### CSE 410: Assignment 2 (Jan 2023) Raster Based Graphics Pipeline

### **Change log:**

• [8 July 2023, 2:00 PM] New sentence in the description of stage 1. Page 3.

### Overview:

In this assignment, you will develop the raster-based graphics pipeline used in OpenGL. The pipeline can be thought of as a series of six stages. Yu will implement roughly 4 stages of the pipeline.

- 1. Stage 1: modeling transformation
- 2. Stage 2: view transformation
- 3. Stage 3: projection transformation
- 4. Stage 4: clipping & scan conversion using Z-buffer algorithm

Your program will output four files: stage1.txt, stage2.txt, stage3.txt and out.bmp. The first three files will contain the output of the first three stages, respectively. The fourth file will be a bmp image generated by the pipeline.

Three will be two input files: scene.txt and config.txt

The first file will contain the scene description and second file will contain the necessary information for Z-buffer algorithm.

## Scene description:

You will be given a text file named "scene.txt". This will contain the following lines:

```
Line 1: eyeX eyeY eyeZ
Line 2: lookX lookY lookZ
Line 3: upX upY upZ
Line 4: fovY aspectRatio near far
```

Lines 1-3 of scene.txt state the parameters of the <code>gluLookAt</code> function and Line 4 provides the <code>gluPerspective</code> parameters.

The display code contains 7 commands as follows:

1. triangle command – this command is followed by three lines specifying the coordinates of the three points of the triangle to be drawn. The points being p1, p2, and p3, 9 double values, i.e., p1.x, p1.y, p1.z, p2.x, p2.y, p2.z, p3.x, p3.y, and p3.z indicate the coordinates.

This is equivalent to the following in OpenGL code.

```
glBegin(GL_TRIANGLE);{
    glVertex3f(p1.x, p1.y, p1.z);
    glVertex3f(p2.x, p2.y, p2.z);
    glVertex3f(p3.x, p3.y, p3.z);
}glEnd();
```

- 2. translate command this command is followed by 3 double values (tx, ty, and tz) in the next line indicating translation amounts along X, Y, and Z axes. This is equivalent to glTranslatef(tx, ty, tz) in OpenGL.
- 3. scale command this command is followed by 3 double values (sx, sy, and sz) in the next line indicating scaling factors along X, Y, and Z axes. This is equivalent to glscalef(sx, sy, sz) in OpenGL.
- 4. rotate command this command is followed by 4 double values in the next line indicating the rotation angle in degree (angle) and the components of the vector defining the axis of rotation (ax, ay, and az). This is equivalent to glRotatef (angle, ax, ay, az) in OpenGL.
- 5. push command This is equivalent to glPushMatrix in OpenGL.
- 6. pop command This is equivalent to glPopMatrix in OpenGL.
- 7. end command This indicates the end of the display code.

In this assignment, you will generate the output of the first three stages of the raster-based graphics pipeline according to the scene description provided in scene.txt file. The output of the stages should be put in stage1.txt, stage2.txt, and stage3.txt file.

Please check the scene.txt carefully to have a more comfortable understanding of the input.

## Stage 1: Modeling Transformation

In the Modeling transformation phase, the display code in scene.txt is parsed, the transformed positions of the points that follow each triangle command are determined, and the transformed coordinates of the points are written in stage1.txt file. We maintain a stack S of transformation matrices which is manipulated according to the commands given in the display code. We also have to maintain a matrix M which stores the current state of transformation. The transform closest to the object gets multiplied first. The pseudo-code for the modeling transformation phase is as follows:

```
initialize empty stack S
initialize M = Identity matrix
while true
       read command
       if command = "triangle"
            read three points
            for each three-point P
                    P' <- transformPoint(M, P)
                    output P'
       else if command = "translate"
             read translation amounts
             generate the corresponding translation matrix T
             M = product(M, T)
       else if command = "scale"
            read scaling factors
             generate the corresponding scaling matrix T
             M = product(M, T)
       else if command = "rotate"
             read rotation angle and axis
             generate the corresponding rotation matrix T
             M = product(M, T)
       else if command = "push"
             S.push(M)
       else if command ="pop"
            // do it yourself
       else if command ="end"
            break
```

#### **Transformation matrix for Translation**

```
translate
tx ty tz
```

The transformation matrix for the above translation is as follows:

```
1 0 0 tx
0 1 0 ty
0 0 1 tz
0 0 0 1
```

### **Transformation matrix for Scaling**

```
scale
sx sy sz
```

The transformation matrix for the above scaling is as follows:

#### **Transformation matrix for Rotation**

Remember that, the columns of the rotation matrix indicate where the unit vectors along the principal axes (namely, i, j, and k) are transformed. We will use the vector form of Rodrigues formula to determine where i, j, and k are transformed and use those to generate the rotation matrix. The vector form of Rodrigues formula is as follows:

$$R(\vec{x}, \vec{a}, \theta) = \cos \theta \, \vec{x} + (1 - \cos \theta)(\vec{a} \cdot \vec{x})\vec{a} + \sin \theta \, (\vec{a} \times \vec{x})$$

In the above formula,  $\vec{a}$  is a unit vector defining the axis of rotation,  $\theta$  is the angle of rotation, and  $\vec{x}$  is the vector to be rotated.

Now we outline the process of generating transformation matrix for the following rotation:

```
rotate
angle ax ay az
```

We denote the vector (ax, ay, az) by a. The steps to generate the rotation matrix are as follows:

```
a.normalize()
c1=R(i,a,angle)
c2=R(j,a,angle)
c3=R(k,a,angle)
```

The corresponding rotation matrix is given below:

### **Managing Push and Pop**

The following table demonstrates how push and pop works. The state of the transformation matrix stack after execution of each line of the code in the left is shown in the right. Design a data structure that manages push and pop operations on the transformation matrix stack accordingly.

	Stack (S) State after Lines												
Code	0	1	2	3	4	5	6	7	8	9	10	11	
1.Push													
2.Translate1													
3.Push													
4.Rotate1													
5.Pop													
6.Scale1					•			•	•				
7.Push													
8.Rotate <sub>2</sub>													
9.Pop													
10.Scale2				T1	T1			T1S1	T1S1				
11.Pop		I	I	I	I	I	I	I	I	I	I		
	-	Transformation Matrix (M) State after Lines											
	I	I	T1	T1	T1R1	T1	T1S1	T1S1	T1S1R2	T1S1	T1S1S2	Ι	

# Stage 2: View Transformation

In the view transformation phase, the gluLookAt parameters in scene.txt is used to generate the view transformation matrix V, and the points in stage1.txt are transformed by V and written in stage2.txt. The process of generating V is given below.

First determine mutually perpendicular unit vectors 1, r, and u from the gluLookAt parameters.

```
l = look - eye
l.normalize()
r = l X up
r.normalize()
u = r X l
```

Apply the following translation T to move the eye/camera to origin.

```
1 0 0 -eyeX
0 1 0 -eyeY
0 0 1 -eyeZ
0 0 0 1
```

Apply the following rotation R such that the 1 aligns with the -Z axis, r with X axis, and u with Y axis. Remember that, the rows of the rotation matrix contain the unit vectors that align with the unit vectors along the principal axes after transformation.

Thus the view transformation matrix *V=RT*.

## Stage 3: Projection Transformation

In the projection transformation phase, the gluPerspective parameters in scene.txt are used to generate the projection transformation matrix P, and the points in stage2.txt are transformed by P and written in stage3.txt. The process of generating P is as follows:

First compute the field of view along X (fovX) axis and determine r and t.

```
fovX = fovY * aspectRatio
t = near * tan(fovY/2)
r = near * tan(fovX/2)
```

The projection matrix *P* is given below:

```
near/r 0 0 0 0
0 near/t 0 0 0
0 0 -(far+near)/(far-near) -(2*far*near)/(far-near)
0 0 -1 0
```

Refer to [1] for understanding the 3<sup>rd</sup> row of the above projection matrix. Image source: [2].

## Stage 3: Clipping & scan conversion using Z-buffer algorithm

To be declared

#### Do's and Don'ts

- 1. Use homogeneous coordinates. The points should be represented by 4\*1 matrices and transformations by 4\*4 matrices.
- 2. While transforming a homogeneous point by multiplying it with a transformation matrix, don't forget to scale the resultant point such that the w coordinate of the point becomes 1.
- 3. Do not use the matrix form of Rodrigues formula directly to generate the rotation matrix. Use the procedure shown above that uses the vector form of Rodrigues formula.
- 4. Do not specify <code>gluLookAt</code> parameters in <code>scene.txt</code> such that the looking direction, i.e., <code>look-eye</code>, becomes parallel to the up direction.
- 5. Make sure that the model is situated entirely in front of the near plane.

#### Reference

- [1] http://www.songho.ca/opengl/gl\_projectionmatrix.html
- [2] http://www.opengl-tutorial.org/beginners-tutorials/tutorial-3-matrices/