarrow E$$

$$\text{Move}(F, b) = \{8\} \Rightarrow \{8, 7, 9\} \rightarrow F$$

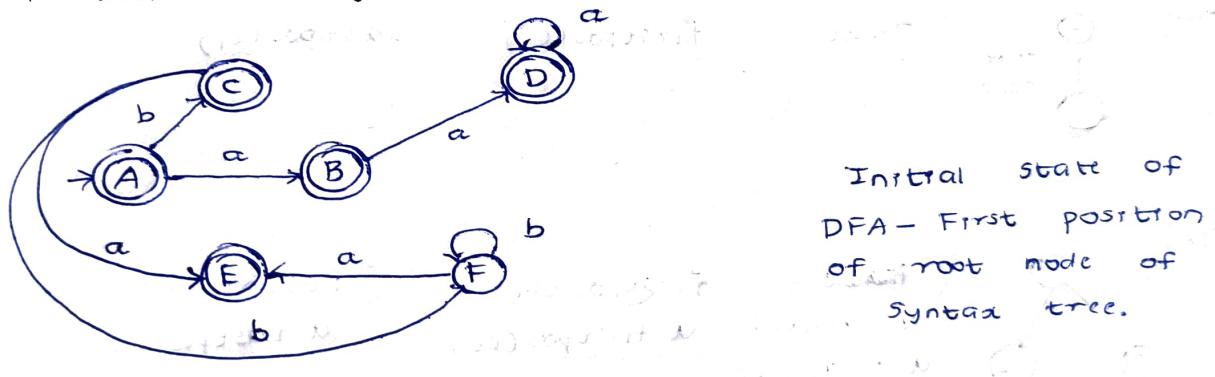
Step 4:

### Transition table

		Input symbol)	
states	a	b	c
A	B	C	-
B	D	-	-
C	E	F	-
D	D	-	-
E	-	-	-
F	E	F	-

Step 5:

### Transition diagram



Initial state of  
DFA - First position  
of root node of  
Syntax tree.

Regular Expression to DFA - Direct method:

Step 1: Place an unique end marker  $\#$  expression  $R^* \cdot R\#$  is called for the regular as augmented grammar.

Step 2: Any DFA state, having a transition to  $\#$  must be the final state of DFA.

Step 3: construct a syntax tree for the augmented grammar. The nodes of the syntax tree will be the operators of the regular expression. The leaves may be alphabets or  $\#$ .

Step 4: OR nodes are represented as  $\wedge$ ?

(ii) cat nodes will be represented with '\*'.

(iii) star nodes will be represented with '\*'.

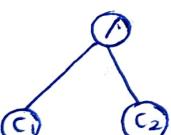
/ & \* will have two children + have one child

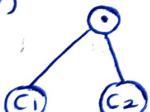
Step 5: compute the nullable, first position, last position for the + nodes and leaves of the Syntax tree using the following table. All leaves nodes except '\*' will be given positions which starts from node nullable firstpos lastpos

(i) leaf is labelled with 'ε' True  $\emptyset$   $\emptyset$

(ii) leaf is labelled with some position  $\{?\}$   $\{?\}$   
 $\{?\}$

(iii)  Star node  
True firstpos(c<sub>1</sub>) Lastpos(c<sub>1</sub>)

(iv)  Plus node  
False firstpos(c<sub>1</sub>)  $\cup$  firstpos(c<sub>2</sub>) Lastpos(c<sub>1</sub>)  $\cup$  Lastpos(c<sub>2</sub>)  
Nullable(c<sub>1</sub>) Nullable(c<sub>2</sub>)

(v)  Cat node  
False if nullable(c<sub>1</sub>) then firstpos(c<sub>1</sub>)  $\cup$  firstpos(c<sub>2</sub>) else firstpos(c<sub>1</sub>).  
Nullable(c<sub>1</sub>) && Nullable(c<sub>2</sub>)  
if nullable(c<sub>2</sub>) then lastpos(c<sub>1</sub>)  $\cup$  lastpos(c<sub>2</sub>) else lastpos(c<sub>2</sub>)

Step 6: (i) Compute the follow position for \* and cat(\*) node.

(i) If 'n' is a star node then,  
 $\text{lastpos}(n) \leftarrow \text{firstpos}(n)$ .

(ii) If 'n' is a cat node then,

$\text{lastpos}(c_1) \leftarrow \text{firstpos}(c_2)$

Step 7: Compute the DFA transition with the initial state as the first position of the rootnode of the syntax tree.

Step 8: The obtained DFA is the minimised DFA.

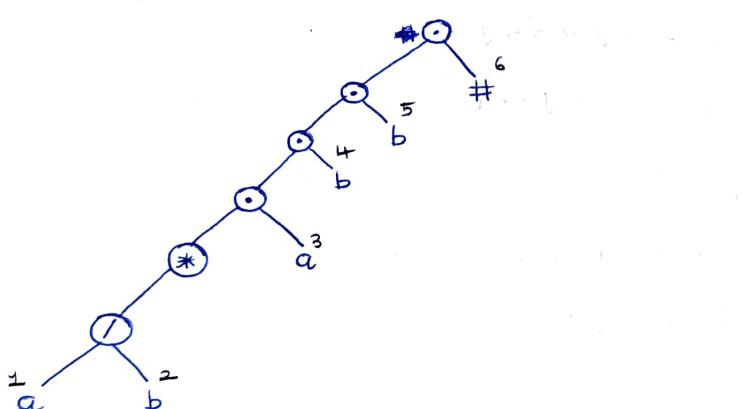
i) Construct a DFA for RE  $(a/b)^*abb$  using direct method.

Soln:  
= (i) Add an # (unique marker) to the end of the regular expression.

Augmented grammar

$(a/b)^* \cdot a.b.b.\#$

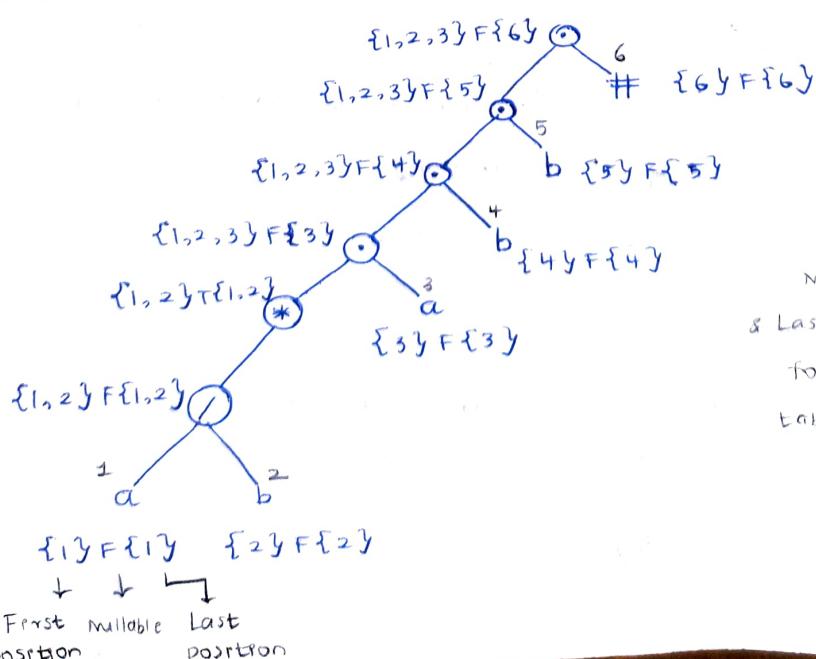
(ii) Syntax tree



Here operators are nodes and variables are leaf.

(After constructing syntax tree, all leaves nodes except # should be numbered from 1 to n).

(iii)



Nullable, First position & Last position are found using the table given.

(iv) Finding follow positions for \* and + node

Nodes	position
1	{1, 2, 3}
2	{1, 2, 3}
3	{4}
4	{5}
5	{6}
6	-

DFA transition

Initial state - {1, 2, 3} - A (Intha values kaach tree axi compare pananum, athu tree la enga a vanithunu)

$$\text{Move}(A, a) = \{1, 3\}$$

paakanum for Move(A, a)

$$D\text{tran}(\text{Move}(A, a)) = \text{Followpos}(1) \cup$$

$$\text{Followpos}(3)$$

$$= \{1, 2, 3\} \cup \{4\}$$

$$= \{1, 2, 3, 4\} \rightarrow B$$

$$\text{Move}(A, b) = \{2\}$$

$$D\text{tran}(\text{Move}(A, b)) = \text{Followpos}(2)$$

$$= \{1, 2, 3\} \rightarrow A$$

$$\text{Move}(B, a) = \{1, 3\}$$

~~$$D\text{tran}(\text{Move}(B, a)) = \text{Followpos}(1) \cup \text{Followpos}(3)$$~~

$$= \{1, 2, 3, 4\} \rightarrow B$$

$$\text{Move}(B, b) = \{2, 4\}$$

$$D\text{tran}(\text{Move}(B, b)) = \text{Followpos}(2) \cup \text{Followpos}(4)$$

$$= \{1, 2, 3\} \cup \{5\}$$

$$= \{1, 2, 3, 5\} \rightarrow C$$

$$\text{Move}(C, a) = \{1, 3\}$$

$$D\text{tran}(\text{Move}(C, a)) = \text{Followpos}(1) \cup \text{Followpos}(3)$$

$$= \{1, 2, 3, 4\} \rightarrow B$$

$$\text{Move}(C, b) = \{2, 5\}$$

$$\text{Dtran}(\text{More}(c, b)) = \text{Followpos}(2) \cup \text{Followpos}(5)$$

$$= \{1, 2, 3, 6\} \rightarrow D$$

$$\text{More}(D, a) = \{1, 3\}$$

$$\text{Dtran}(\text{More}(D, a)) = \{1, 2, 3, 4\} \rightarrow B$$

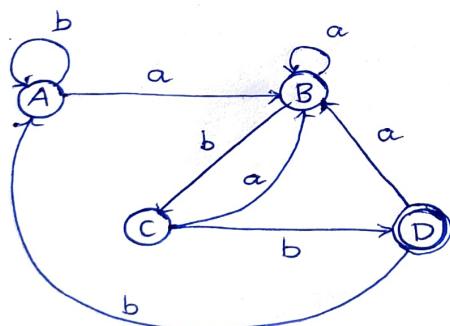
$$\text{More}(P, b) = \{5\}$$

$$\text{Dtran}(\text{More}(P, b)) = \{1, 2, 3\} \rightarrow A$$

Transition table:

states	Input symbol		syntax tree
	a	b	
A	B	A	la ethukku #
B	B	C	inukkun paakanum,
C	B	D	athu entha state
D	B	A	lilaam inko athu thaan final state

Transition Diagram:



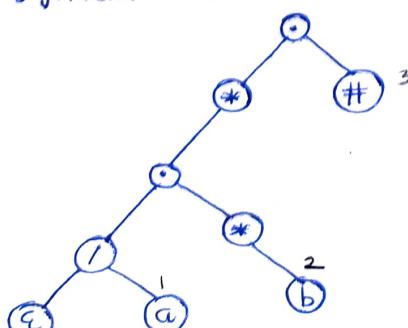
$$2) ((\epsilon/a) \cdot b^*)^*$$

Soln:

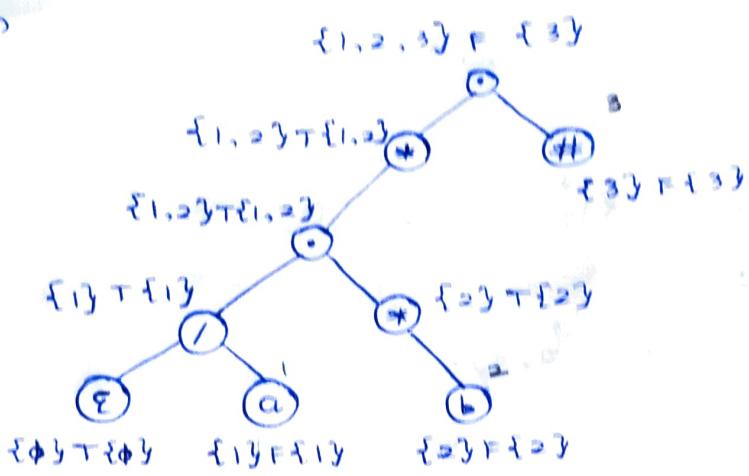
(i) Augmented grammar

$$((\epsilon/a) \cdot b^*)^* \cdot \#$$

(ii) Syntax tree



(iii)



Follow na lai  
position kya apan  
na rakhne  
padane.

(iv)

Nodes position

1  $\{2, 1, 3\}$ 2  $\{2, 1, 3\}$ 

3 —

Transition table

states	input symbol	
	a	b
A	A	A

Transition Diagram:

3)  $a^*/b^*, a/b$  ( $*$  >  $.$  >  $/$ )

soln:

(1) Augumented

Grammar

 $a^*/b^*, a/b \cdot \#$ 

(ii)

