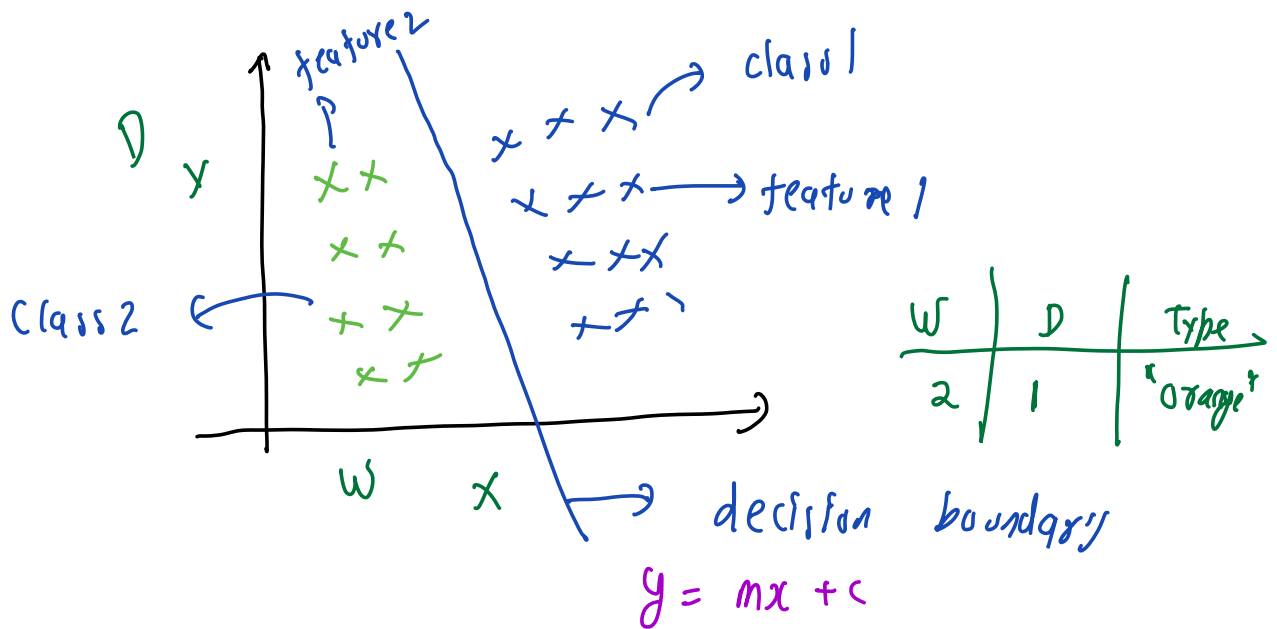


will start at 7:05 am



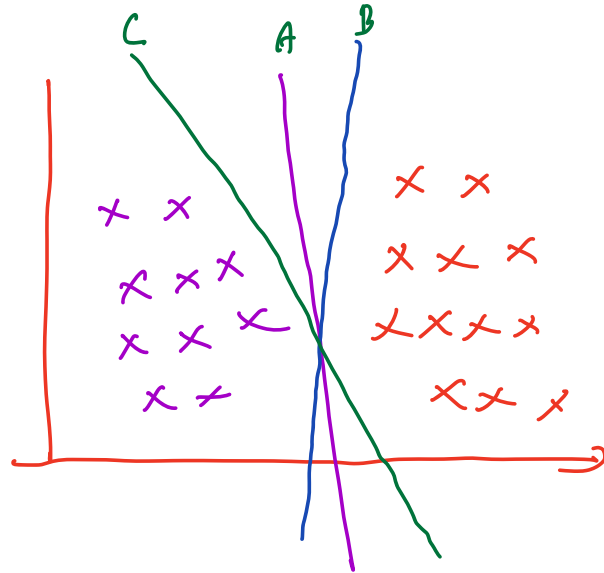
Linear Algebra 2



Classification

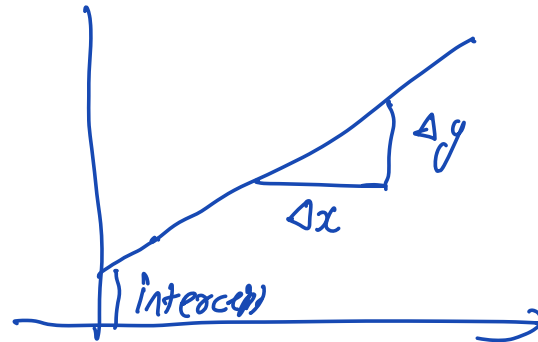
Q \Rightarrow

Decision Boundary ?



$$y = mx + c$$

$$m = \frac{\Delta y}{\Delta x}$$



Q \Rightarrow Find the value of m if $y = mx + c$ is parallel to $0.5y - x = 0$

$$0.5y = x$$

$$y = \frac{+0.2}{0.5}x$$

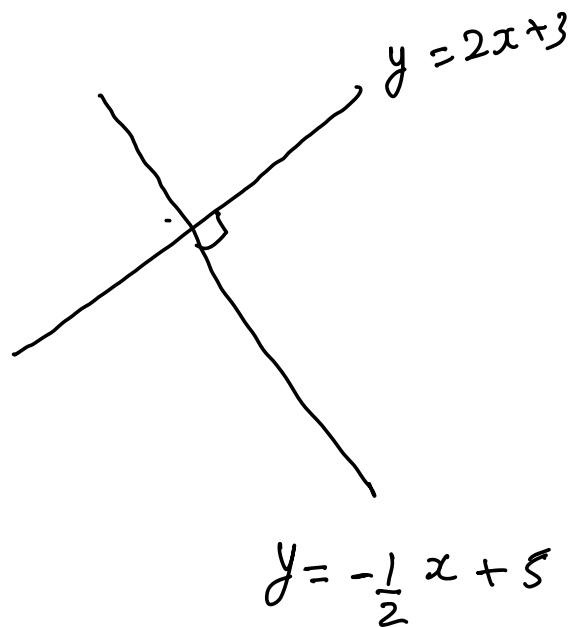
$$y = 2x + 0$$

$$m = 2$$

⇒ Perpendicular line

$$m_1 \cdot m_2 = -1$$

$$m_2 = -\frac{1}{m_1}$$



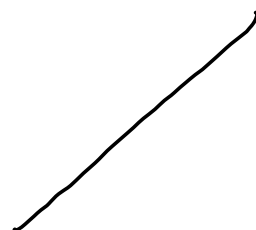
① $y = mx + c$

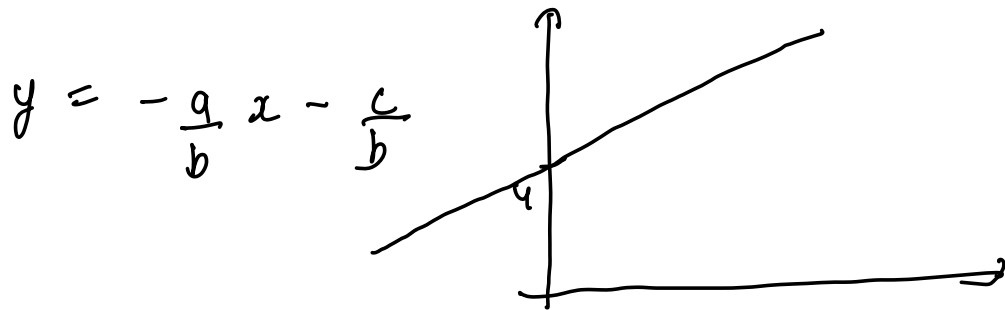
$$mx - y + c = 0$$

② $ax + by + c = 0$

$$2x + 3y + 4 = 0$$

$$by = -ax - c$$





$$2x + 3y + 4 = 0$$

$$3y = -2x - 4$$

$$y = -\frac{2}{3}x - \frac{4}{3}$$

Q \Rightarrow What is the slope & intercept of
 $3x + 2y + 5 = 0$

$$2y = -3x - 5$$

$$y = -\frac{3}{2}x - \frac{5}{2}$$

$$ax + by + c = 0$$

$$w_1 x + w_2 y + w_0 = 0 \Rightarrow \text{line}$$

$$w_1 x_1 + w_2 x_2 + w_3 z + w_0 = 0 \Rightarrow \text{plane}$$

$$w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_n x_n + w_0 = 0$$

\Downarrow
hyperplane

\Rightarrow vector

$$\begin{bmatrix} A \\ B \\ C \\ D \end{bmatrix} \Rightarrow [A \ B \ C \ D] x$$

$$w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_n x_n + w_0 = 0$$

$$\begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{bmatrix}_{n \times 1} = \vec{w} \quad \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{bmatrix}_{n \times 1} = \vec{x}$$

$\vec{w} \in \mathbb{R}^n$ \Downarrow Transpose $\vec{x} \in \mathbb{R}^n$

$$[w_1 \ w_2 \ \dots \ w_n]_{1 \times n}$$

$$[w_1, w_2 \dots w_n] \times \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} + w_0 = 0$$

$$\boxed{\vec{w}^T \cdot \vec{x} + w_0 = 0}$$

x_1 weight	x_2 diameter	x_3 Color	x_4 taste	type
2	1	Red	sweet	orange
4	2	green	sour	santog

$$m_1 x_1 + m_2 x_2 + m_3 x_3 + m_4 x_4 + w_0 = y$$

$$w^T x + w_0 = 0$$

\Downarrow

$$w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_n x_n + w_0 = 0$$

\Downarrow

Dot product
(inner product)

Dot Product

\vec{a} & \vec{b}

$$\vec{a} \cdot \vec{b} = a_1 b_1 + a_2 b_2 + a_3 b_3 + \dots + a_n b_n$$

$$\vec{a} \cdot \vec{b} = \sum_{i=1}^n a_i b_i$$

$$\langle \vec{a}, \vec{b} \rangle$$

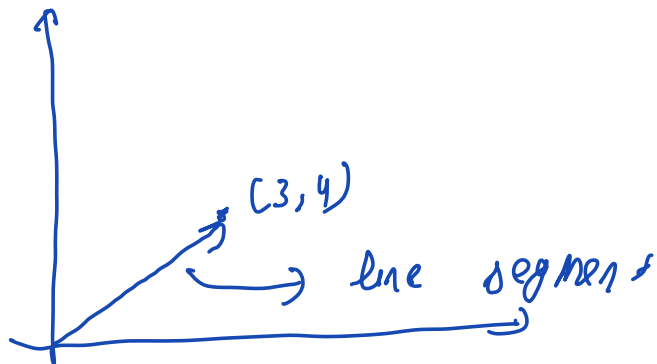
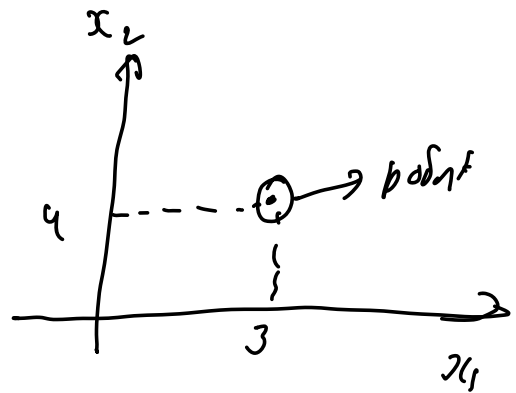
\Rightarrow find the dot product of
 $[1, 2, 3]$ & $[-1, 2, 5]$

$$\begin{aligned} 1 \times -1 + 2 \times 2 + 3 \times 5 \\ -1 + 4 + 15 \\ \Rightarrow 18 \end{aligned}$$

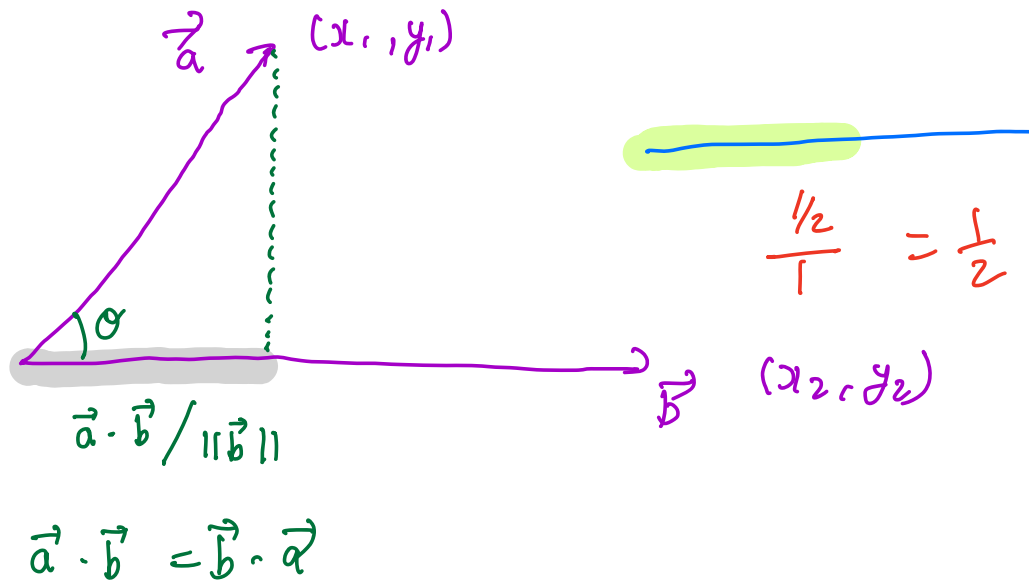
Geometric Intuition of Vectors

$$\vec{x} = [x_1, x_2]$$

$$\vec{x} = [3, 4]$$

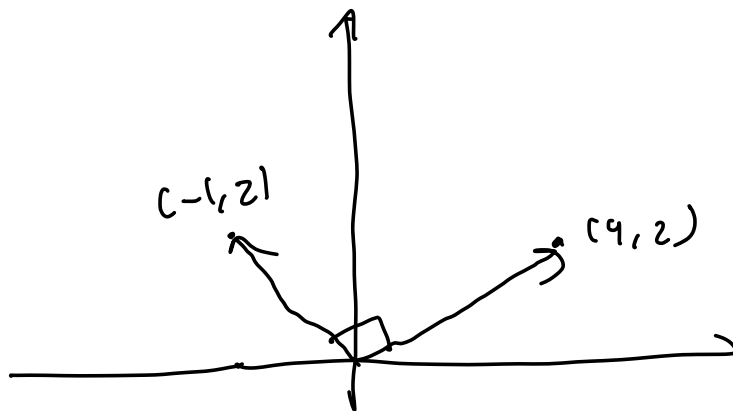


Geometric Meaning of Dot Product



\Rightarrow What is the dot product of $(-1, 2)$ & $(4, 2)$

$$-1 \times 4 + 2 \times 2 = 0$$



if $\vec{a} \perp \vec{b}$

$$\vec{a} \cdot \vec{b} = 0$$

Break : 8:05 am

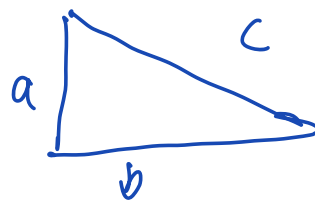
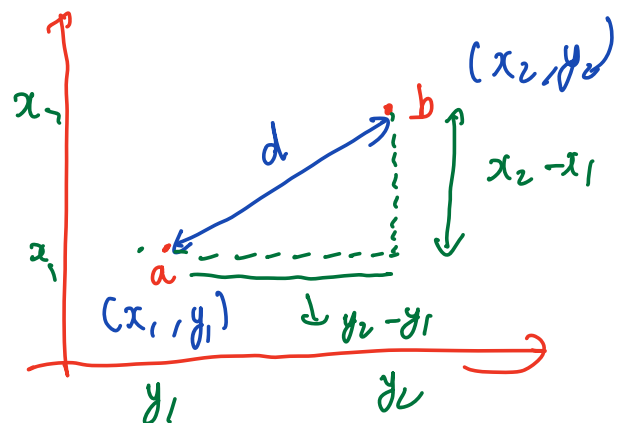
Sat : 7/8 am - 10 am

Sun : 7/8 am - 10 am

Thurs : 9 pm - 11 pm

Distance b/w 2 points

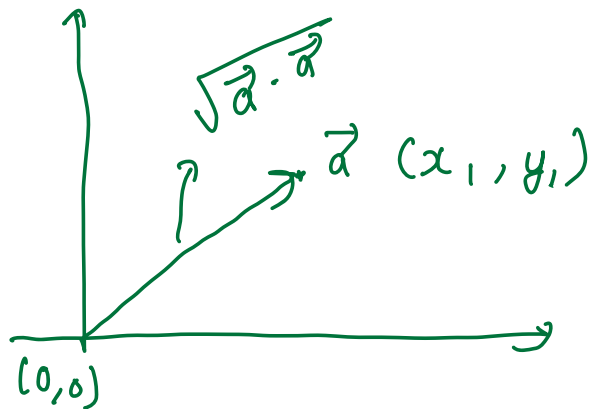
$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$c = \sqrt{a^2 + b^2}$$

$$d = \sqrt{x_1^2 + y_1^2}$$

$$\underline{d}^2 = [x_1 \ y_1] \times \begin{bmatrix} x_1 \\ y_1 \end{bmatrix}$$



$$(x_1, y_1) \cdot (x_1, y_1)$$

$$\| \vec{a} \| = \sqrt{\vec{a} \cdot \vec{a}}$$

Norm or Magnitude

Q \Rightarrow Find the distance b/w (3, 4) & (7, 7)

$$\sqrt{(4)^2 + (3)^2}$$

$$= \sqrt{16 + 9} = \sqrt{25} = 5$$

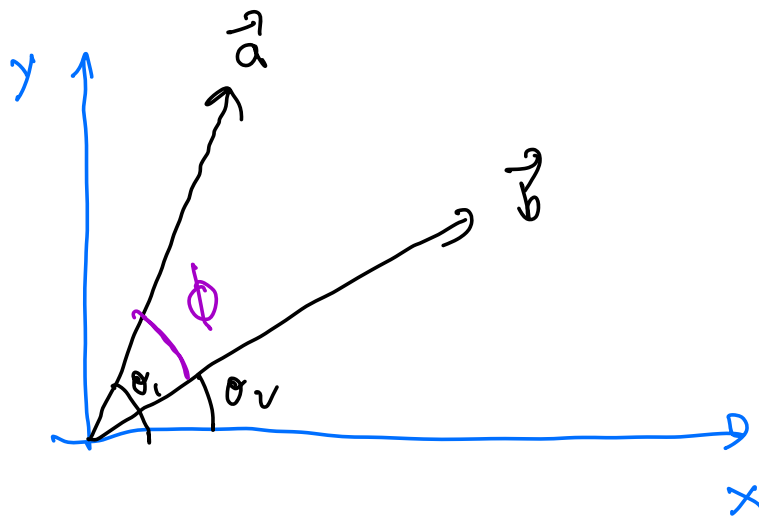
Q \Rightarrow Find the difference b/w the norm of $(6, 8)$ & magnitude of $(3, 4)$

$$\sqrt{36 + 64} \Rightarrow 10$$

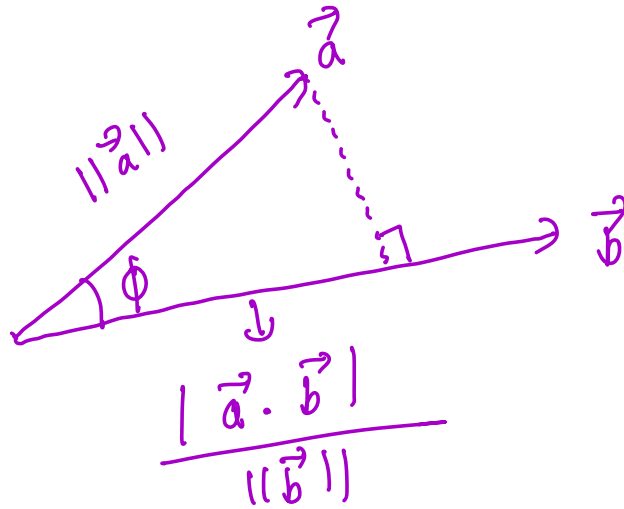
$$\sqrt{9 + 16} \Rightarrow 5$$

$$\begin{array}{r} 10 - 5 \\ 5 \end{array}$$

Angle b/w 2 vectors

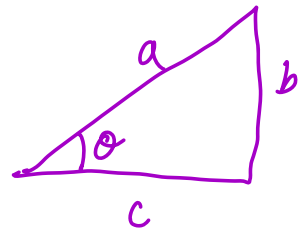


$$\phi = \theta_1 - \theta_2$$



$$\cos \theta =$$

$$\frac{|\vec{a} \cdot \vec{b}|}{\|\vec{b}\| \cdot \|\vec{a}\|}$$



$$\tan \theta = \frac{b}{c}$$

$$\cos \theta = \frac{c}{a}$$

Recap

Line:

$$y = mx + c$$

$$ax + by + c = 0$$

Hyperplane:

$$w_1 x_1 + w_2 x_2 + \dots + w_n x_n + w_0 = 0$$

$$w^T x + w_0 = 0$$

Vector :

$$\vec{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} \in \mathbb{R}^n$$

$$\vec{x}^T = [x_1 \ x_2 \ x_3 \ \dots \ x_n]$$

Dot product :

$$\vec{x} \cdot \vec{y} = \sum x_i y_i$$

$$\begin{aligned} \vec{x} \cdot \vec{x} &= x_1^2 + x_2^2 = d^2 \\ &= \text{norm}^2 \\ &= \text{magnitude}^2 \end{aligned}$$

Distance :

$$(x_1, y_1) \quad (x_2, y_2)$$

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Angle :

$$\cos \phi = \frac{|\vec{a} \cdot \vec{b}|}{\|\vec{a}\| \cdot \|\vec{b}\|}$$