

Continuous-time Fourier transform	Discrete-time Fourier transform	Laplace Transform	
$X(j\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$	$X(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x(n) e^{-j\omega n}$	$X(s) = \int_{-\infty}^{\infty} x(t) e^{-st} dt$	1. Formula
$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{j\omega t} d\omega$	$x(n) = \frac{1}{2\pi} \int_{-\pi}^{\pi} X(e^{j\omega}) e^{j\omega n} d\omega$	$x(t) = \frac{1}{2\pi j} \int_{\sigma-j\infty}^{\sigma+j\infty} X(s) e^{st} ds$	2. Inverse formula
$a_1 x_1(t) + a_2 x_2(t) \longleftrightarrow a_1 X_1(j\omega) + a_2 X_2(j\omega)$	$a_1 x_1(n) + a_2 x_2(n) \longleftrightarrow a_1 X_1(e^{j\omega}) + a_2 X_2(e^{j\omega})$	$a x_1(t) + b x_2(t) \longleftrightarrow a X_1(s) + b X_2(s)$	3. Linearity
$x(t-t_0) \longleftrightarrow e^{-j\omega t_0} X(j\omega)$	$x[n-n_0] \longleftrightarrow e^{-j\omega n_0} X(e^{j\omega})$	$x(t-t_0) \longleftrightarrow e^{-st_0} X(s)$	4. Time shifting
$e^{j\omega_0 t} x(t) \longleftrightarrow X(j(\omega - \omega_0))$	$e^{j\omega_0 n} x[n] \longleftrightarrow X(e^{j(\omega - \omega_0)})$	$e^{s_0 t} x(t) \longleftrightarrow X(s-s_0)$	5. Frequency shifting
$x(at) \longleftrightarrow \frac{1}{ a } X\left(\frac{j\omega}{a}\right)$	-	$x(at) \longleftrightarrow \frac{1}{ a } X\left(\frac{s}{a}\right)$	6. Time scaling
$\frac{d}{dt} x(t) \longleftrightarrow j\omega X(j\omega)$	$x[n] - x[n-1] \longleftrightarrow (1 - e^{-j\omega}) \cdot X(e^{j\omega})$	$\frac{d}{dt} x(t) \longleftrightarrow s X(s)$	7. Diff (in t) or differencing
$t x(t) \longleftrightarrow j \frac{d}{d\omega} X(j\omega)$	$n x[n] \longleftrightarrow j \frac{d}{d\omega} X(e^{j\omega})$	$-t x(t) \longleftrightarrow \frac{d}{ds} X(s)$	8. Diff in frequency

$\int_{-\infty}^t x(t) dt \longleftrightarrow \frac{1}{j\omega} x(j\omega) + \pi x(0) \delta(\omega)$	$\sum_{k=-\infty}^{\infty} x[k] \longleftrightarrow \frac{1}{1-e^{-j\omega}} x(e^{j\omega})$	$\int_{-\infty}^t x(t) dt \longleftrightarrow \frac{1}{s} X(s)$	9. Integration (Accumulation)
<u>Parseval's relation for Aperiodic signals</u> $\int_{-\infty}^{\infty} x(t) ^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) ^2 d\omega$	<u>Parseval's relation for Aperiodic signals</u> $\sum_{n=-\infty}^{\infty} x[n] ^2 = \frac{1}{2\pi} \int_{-\pi}^{\pi} X(e^{j\omega}) ^2 d\omega$	<u>IVT and FVT</u> $\text{IVT: } x(0^+) = \lim_{s \rightarrow \infty} sX(s)$ $\text{FVT: } x(\infty) = \lim_{s \rightarrow 0} sX(s)$	10. Theorems
$\sum_{k=-\infty}^{\infty} X_k e^{jkw_0 t} \longleftrightarrow \sum_{k=-\infty}^{\infty} X_k \delta(\omega - kw_0)$	$\sum_{k=-\infty}^{\infty} X_k e^{jkw_0 n} \longleftrightarrow \sum_{k=-\infty}^{\infty} X_k \delta(\omega - kw_0)$	—	Transforms of Periodic signals
$x(-t) \longleftrightarrow X^*(-j\omega)$	$x[n] \longleftrightarrow X(e^{-j\omega})$	$x(-t) \longleftrightarrow X(-s)$	11. Time reversal
$x^*(t) \longleftrightarrow X^*(-j\omega)$	$x^*[n] \longleftrightarrow X^*(e^{-j\omega})$	$x^*(t) \longleftrightarrow X^*(s)$	12. Conjugation
$\text{Ev}\{x(t)\} \longleftrightarrow \text{Re}\{X(j\omega)\}$ $\text{Od}\{x(t)\} \longleftrightarrow j\text{Im}\{X(j\omega)\}$ $x(t) \rightarrow \text{real}$	$\text{Ev}\{x[n]\} \longleftrightarrow \text{Re}\{X(e^{j\omega})\}$ $\text{Od}\{x[n]\} \longleftrightarrow j\text{Im}\{X(e^{j\omega})\}$ $x[n] \rightarrow \text{real}$	—	13. Even + odd Symmetry
$x(t) * y(t) \longleftrightarrow X(j\omega) Y(j\omega)$ $X(j\omega) = \mathcal{L}\{x(t)\} + \mathcal{L}\{H(j\omega)\}$	$x[n] * y[n] \longleftrightarrow X(e^{j\omega}) Y(e^{j\omega})$	$x(t) * y(t) \longleftrightarrow X(s) Y(s)$	14. Convolution

