

Wednesday, 18 Jan 2023

10 points total.

Name: _____

UID: _____

1. (10 points) Consider the following signal:

$$x[n] = \sin\left(\frac{\pi}{3}n + \frac{\pi}{6}\right).$$

Write out the proof of whether $y[n]$ is periodic or not. If yes it is periodic, please also include the fundamental period:

(a) $y[n] = x[n + 5]$

(b) $y[n] = x\left[\frac{n}{3}\right]$

Solution:

The fundamental period N for $x[n]$ should be 6 (Simply apply $\frac{2\pi}{N} = \frac{\pi}{3}$).

(a) Yes, $y[n + 6] = x[n + 6 + 5] = x[n + 5] = y[n]$, so the fundamental period $N_y = 6$.

(b) Yes, $y[n + N_y] = x\left[\frac{1}{3}(n + N_y)\right] = x\left[\frac{1}{3}n + \frac{1}{3}N_y\right]$, if periodic, $\frac{1}{3}N_y = 6$, so $N_y = 18$. Also, you can think as follows: $y[n]$ is actually up-sampling (expand) $x[n]$ by 3, so correspondingly, $N_y = 3N = 18$.