

## MidTerm Review

Anurag Nagar

Topics  
Covered

Inductive  
Learning

Information  
Based  
Learning

Decision Tree

Entropy

Information Gain

Probability

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Expected Value

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Neural  
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SVM

# MidTerm Review

Anurag Nagar

Machine Learning Class

# Outline

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# Topics Covered

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List of topics covered so far (in no particular order)

- Inductive Learning - Linear Regression
- Information Based Learning - Entropy and Information Gain, Decision Trees
- Probability and naive Bayes Classifier
- Perceptron
- Artificial Neural Network
- SVM

Deep Learning will **not** be included

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# Inductive Learning

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## What is Inductive Learning?

- A dataset is available with following data for each instance:  
target variable  $Y$

$$\text{feature vector } X = \begin{pmatrix} X_1 \\ X_2 \\ X_3 \end{pmatrix}$$

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## What is Inductive Learning?

- A dataset is available with following data for each instance:  
target variable  $Y$

$$\text{feature vector } X = \begin{pmatrix} X_1 \\ X_2 \\ X_3 \end{pmatrix}$$

- You assume that there is a function  $f(X)$  that relates  $X$  to  $Y$ .

$$Y = f(X) + \epsilon$$

where  $\epsilon$  is the error.

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## What is Inductive Learning?

- A dataset is available with following data for each instance:  
target variable  $Y$

$$\text{feature vector } X = \begin{pmatrix} X_1 \\ X_2 \\ X_3 \end{pmatrix}$$

- You assume that there is a function  $f(X)$  that relates  $X$  to  $Y$ .

$$Y = f(X) + \epsilon$$

where  $\epsilon$  is the error.

- For example,  $Y$  could be the GPA, and  $X_1$  could be the SAT score,  $X_2$  could be percent attendance, and  $X_3$  could be the hours studied every week.

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## Function Estimation

- Based on the training data, you propose a function  $\hat{f}$  that approximates  $f$

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## Function Estimation

- Based on the training data, you propose a function  $\hat{f}$  that approximates  $f$
- You would like  $\hat{f}$  to be such that it minimizes the mean squared error over all examples  $i$

$$\text{MSE} = \frac{1}{N} \sum_{i=1}^N (Y_i - \hat{f}(x_i))^2$$

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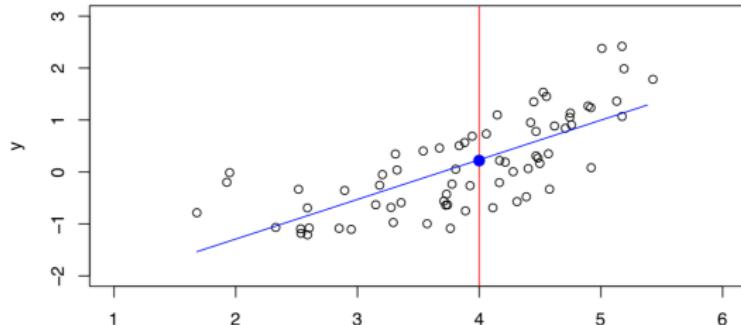


Figure: Linear Model

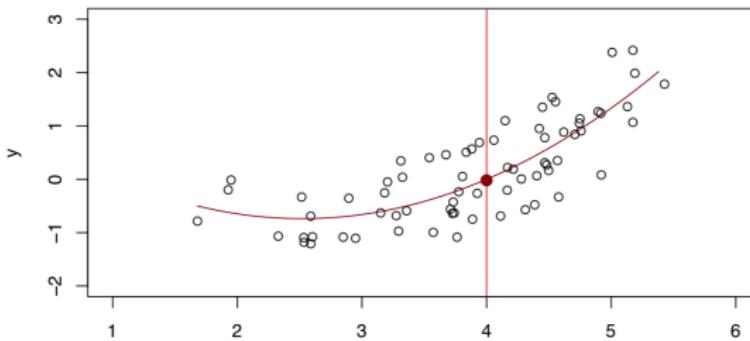
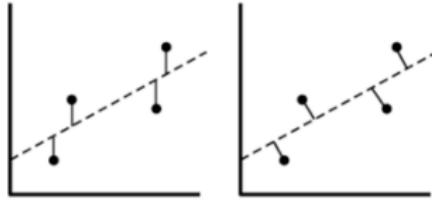


Figure: Quadratic Model

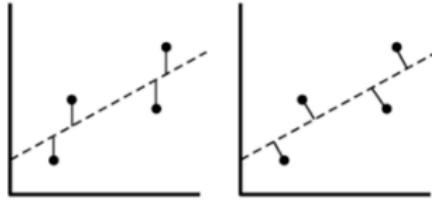
# Example 1

In the figures below, the circles represent the data points, and the dashed line represents the function fitted to the line. Which of the following shows the correct value of error for each point?



# Example 1

In the figures below, the circles represent the data points, and the dashed line represents the function fitted to the line. Which of the following shows the correct value of error for each point?



The one on the left as it shows the distance between prediction and actual value.

# Example 2

For predicting the output variable  $Y$  as a function of input variable  $x$ , you design a linear model of the following form:

$$Y = a + bx$$

What do  $a$  and  $b$  represent?

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## Example 2

For predicting the output variable  $Y$  as a function of input variable  $x$ , you design a linear model of the following form:

$$Y = a + bx$$

What do  $a$  and  $b$  represent?

a represents the Y-intercept and b represents the slope.

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## Example 3

For the following dataset,  $x$  represents the independent variable, and  $y$  is the output variable.

$x$	1	10	20
$y$	1	100	400

You propose a linear regression equation as below:

$$Y = -140 + 30x$$

What will be the value of Mean Squared Error (MSE)?

# Example 3

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For the following dataset,  $x$  represents the independent variable, and  $y$  is the output variable.

$x$	1	10	20
$y$	1	100	400

You propose a linear regression equation as below:

$$Y = -140 + 30x$$

What will be the value of Mean Squared Error (MSE)?

The predicted values for each of the points would be: -110, 160, and 460. So the MSE would be:

$$MSE = \frac{1}{3}[(1 + 110)^2 + (100 - 160)^2 + (400 - 460)^2] = 6507$$

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Which of the following is/are types of nodes in a decision tree

- 1 Root Node**
- 2 Leaf Node**
- 3 Internal Node**
- 4 Jump Node**

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Which of the following node in a decision tree gives the predicted label?

- 1 Root Node**
- 2 Leaf Node**
- 3 Internal Node**
- 4 Jump Node**

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In a decision tree, which node contains all of the input data?

- 1 Root Node**
- 2 Leaf Node**
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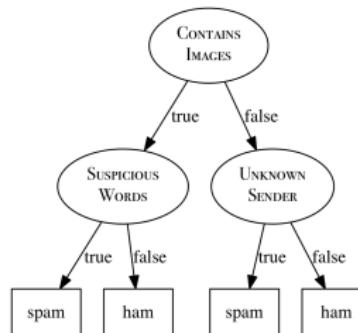
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Suppose you have an email dataset with three Boolean attributes - Suspicious Words, Unknown Sender, and Contains Images, and an Boolean output which could be spam or ham. You create the decision tree below.



What would be the predicted classification for Suspicious Words = true, Unknown Sender = True, and Contains Images = False

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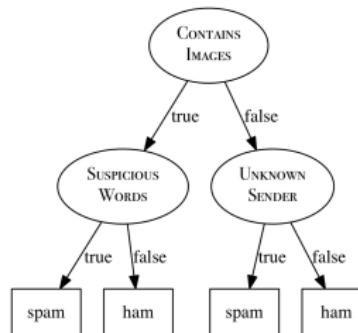
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Spam

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What is the definition of Entropy of a dataset containing  $k$  classes,  $1, 2, \dots, k$ , where each class  $i$  has probability  $p_i$ .

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What is the definition of Entropy of a dataset containing  $k$  classes,  $1, 2, \dots, k$ , where each class  $i$  has probability  $p_i$ .

$$H(\text{dataset}) = - \sum_{i=1}^k p_i \log_2(p_i)$$

# Entropy

What is the entropy of a set of 52 playing cards if we only distinguish between the cards based on their suit  
 $\{\heartsuit, \clubsuit, \diamondsuit, \spadesuit\}$ ?

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What is the entropy of a set of 52 playing cards if we only distinguish between the cards based on their suit  
 $\{\heartsuit, \clubsuit, \diamondsuit, \spadesuit\}$ ?

$$\begin{aligned} H(\text{suit}) &= - \sum_{l \in \{\heartsuit, \clubsuit, \diamondsuit, \spadesuit\}} P(\text{suit} = l) \times \log_2(P(\text{suit} = l)) \\ &= -((P(\heartsuit) \times \log_2(P(\heartsuit))) + (P(\clubsuit) \times \log_2(P(\clubsuit))) \\ &\quad + (P(\diamondsuit) \times \log_2(P(\diamondsuit))) + (P(\spadesuit) \times \log_2(P(\spadesuit)))) \\ &= -\left(\left(\frac{13}{52} \times \log_2\left(\frac{13}{52}\right)\right) + \left(\frac{13}{52} \times \log_2\left(\frac{13}{52}\right)\right)\right. \\ &\quad \left.+ \left(\frac{13}{52} \times \log_2\left(\frac{13}{52}\right)\right) + \left(\frac{13}{52} \times \log_2\left(\frac{13}{52}\right)\right)\right) \\ &= -((0.25 \times -2) + (0.25 \times -2) \\ &\quad + (0.25 \times -2) + (0.25 \times -2)) \\ &= 2 \text{ bits} \end{aligned}$$

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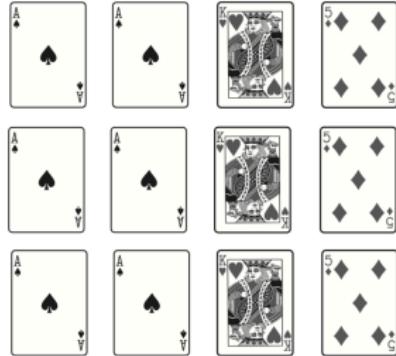
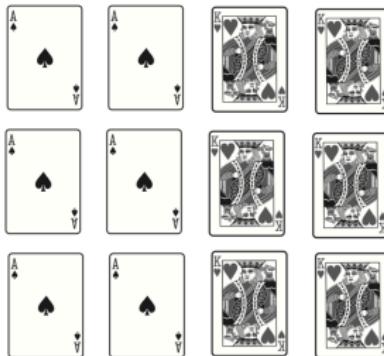
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Which of the following has lower entropy?



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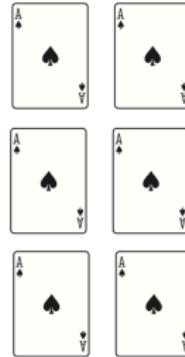
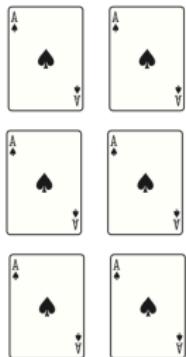
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Which of the following has lower entropy?



Left one has entropy of 1.00 and right has entropy of 1.50

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In the following dataset, which attribute out of X, Y, and Z would give the best information gain

X	Y	Z	C
1	1	1	I
1	1	0	I
0	0	1	II
1	0	0	II

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In the following dataset, which attribute out of X, Y, and Z would give the best information gain

X	Y	Z	C
1	1	1	I
1	1	0	I
0	0	1	II
1	0	0	II

Best Attribute: Y

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- Go through some examples of creating decision trees using ID3

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- Go through some examples of creating decision trees using ID3
- No need to study alternate information measures, noise, overfitting, etc

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## Conditional Probability:

$$\begin{aligned} P(X = a | Y = b) &= \frac{P(X = a, Y = b)}{P(Y = b)} \\ &= \frac{P(X = a)P(Y = b | X = a)}{P(Y = b)} \end{aligned}$$

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10% of patients entering a doctor's office have liver disease, and 5% of patients walking in are alcoholics. Of those that are diagnosed with liver disease, 7% are alcoholics. Given a patient walking into the office is alcoholic, what is the probability that he will be diagnosed with liver disease.

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A = having liver disease

B = being alcoholic

$$\begin{aligned} P(A|B) &= \frac{P(B|A)P(A)}{P(B)} \\ &= \frac{0.07 \times 0.10}{0.05} \\ &= 0.14 \end{aligned}$$

14%

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From a standard deck of playing cards, someone draws a random card and tells you it's a face card. What is the probability that it is a king of any suit?

Hint: J, Q, K are called face cards.

# Probability

From a standard deck of playing cards, someone draws a random card and tells you it's a face card. What is the probability that it is a king of any suit?

Hint: J, Q, K are called face cards.

A = card being a king

B = drawing a face card

$$\begin{aligned}P(A|B) &= \frac{P(B|A)P(A)}{P(B)} \\&= \frac{1.00 \times (4/52)}{(12/52)} \\&= 1/3\end{aligned}$$

33.3%

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In an experiment if there are  $n$  possible outcomes which are denoted by random variable  $X$  taking values  $X_1, X_2, \dots, X_n$  with respected probability values  $p_1, p_2, \dots, p_n$ , the **expected value** of  $X$  is :

$$E(X) = \mu(X) = \sum_{i=1}^n p_i X_i$$

and **variance** of  $X$  is:

$$\begin{aligned} \text{var}(X) &= E[(X - \mu)^2] \\ &= E[X^2] - E[X]^2 \end{aligned}$$

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An insurance company sells a policy that costs \$150, and pays \$5000 for major accident, and \$1000 for a minor accident only once. The probability of major accident is 0.005 and that of minor incident is 0.08. What is the expected value of the profit/loss for each policy sold by the company.

# Expected Value

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There could be three cases for the company

1. No accident, profit = \$150, probability =  $1 - 0.005 - 0.08 = 0.915$
2. Major accident, profit = \$  $(150 - 5000) = -\$4850$ , probability = 0.005
3. Minor accident, profit = \$  $(150 - 1000) = -\$850$ , probability = 0.08

$$\begin{aligned}E(X) &= 150 * 0.915 - 4850 * 0.005 - 850 * 0.08 \\&= 45\end{aligned}$$

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In a game, the probability of success is 0.6, and for a win you are paid \$1 and for a loss you lose \$1. What is the variance of outcome?

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In a game, the probability of success is 0.6, and for a win you are paid \$1 and for a loss you lose \$1. What is the variance of outcome?

$$E(X) = p = 0.6$$

<b>X</b>	+1	-1
<b>p(X)</b>	0.6	0.4
$(X - E(X))^2$	$(1 - 0.6)^2$	$(-1 - 0.6)^2$

$$\begin{aligned}\text{var}(X) &= 0.6 * (0.4)^2 + 0.4 * (1.6)^2 \\ &= 1.12\end{aligned}$$

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# Naive Bayes Classifier

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Suppose there are two classes  $C_1$  and  $C_2$ , and we are given data  $X = (X_1, X_2, \dots, X_n)$ , the probability of it belonging to  $C_1$  and  $C_2$  is:

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$$P(C_1|X) = \frac{P(X|C_1)P(C_1)}{P(X)} \propto P(X|C_1)P(C_1)$$

$$P(C_2|X) = \frac{P(X|C_2)P(C_2)}{P(X)} \propto P(X|C_2)P(C_2)$$

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$$P(C_1|X) = \frac{P(X|C_1)P(C_1)}{P(X)} \propto P(X|C_1)P(C_1)$$

$$P(C_2|X) = \frac{P(X|C_2)P(C_2)}{P(X)} \propto P(X|C_2)P(C_2)$$

The Maximum a Posteriori (MAP) hypothesis compares  $P(X|C_i)P(C_i)$  for each class  $C_i$  and assigns  $X$  to the class that has the maximum value.

# Naive Assumption

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In many cases, it's not possible to evaluate  $P(X|C_1) = P((X_1, X_2, \dots, X_n)|C_i)$  because of lack of training data.

In such cases, we make the assumption that each of the features  $X_1, X_2, \dots, X_n$  is independent of each other for every class  $C_i$  (called the naive Bayes assumption)

$$\begin{aligned}P(X|C_1) &= P((X_1, X_2, \dots, X_n)|C_i) \\&= P(X_1|C_i)P(X_2|C_i)\dots P(X_n|C_i)\end{aligned}$$

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We have a small dataset consisting of three classes *well*, *cold*, *allergy* and three words *sneeze*, *cough*, *fever*. The distribution of the words for each class is shown below:

Prob	Well	Cold	Allergy
$P(c_i)$	0.9	0.05	0.05
$P(\text{sneeze} c_i)$	0.1	0.9	0.9
$P(\text{cough} c_i)$	0.1	0.8	0.7
$P(\text{fever} c_i)$	0.01	0.7	0.4

What would be the predicted tag for the a text containing words  $W = \text{sneeze}, \text{cough}, \neg \text{fever}$

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$$\begin{aligned}P(\text{well}|W) &= P(\text{sneeze}|\text{well})P(\text{cough}|\text{well})P(\neg\text{fever}|\text{well})P(\text{well}) \\&= 0.1 \times 0.1 \times 0.99 \times 0.9 \\&= 0.0089\end{aligned}$$

$$\begin{aligned}P(\text{cold}|W) &= P(\text{sneeze}|\text{cold})P(\text{cough}|\text{cold})P(\neg\text{fever}|\text{cold})P(\text{cold}) \\&= 0.9 \times 0.8 \times 0.3 \times 0.05 \\&= 0.01\end{aligned}$$

$$\begin{aligned}P(\text{allergy}|W) &= P(\text{sneeze}|\text{allergy})P(\text{cough}|\text{allergy})P(\neg\text{fever}|\text{allergy})P(\text{allergy}) \\&= 0.9 \times 0.7 \times 0.6 \times 0.05 \\&= 0.019\end{aligned}$$

The predicted class is **allergy**

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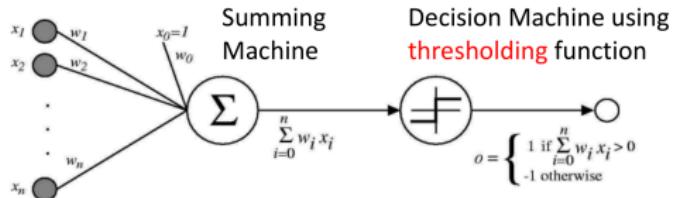
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Perceptron is a single unit of computation, that consists of an addition operation followed by an activation operation.

## Perceptron



$$o(x_1, \dots, x_n) = \begin{cases} 1 & \text{if } w_0 + w_1 x_1 + \dots + w_n x_n > 0 \\ -1 & \text{otherwise.} \end{cases}$$

Sometimes we'll use simpler vector notation:

$$o(\vec{x}) = \begin{cases} 1 & \text{if } \vec{w} \cdot \vec{x} > 0 \\ -1 & \text{otherwise.} \end{cases}$$

Note the classification rule above.

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## Another way of binary classification

## Linear Classification

- Two equivalent ways:

$$w^T x > \theta \text{ where } w = \begin{pmatrix} w_1 \\ w_2 \\ \dots \\ w_n \end{pmatrix} x = \begin{pmatrix} x_1 \\ x_2 \\ \dots \\ x_n \end{pmatrix} \text{ for class +1}$$

$$w^T x > 0 \text{ where } w = \begin{pmatrix} w_0 \\ w_1 \\ w_2 \\ \dots \\ w_n \end{pmatrix} x = \begin{pmatrix} x_0 \\ x_1 \\ x_2 \\ \dots \\ x_n \end{pmatrix} \text{ for class +1}$$

Note the classification rule above.

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Go through **AND, OR** classification using Perceptron from class slides.

You could be asked similar questions for AND NOT, NOT OR, etc

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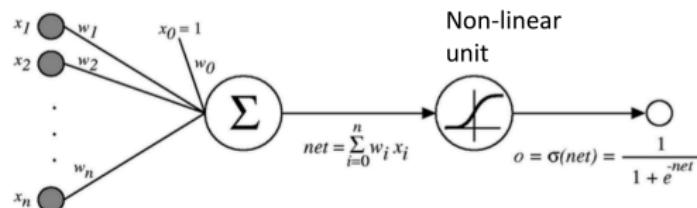
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In neural nets, each neuron uses a non-linear activation function, such as sigmoid.



$\sigma(x)$  is the sigmoid function

$$\frac{1}{1 + e^{-x}}$$

Nice property:  $\frac{d\sigma(x)}{dx} = \sigma(x)(1 - \sigma(x))$  **Really useful result**

Note the properties of sigmoid and its derivative.

# Neural Networks

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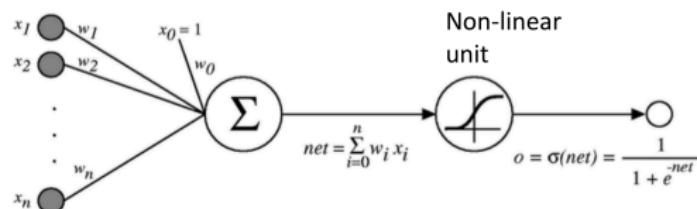
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Nice property:  $\frac{d\sigma(x)}{dx} = \sigma(x)(1 - \sigma(x))$  **Really useful result**

Note the properties of sigmoid and its derivative.

# Backpropagation Algorithm for Sigmoid Activation

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## Backpropagation Algorithm

Initialize all weights to small random numbers

Until convergence, Do

For each training example, Do

1. Input it to network and compute network outputs Forward pass
2. For each output unit  $k$

$$\delta_k \leftarrow o_k(1 - o_k)(t_k - o_k)$$

3. For each hidden unit  $h$

$$\delta_h \leftarrow o_h(1 - o_h) \sum_{k \in \text{outputs}} w_{h,k} \delta_k$$

4. Update each network weight  $w_{i,j}$  Backward pass

$$w_{i,j} \leftarrow w_{i,j} + \Delta w_{i,j}$$

$$\text{where } \Delta w_{i,j} = \eta \delta_j x_{i,j}$$

# Some possible questions

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Go through a simple example of backpropagation from class slides and questions.

Calculate square error at the output layer

Compute weight updates for backward pass

Given number of neurons in each layer, find number of connections.

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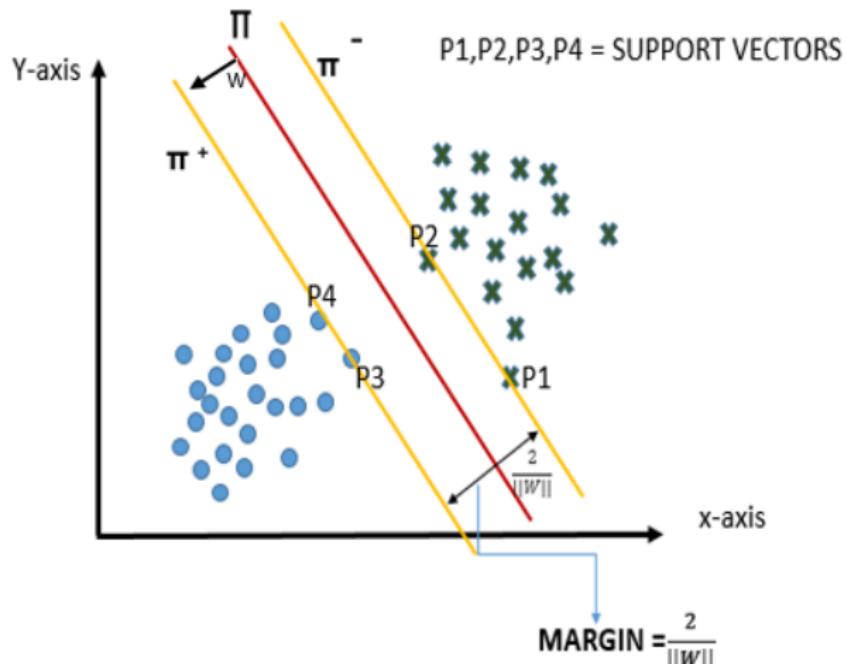
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Aim of SVM is to find the maximum margin classifier.



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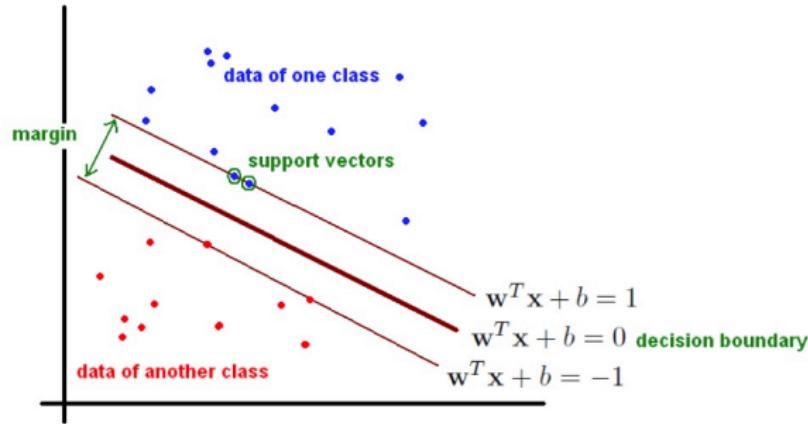
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SVM line is the center of two parallel lines passing through closest points on either sides, known as **support vectors**.



Source: <https://web.mit.edu/zoya/www/SVM.pdf>

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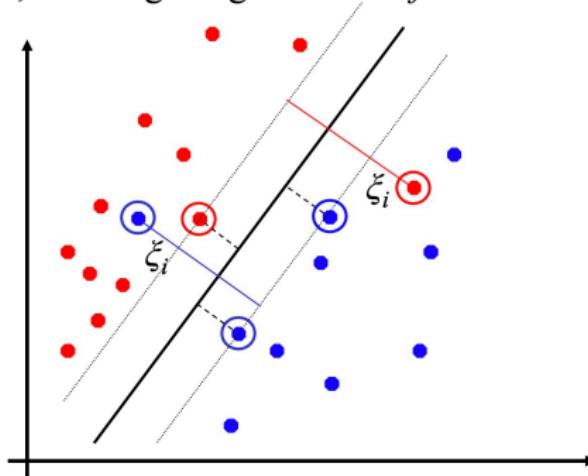
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## Non-separable case

What if the training set is not linearly separable?

*Slack variables*  $\xi_i$  can be added to allow misclassification of difficult or noisy examples, resulting margin called *soft*.



# Support Vector Machines

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Learn to compute following:

- Distance between a point and a line (or hyperplane) in scalar and vector formats.
- Distance between two parallel lines (or hyperplanes) in scalar and vector formats.
- Distance between two points in scalar and vector formats.
- Setting up of SVM optimization equation.
- Kernel Method
- Non-separable case, and C parameter