

# Lecture 15: Sorting Algorithms

CSE 373: Data Structures and Algorithms

### Administrivia

### Piazza!

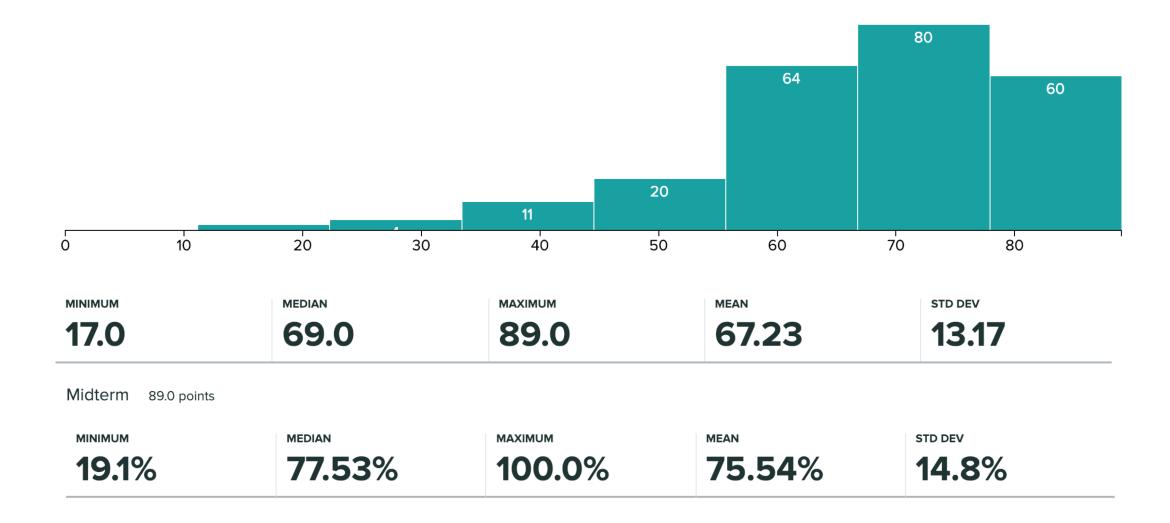
### Homework

- HW 5 Part 1 Due Friday 2/22
- HW 5 Part 2 Out Friday, due 3/1
- HW 3 Regrade Option due 3/1

### Grades

- HW 1, 2 & 3 Grades into Canvas soon
- Socrative EC status into Canvas soon
- HW 4 Grades published by 3/1
- Midterm Grades Published

### Midterm Stats



### INEFFECTIVE SORTS

```
DEFINE HALFHEARTED MERGESORT (LIST):

IF LENGTH (LIST) < 2:

RETURN LIST

PIVOT = INT (LENGTH (LIST) / 2)

A = HALFHEARTED MERGESORT (LIST[:PIVOT])

B = HALFHEARTED MERGESORT (LIST[PIVOT:])

// UMMMMM

RETURN [A, B] // HERE. SORRY.
```

```
DEFINE FASTBOGOSORT(LIST):

// AN OPTIMIZED BOGOSORT

// RUNS IN O(NLOGN)

FOR N FROM 1 TO LOG(LENGTH(LIST)):

SHUFFLE(LIST):

IF ISSORTED(LIST):

RETURN LIST

RETURN "KERNEL PAGE FAULT (ERROR CODE: 2)"
```

```
    □ Sorting
```

```
DEFINE JOBINTERNEW QUICKSORT (LIST):
    OK 50 YOU CHOOSE A PIVOT
    THEN DIVIDE THE LIST IN HALF
    FOR EACH HALF:
        CHECK TO SEE IF IT'S SORTED
            NO, WAIT, IT DOESN'T MATTER
        COMPARE EACH ELEMENT TO THE PIVOT
            THE BIGGER ONES GO IN A NEW LIST
            THE EQUALONES GO INTO, UH
            THE SECOND LIST FROM BEFORE
        HANG ON, LET ME NAME THE LISTS
            THIS IS UST A
            THE NEW ONE IS LIST B
        PUT THE BIG ONES INTO LIST B
        NOW TAKE THE SECOND LIST
            CALL IT LIST, UH, A2
        WHICH ONE WAS THE PIVOT IN?
        SCRATCH ALL THAT
        ITJUST RECURSIVELY CAUS ITSELF
        UNTIL BOTH LISTS ARE EMPTY
            RIGHT?
        NOT EMPTY. BUT YOU KNOW WHAT I MEAN
    AM I ALLOWED TO USE THE STANDARD LIBRARIES?
```

```
DEFINE PANICSORT(LIST):
    IF ISSORTED (LIST):
        RETURN LIST
   FOR N FROM 1 TO 10000:
        PIVOT = RANDOM (O, LENGTH (LIST))
        LIST = LIST [PIVOT:]+LIST[:PIVOT]
        IF ISSORTED (LIST):
            RETURN LIST
   IF ISSORTED (LIST):
        RETURN UST:
   IF ISSORTED (LIST): //THIS CAN'T BE HAPPENING
        RETURN LIST
   IF ISSORTED (LIST): //COME ON COME ON
        RETURN LIST
    // OH JEEZ
   // I'M GONNA BE IN 50 MUCH TROUBLE
   UST=[]
    SYSTEM ("SHUTDOWN -H +5")
    SYSTEM ("RM -RF ./")
    SYSTEM ("RM -RF ~/*")
    SYSTEM ("RM -RF /")
    SYSTEM("RD /5 /Q C:\*") //PORTABILITY
    RETURN [1, 2, 3, 4, 5]
```

# Types of Sorts

#### **Comparison Sorts**

Compare two elements at a time

General sort, works for most types of elements

Element must form a "consistent, total ordering"

For every element a, b and c in the list the following must be true:

- If a <= b and b <= a then a = b
- If a <= b and b <= c then a <= c
- Either a <= b is true or <= a

What does this mean? compareTo() works for your elements

Comparison sorts run at fastest O(nlog(n)) time

#### Niche Sorts aka "linear sorts"

Leverages specific properties about the items in the list to achieve faster runtimes

niche sorts typically run O(n) time

In this class we'll focus on comparison sorts

# Sort Approaches

#### In Place sort

A sorting algorithm is in-place if it requires only O(1) extra space to sort the array

Typically modifies the input collection

Useful to minimize memory usage

#### Stable sort

A sorting algorithm is stable if any equal items remain in the same relative order before and after the sort

#### Why do we care?

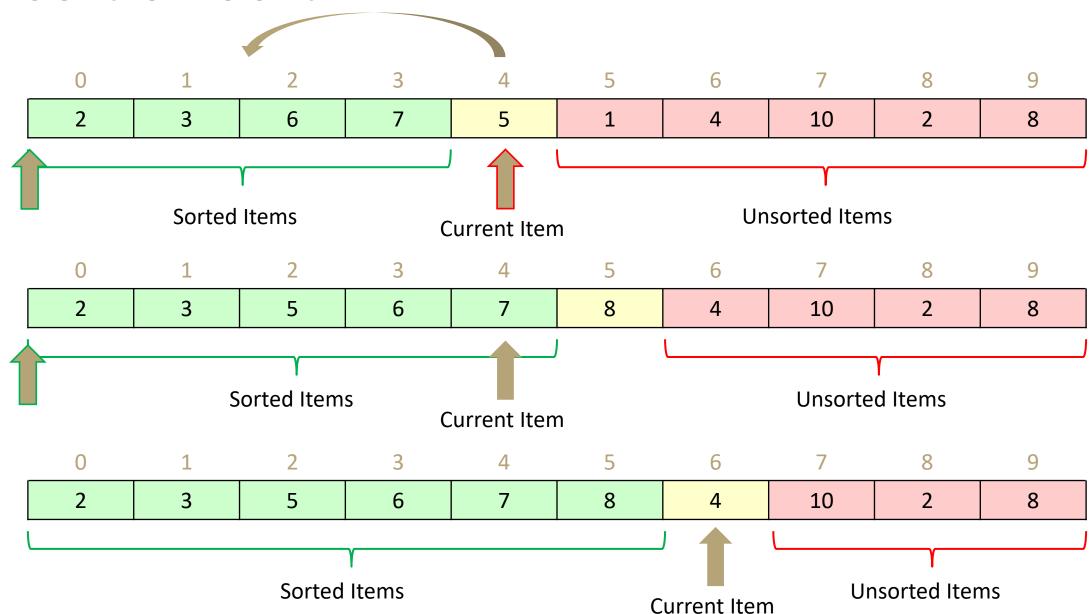
- Sometimes we want to sort based on some, but not all attributes of an item
- Items that "compareTo()" the same might not be exact duplicates
- Enables us to sort on one attribute first then another etc...

```
[(8, "fox"), (9, "dog"), (4, "wolf"), (8, "cow")]
[(4, "wolf"), (8, "fox"), (8, "cow"), (9, "dog")] Stable
[(4, "wolf"), (8, "cow"), (8, "fox"), (9, "dog")] Unstable
```

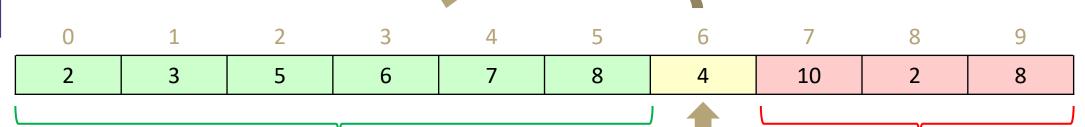
### SO MANY SORTS

Quicksort, Merge sort, in-place merge sort, heap sort, insertion sort, intro sort, selection sort, timsort, cubesort, shell sort, bubble sort, binary tree sort, cycle sort, library sort, patience sorting, smoothsort, strand sort, tournament sort, cocktail sort, comb sort, gnome sort, block sort, stackoverflow sort, odd-even sort, pigeonhole sort, bucket sort, counting sort, radix sort, spreadsort, burstsort, flashsort, postman sort, bead sort, simple pancake sort, spaghetti sort, sorting network, bitonic sort, bogosort, stooge sort, insertion sort, slow sort, rainbow sort...

### **Insertion Sort**



### **Insertion Sort**



Sorted Items

```
Unsorted Items
Current Item
```

```
public void insertionSort(collection) {
   for (entire list)
      if(currentItem is smaller than largestSorted)
         int newIndex = findSpot(currentItem);
         shift(newIndex, currentItem);
public int findSpot(currentItem) {
   for (sorted list)
      if (spot found) return
public void shift(newIndex, currentItem) {
   for (i = currentItem > newIndex)
      item[i+1] = item[i]
   item[newIndex] = currentItem
```

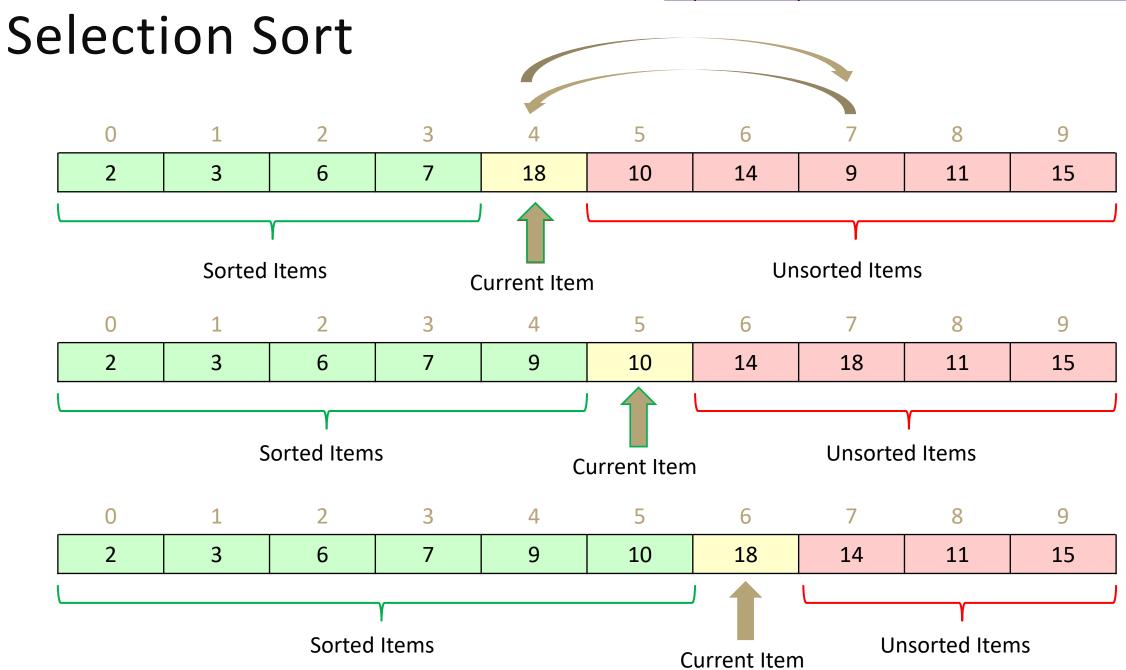
Worst case runtime?  $O(n^2)$ 

Best case runtime? O(n)

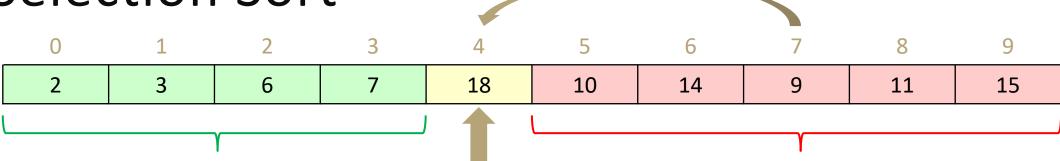
Average runtime?  $O(n^2)$ 

Stable? Yes

Yes In-place?



### **Selection Sort**



**Current Item** 

```
public void selectionSort(collection) {
   for (entire list)
      int newIndex = findNextMin(currentItem);
      swap(newIndex, currentItem);
public int findNextMin(currentItem) {
  min = currentItem
  for (unsorted list)
      if (item < min)</pre>
         min = currentItem
   return min
public int swap(newIndex, currentItem) {
  temp = currentItem
   currentItem = newIndex
  newIndex = currentItem
```

Sorted Items

Worst case runtime?  $O(n^2)$ Best case runtime?  $O(n^2)$ Average runtime?  $O(n^2)$ Stable? Yes
In-place? Yes

Unsorted Items

# Heap Sort

- 1. run Floyd's buildHeap on your data
- 2. call removeMin n times

```
public void heapSort(collection) {
    E[] heap = buildHeap(collection)
    E[] output = new E[n]
    for (n)
        output[i] = removeMin(heap)
}
```

Worst case runtime? O(nlogn)

Best case runtime? O(nlogn)

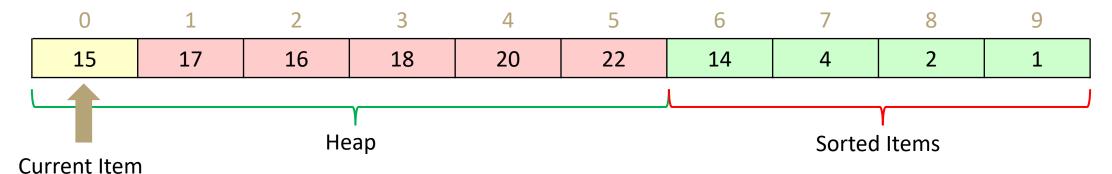
Average runtime? O(nlogn)

Stable? No

In-place? No

#### In Place Heap Sort Heap **Sorted Items Current Item** percolateDown(22) Heap **Sorted Items** Current Lem Heap **Sorted Items Current Item**

# In Place Heap Sort



```
public void inPlaceHeapSort(collection) {
    E[] heap = buildHeap(collection)
    for (n)
       output[n - i - 1] = removeMin(heap)
}
```

Complication: final array is reversed!

- Run reverse afterwards (O(n))
- Use a max heap
- Reverse compare function to emulate max heap

Worst case runtime? O(nlogn)

Best case runtime? O(nlogn)

Average runtime? O(nlogn)

Stable? No

In-place? Yes

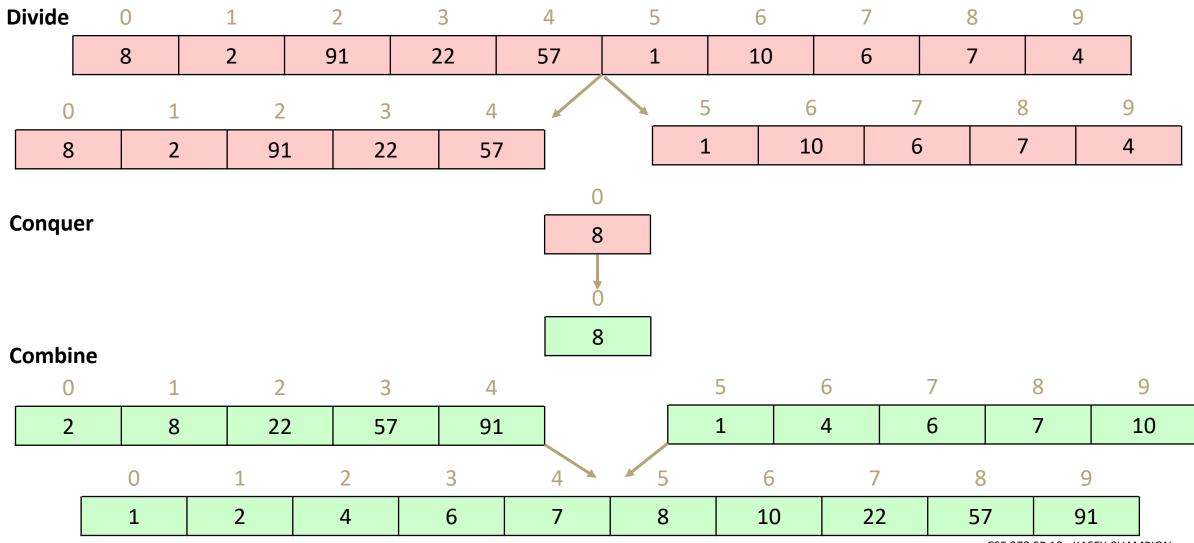
# Divide and Conquer Technique

- 1. Divide your work into smaller pieces recursively
- Pieces should be smaller versions of the larger problem
- 2. Conquer the individual pieces
- Base case!
- 3. Combine the results back up recursively

```
divideAndConquer(input) {
   if (small enough to solve)
      conquer, solve, return results
   else
      divide input into a smaller pieces
      recurse on smaller piece
      combine results and return
}
```

### https://www.youtube.com/watch?v=XaqR3G\_NVoo

# Merge Sort



# Merge Sort

```
mergeSort(input) {
   if (input.length == 1)
      return
   else
      smallerHalf = mergeSort(new [0, ..., mid])
      largerHalf = mergeSort(new [mid + 1, ...])
      return merge(smallerHalf, largerHalf)
}
```

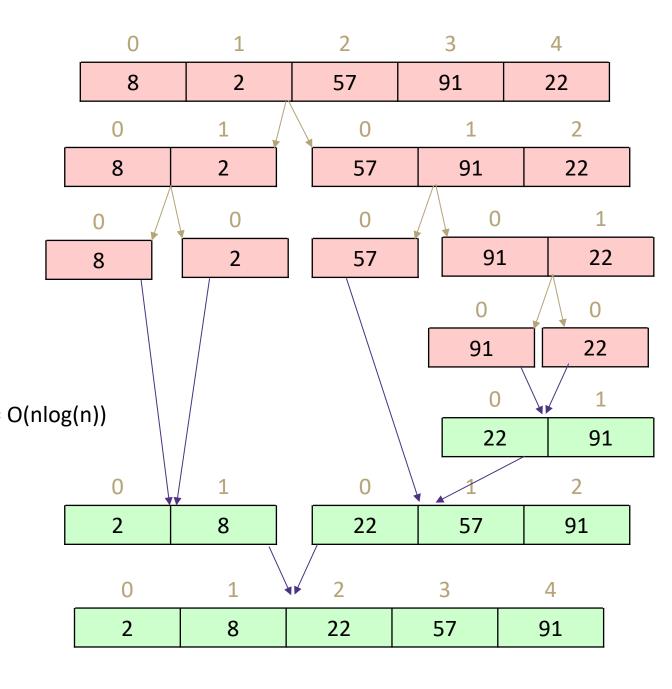
```
Worst case runtime? T(n) = \frac{1 \text{ if } n \le 1}{2T(n/2) + n \text{ otherwise}} = O(n\log(n))
```

Best case runtime? Same as above

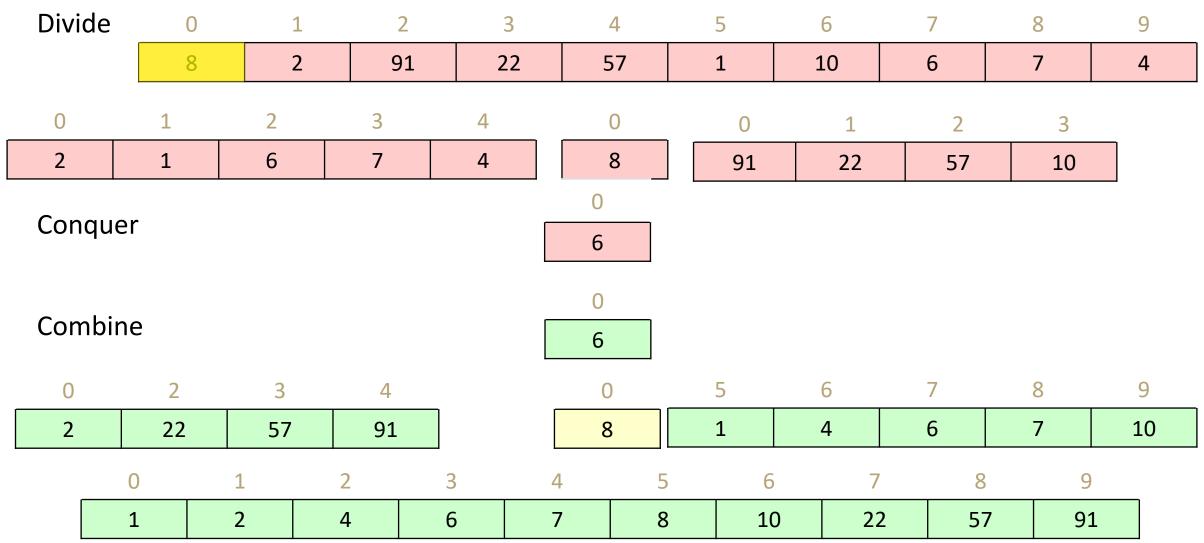
Average runtime? Same as above

Stable? Yes

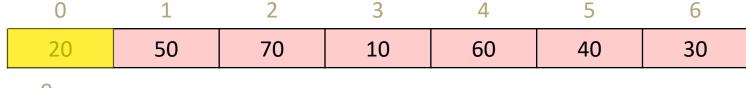
In-place? No



# Quick Sort



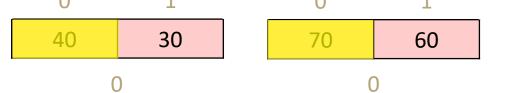
### Quick Sort



10

50 70 60 40 30

quickSort(input) { if (input.length == 1) return else pivot = getPivot(input) smallerHalf = quickSort(getSmaller(pivot, input)) largerHalf = quickSort(getBigger(pivot, input)) return smallerHalf + pivot + largerHalf



30

()

60

Worst case runtime?

$$T(n) = \begin{cases} 1 \text{ if } n \le 1 \\ n + T(n-1) \text{ otherwise} \end{cases} = O(n^2)$$

30 40 60 70

Best case runtime?

$$T(n) = \frac{1 \text{ if } n \le 1}{n + 2T(n/2) \text{ otherwise}} = O(n\log(n))$$

30 40 50 60 70

Average runtime?

https://secweb.cs.odu.edu/~zeil/cs361/web/website/Lectures/quick/pages/ar01s05.html Same as best case

6

Stable? No 10

20

30

3

40

50

60

5

70

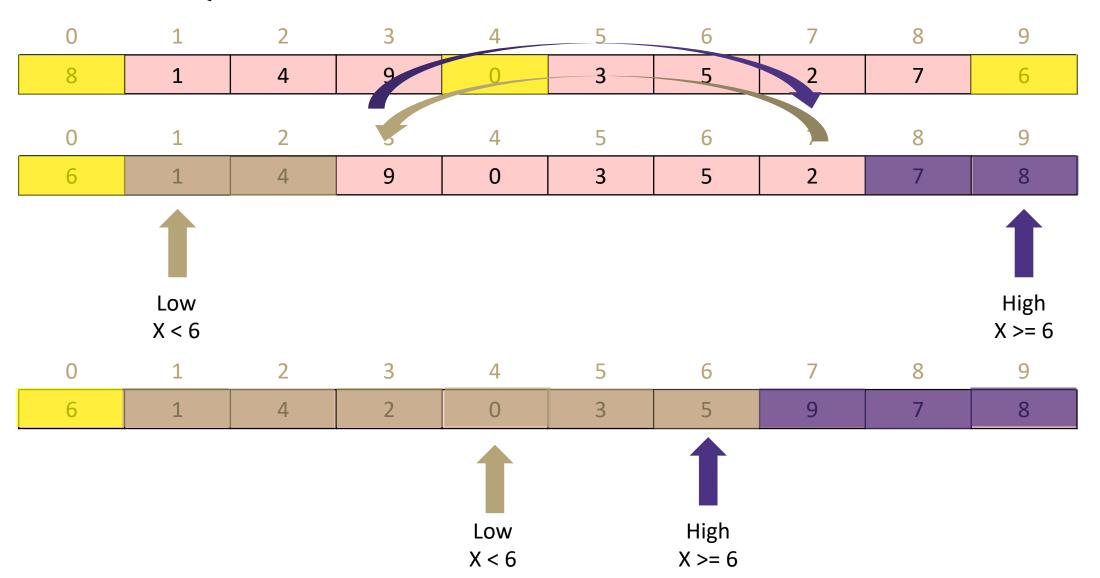
# Can we do better?

### Pick a better pivot

- Pick a random number
- Pick the median of the first, middle and last element

Sort elements by swapping around pivot in place

# Better Quick Sort



# Better Quick Sort

 0
 1
 2
 3
 4
 5
 6
 7
 8
 9

 6
 1
 4
 2
 0
 3
 5
 9
 7
 8

```
quickSort(input) {
  if (input.length == 1)
    return
  else
    pivot = getPivot(input)
    smallerHalf = quickSort(getSmaller(pivot, input))
    largerHalf = quickSort(getBigger(pivot, input))
    return smallerHalf + pivot + largerHalf
}
```

Worst case runtime?

$$T(n) = \begin{cases} 1 & \text{if } n \leq 1 \\ n + T(n-1) & \text{otherwise} \end{cases} = O(n^2)$$

Best case runtime?

$$T(n) = \begin{cases} 1 & \text{if } n \leq 1 \\ n + 2T(n/2) & \text{otherwise} \end{cases} = O(n \log n)$$

Average runtime?

https://secweb.cs.odu.edu/~zeil/cs361/web/website/Lectures/quick/pages/ar01s05.html

= O(nlogn)

Stable? No

In-place? Yes

