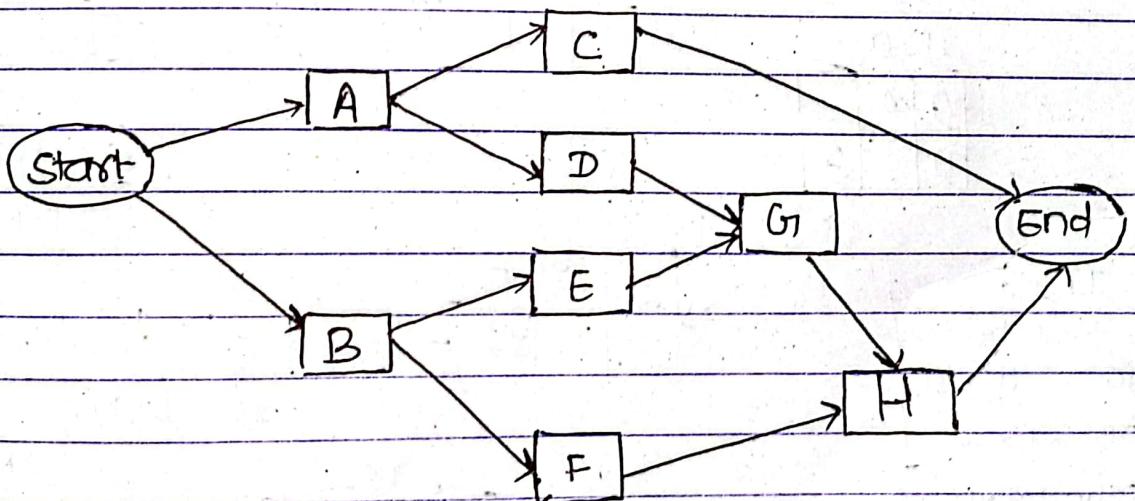
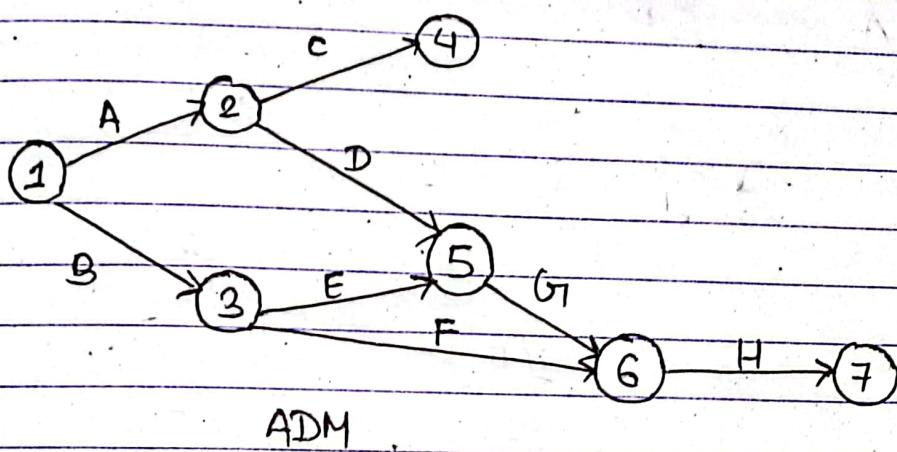


ICT-PN

Q) Generate the Network Diagram for the following data:

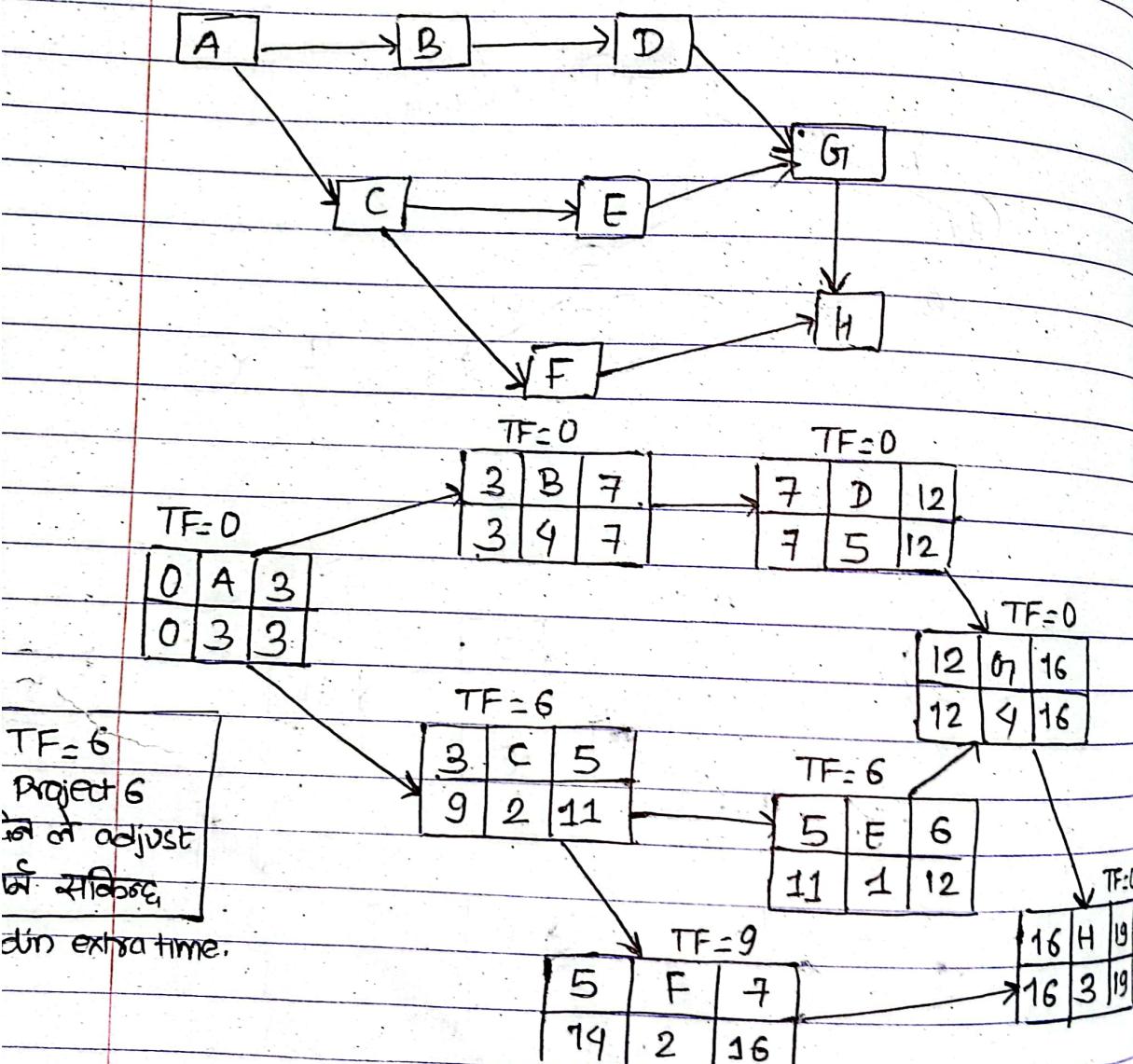
Activities	Predecessors
A	--
B	--
C	A
D	A
E	B
F	B
G	D,E
H	F,G



PDM

Act	predecessor	Duration (days)
A	-	3
B	A	4
C	A	2
D	B	5
E	C	1
F	C	2
G	D,E	9
H	F,G	3

Calculate the earliest duration of project completion.



$$A-B-D-G-H = 3+4+5+4+3 = 19$$

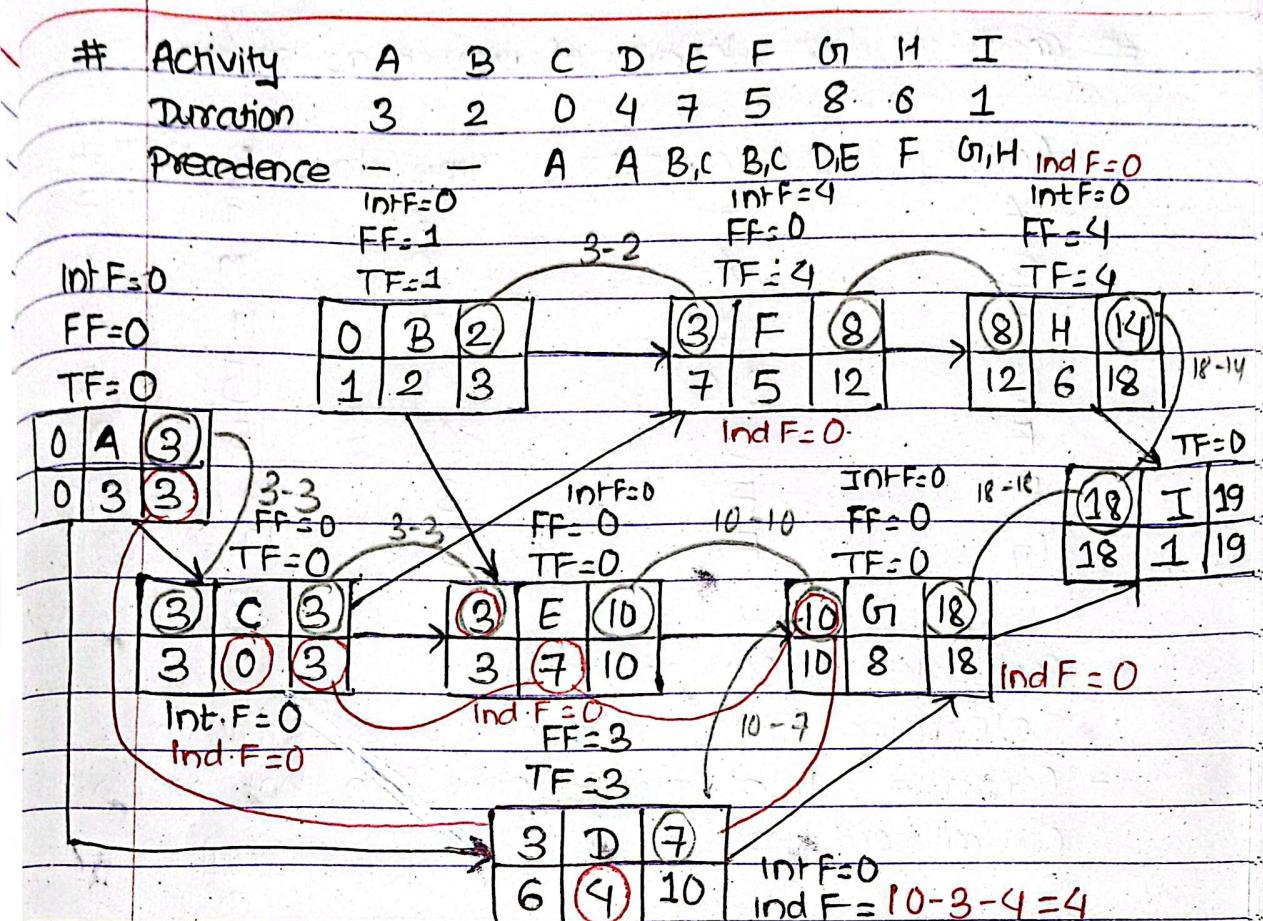
$$A-C-E-G-H = 3+2+1+4+3 = 13 \quad \text{Total float (TF)}$$

$$A-C-F-H = 3+2+2+3 = 10$$

$$TF = LF - EF$$

$$TF = LS - ES$$

Total Float: कुनै एक activity maximum कति दिलाये दिनो तर्फ
सकिए, without affecting the project completion time.



$$A-C-F-H-I = 3+0+5+6+1 = 15$$

$$A-D-G_1-I = 3+4+8+1 = 16$$

$$B-F-H-I = 2+5+6+1 = 14$$

$$B-E-G_1-I = 2+7+8+1 = 18$$

$$A-C-E-G_1-I = 3+0+7+8+1 = 19$$

$$\text{Free Float (FF)} = \min(\text{ES}_i + i) - \text{EF}_i$$

$$\text{Int. F}_i = \text{TF}_i - \text{FF}_i \quad (\text{Interfering float})$$

$$\text{Ind. F}_i = \min(\text{ES}_i + 1) - \max(\text{LF}_{i-1}) - \text{Duration}$$

Act	D	ES	EF	LS	LF	TF	FF	Int. F	Ind F
A	3	0	3	0	3	0	0	0	0
B	2	0	2	1	3	1	1	0	0
C	0	3	3	3	3	0	0	0	0
D	4	3	7	6	10	3	3	0	4
E	7	3	10	3	10	0	0	0	0
F	5	3	8	7	12	4	0	4	0
G ₁	8	10	18	10	18	0	0	0	0
H	6	8	14	12	18	4	4	0	0
I	1	10	19	18	19	0	0	0	0

$$EF = ES + D$$

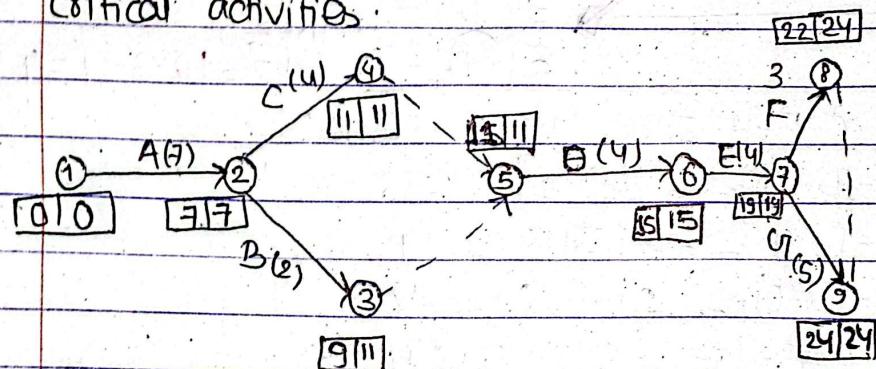
$$LS = LF - D$$

AOA

Consider the details of project as shown:

Activity	Predecessors	Time (days)	ES	LS	EF	LF	TF	FF
A	-	7	0	0	7	7	0	0
B	A	2	7	9	9	11	2	2
C	A	4	11	11	11	11	0	0
D	B, C	4	15	15	15	15	0	0
E	D	4	15	19	19	19	4	4
F	E	3	19	21	21	24	2	2
G	E	5	19	24	24	24	5	5

- Construct a CPM network.
- Determine critical path and project completion time.
- Compute total float and free float for non critical activities.



$$1-2-4-5-6-7-8-9 = 7+4+3+7+4+4+4+3 = 22$$

$$1-2-4-5-6-7-9 = 7+4+4+4+5 = 24$$

$$1-2-3-5-6-7-8-9 = 7+2+4+4+3 = 20$$

$$1-2-3-5-6-7-9 = 7+2+4+4+5 = 22$$

Activity	ES	LS	EF	LF	TF	FF	ES _i	LF _j
A	0	0	7	7	0	0	ES _i = Early Start time (tail event)	
B	7	9	9	11	2	2		
C	7	7	11	11	0	0	LF _j = Late Finish time (head event)	
D	11	11	15	15	0	0		
E	15	15	19	19	0	0	FF = TF - ES _i (slack of head event)	
F	19	21	22	24	2	2		
G	19	19	24	24	0	0	Slack time for each activity \Rightarrow TF \Rightarrow LS - ES or LF - EF	

PERT

- t_0

- t_p

- t_m

t_0

$$\Delta = t_0 + t_p + t_m$$

3

$$\beta = \frac{t_0 + 4t_m + t_p}{6}$$

6

$$V = \left(\frac{t_p - t_0}{6} \right)^2$$

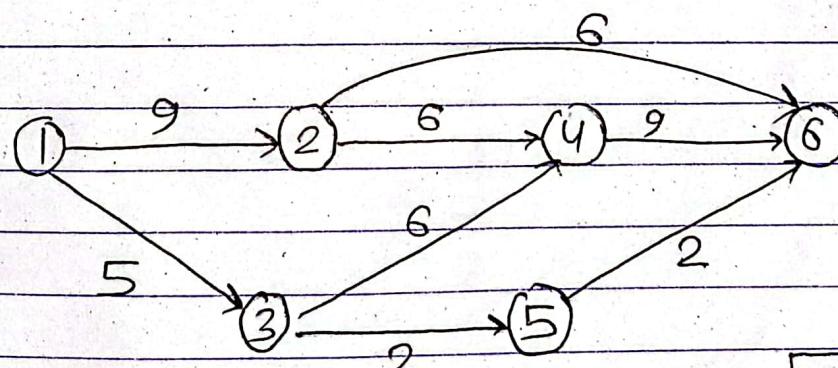
$$S.D = \sqrt{V_1 + V_2 + V_3 + V_4}$$

where (V_1, V_2, V_3, \dots are the variance of critical activities).

process

total estimation.

activities	t_0	t_m	t_p	t_e	\checkmark	Remarks
1-2	6	9	12	9	1	C.P
1-3	3	4	11	5	1.78	
2-4	2	5	14	6	4	C.P
3-4	4	6	8	6	0.44	
3-5	1	1.5	5	2	0.44	
2-6	5	6	7	5.6	0.11	
4-6	7	8	15	9.5	1.78	C.P
5-6	1	2	3	2	0.11	



$$S.D = \sqrt{V_1 + V_3 + V_7}$$

$$P_1 = 1-2-6 = 15$$

$$= \sqrt{1+4+1.78}$$

$$P_2 = 1-2-4-6 = 24 \quad | \text{ C.P.}$$

$$= 2.60$$

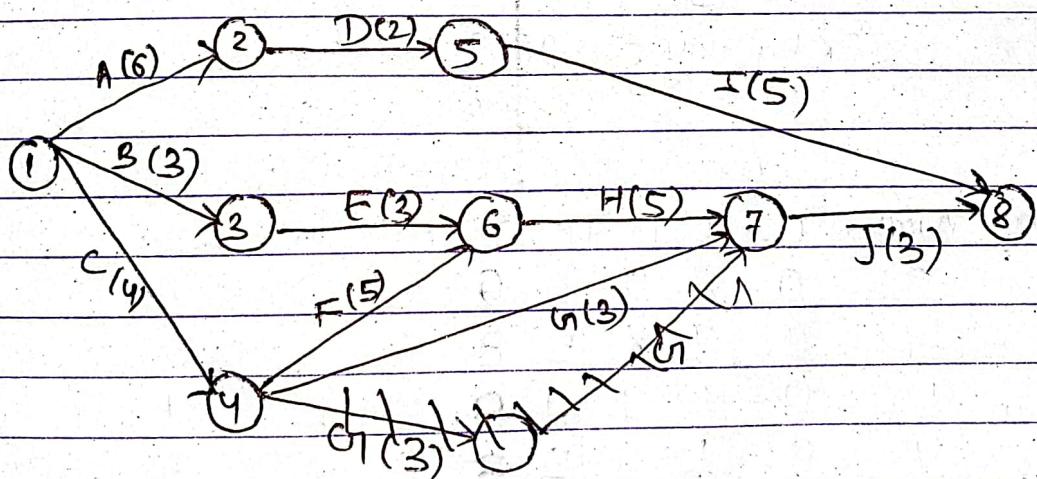
$$P_3 = 1-3-5-6 = 9$$

$$P_4 = 1-3-4-6 = 20$$

For the given project with following details:

- Find the expected duration and variance of each activity.
- Find the critical path and expected project completion time.
- Find the probability of completing the project on or before 22 weeks?

Activity	Predecessor	Opt time (to)	most lik. time (tm)	Pessimistic time (tp)	Exp. duration	Variance
A	-	5	6	7	6	0.11
B	-	1	3	5	3	0.44
C	-	1	4	7	4	1
D	A	1	2	3	2	0.11
E	B	1	2	9	3	1.78
F	C	1	5	9	5	1.78
G	C	2	2	8	3	1
H	E, F	4	4	10	5	1
I	D	2	5	8	5	1
J	H, G	2	2	8	3	1



$$P_1 = A - D - I = 6 + 2 + 5 = 13$$

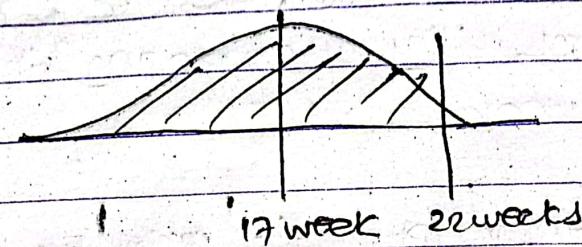
$$P_2 = B - E - H - J = 3 + 3 + 5 + 3 = 14$$

$$P_3 = C - F - H - J = 4 + 5 + 5 + 3 = 17$$

$$P_4 = C - F - G - J = 4 + 3 + 3 = 10$$

Ind.F = FF - Si

Expected project completion time
 $t_e = 17 \text{ weeks}$



$$Z = X - t_e \\ \text{s.d}$$

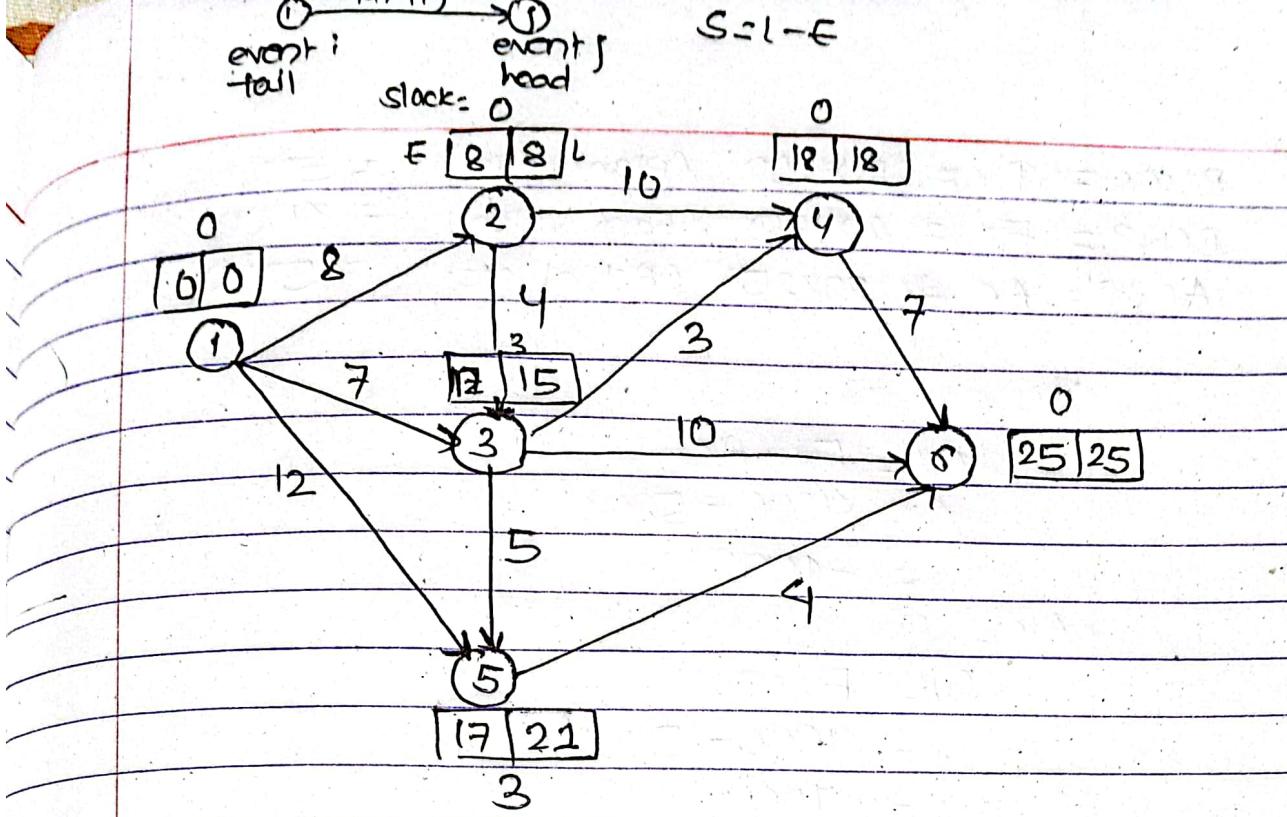
$$\text{s.d} = \sqrt{1^2 + 1.78^2 + 1^2 + 1^2} \\ = 2.18$$

$$Z = 22 - 17 \\ 2.18 \\ = 2.18 = 2.28$$

From Z table

$$\text{Probability} = 0.9887 \\ = 98.87\%$$

Activity	Duration	<u>ES+D</u>		TF-SH		FF-SI		TF-FF	
		ES	EF	LS	LF	TF	FF	Ind.F	Int.F
0-1-2	8	0	8	0	8	0	0	0	0
0-1-3	3	7	0	7	8	15	8	5	5
0-1-5	4	12	0	12	9	21	9	5	5
0-2-3	3	4	8	12	11	15	3	0	3
0-2-4	6	10	8	18	8	18	0	0	0
0-3-4	3	3	12	15	15	18	3	3	0
0-3-5	5	5	12	17	16	21	5	0	-3
0-3-6	6	10	12	22	15	25	3	3	0
0-4-6	7	7	18	25	18	25	0	0	0
0-5-6	4	4	17	21	21	25	4	4	0



Control costs: Tools and Techniques:

Earned Value Management (EVM / EVA) Analysis:

PV: Plan value: budgeted value. Work_P cost_P

AC: Actual cost: Work_A cost_A

SV: Schedule variance: $EV - PV \rightarrow SV \leftarrow EV \text{ बढ़े } PV \text{ बढ़े}$

CV: Cost variance: $EV - AC \rightarrow CV \text{ +ve } \rightarrow EV \text{ अच्छा काम हो } AC \text{ बढ़ी काम बड़ी} \\ CV \text{ -ve } \rightarrow EV \text{ अच्छा काम हो } AC \text{ घटी काम बड़ी} \\ \text{परसा अनुसार काम गएगा।}$

SPI: Scheduled Performance Index = $\frac{EV}{PV} > 1$

CPI: Cost performance Index = $\frac{EV}{AC} > 1$

Example:

50 units of plantation have to be done in two weeks period. Per unit cost of plantation is estimated at Rs 200 of which progress monitoring was done one week after the work was started. Only 40% work was found completed and the account record showed that the actual expenditure (cost) for plantation per unit was Rs 250.

Compute: PV, EV, AC, SV, CV, SPI & CPI.

$$\begin{aligned}
 BCWS &= PV = 25 \times 200 \quad (\text{Plan value}) & = 5000 \\
 BCWP &= EV = 20 \times 200 \quad (\text{Earned value}) & = 4000 \\
 ACWP &= AC \Rightarrow 20 \times 250 \quad (\text{Actual cost}) & = 5000
 \end{aligned}$$

NOW,

$$\begin{aligned}
 CV &= EV - AC \\
 &= 4000 - 5000 \\
 &= -1000
 \end{aligned}$$

ALCO,

$$\begin{aligned}
 SV &= EV - PV \\
 &= 4000 - 5000 \\
 &= -1000
 \end{aligned}$$

$$CPI = \frac{EV}{AC} = \frac{4000}{5000} = 0.8$$

$$SPI = \frac{EV}{PV} = \frac{4000}{5000} = 0.8$$

S-curve:

TCP I : To complete performance index

BAC : Budget at completion. $BAC = 50 \times 200 = 10,000$

VAC : Variance at completion.

EAC : Earned at completion. $EAC = \frac{BAC}{0.8} \Rightarrow \frac{10000}{0.8} = 12,500$

ETC : Estimate to complete $\Rightarrow EAC - AC \Rightarrow 12,500 - 5000 = 7000$

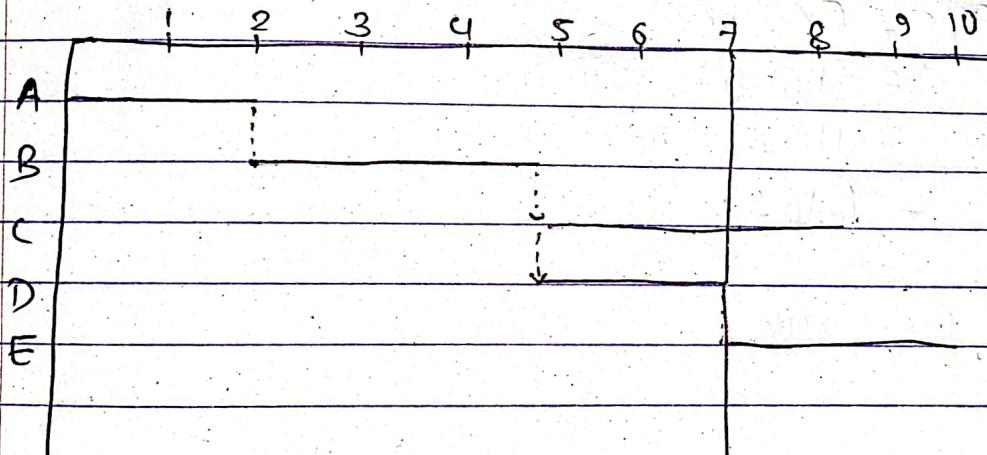
2021 - spring :

$$\Sigma \text{Total cost} = \text{BAC}$$

Activity	Predecessor	Duration (days)	Cost / day	Total cost
A	-	2	300	600
B	A	3	400	1200
C	B	3	400	1200
D	B	2	200	400
E	D	3	100	300

After 7th day, field report says something like below.

Activity	Actual % complete	Incurred cost.
A	100	600
B	100	1400
C	33	500
D	50	200
E	0	0



incurred cost.

(%)

EV = Actual work x budgeted value.

Act	pred	Dur	PV	EV	AC	
A	-	2	600	600	600	
B	A	3	1200	1200	1400	
C	B	3	800	400	500	
D	B	2	400	200	200	
E	D	3	0	0	0	
			3000	2400	2700	

$$\begin{aligned}CV &= EV - AC \\&= 2400 - 2700 \\&= -300\end{aligned}$$

$$\begin{aligned}SV &= EV - PV \\&= 2400 - 3000 \\&= -600\end{aligned}$$

$$CPI = \frac{EV}{AC} = \frac{2400}{2700} = 0.889$$

$$SPI = \frac{EV}{PV} = \frac{2400}{3000} = 0.8$$

$$BAC = 3700$$

$$EAC = \frac{BAC}{CPI} = \frac{3700}{0.889} = 4161.97 = 4162.$$

$$\begin{aligned}ETC &= EAC - AC \\&= 4161.97 - 2700 \\&= 4162 - 2700 \\&= 1462.\end{aligned}$$

* 7 - basic rule: