

(1)  $T(n) = 8T(n/2) + 1000n^2$   
WKT  $T(n) = aT(n/b) + f(n)$   
 $a=8; b=2; f(n) = Cn^d$   
 $= 1000n^2$   
 $C=1000, d=2$

Since  $a > b^d$   
ie  $8 > 2^2$   
using master theorem  
 $T(n) = \Theta(n^{\log_b a})$   
 $= \Theta(n^{\log_2 8})$   
 $= \Theta(n^{\log_2 2^3}) = \Theta(n^3)$

(2)  $T(n) = 2T(n/2) + n^2$   
 $a=2; b=2; c=1; d=2$   
Since  $a < b^d$   
 $2 < 2^2$   
 $T(n) = \Theta(n^d)$   
 $T(n) = \Theta(n^2)$

(3)  $T(n) = 2T(n/2) + 10n$   
 $a=2, b=2, c=10, d=1$   
Since  $a = b^d$   
 $2 = 2^1$   
using master theorem  
 $T(n) = \Theta(n^d \log n)$   
 $T(n) = \Theta(n \log n)$