

## Last Class (Nov 10)

- 1) Breaking down a time series
- 2) Moving averages
- 3) Trend
- 4) Seasonality
- 5) Time Series decomposition  
↳ Decomposition from scratch

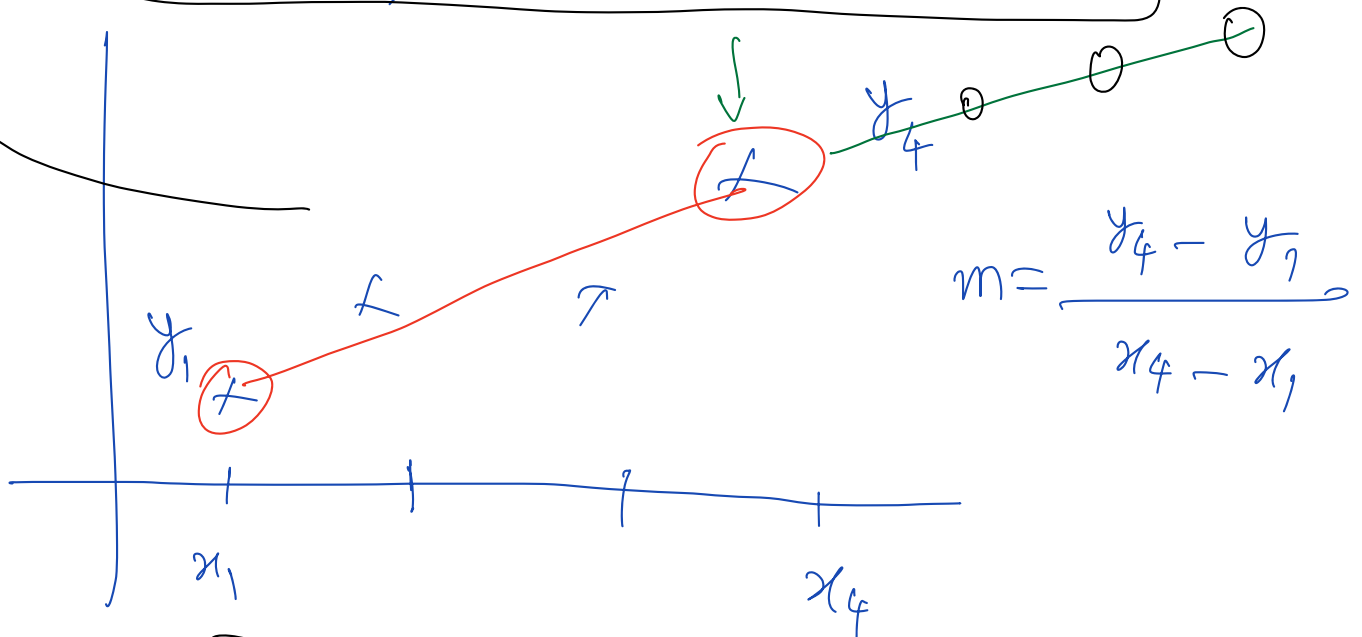
## Today's agenda

- 1) Generating forecasts
- 2) Train test splits
- 3) Simple Forecast methods
- 4) Naive Approach
- 5) Seasonal Naive Forecast
- 6) Drift Method
- 7) Smoothing Based Methods
- 8) Simple exponential smoothing

$$\hat{y}_{t+1} = \boxed{m} \cdot t + \boxed{c} \rightarrow \text{linear method}$$

$$\hat{y}_{t+1} = \boxed{m_1} t^2 + \boxed{m_2} t + \boxed{c}$$

$\downarrow$                        $\downarrow$                        $\downarrow$   
 $\hookrightarrow$                        $\downarrow$                        $\downarrow$



[YYYY/MM/DD]

2019/01/01

↑

1

2019/02/01

2

2019/03/01

3

...

13

X 0

[1: 12]

$$\hat{y}_{t+1}$$

$$h = 1$$

$$t+1, t+2, t+3, \dots$$

$$\alpha y_t + (1-\alpha) \hat{y}_t$$

actual value

pred value

$$= \alpha y_t + (1-\alpha) [\alpha y_{t-1} + (1-\alpha) \hat{y}_{t-1}]$$

$$\hat{y}_t = \alpha y_{t-1} + (1-\alpha) \hat{y}_{t-1}$$

$$= \alpha y_t + \alpha (1-\alpha) y_{t-1} + (1-\alpha)^2 \hat{y}_{t-1}$$

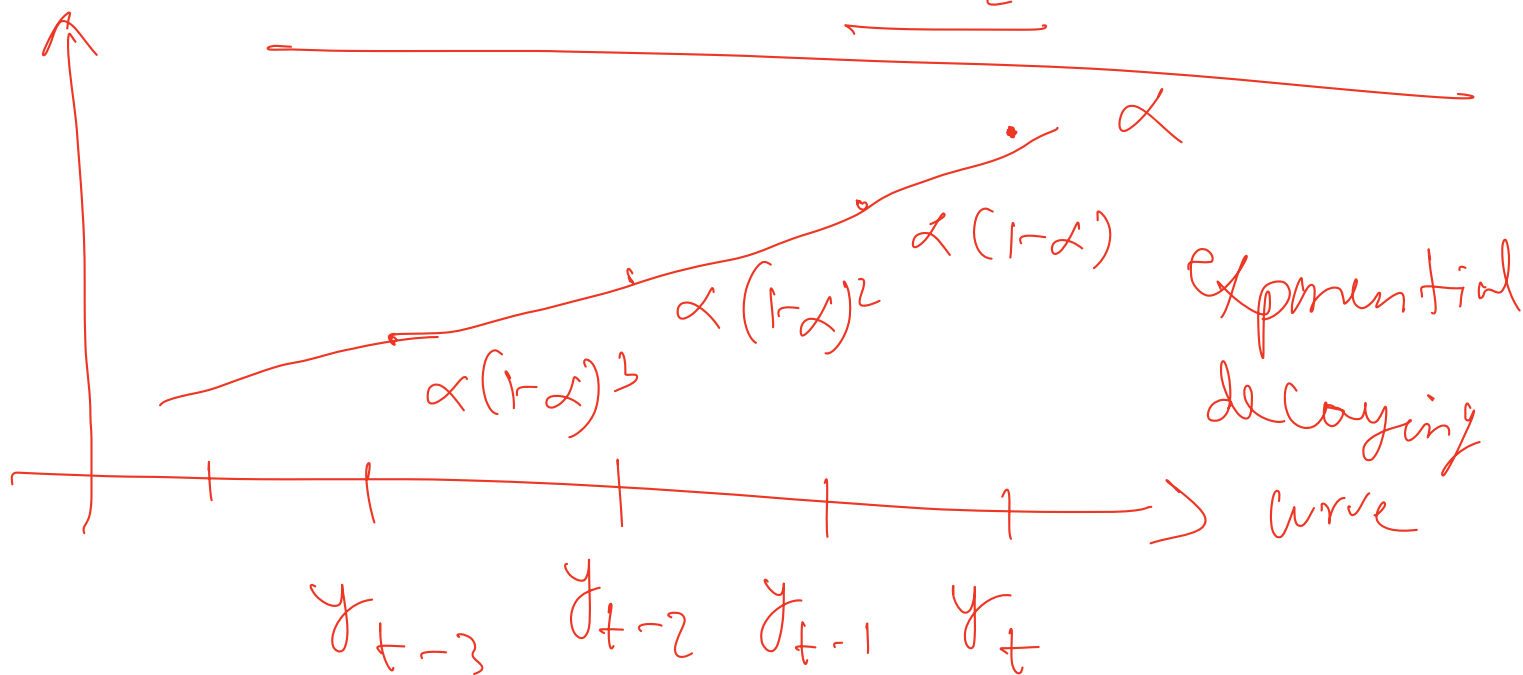
$$\alpha (1-\alpha)$$

$$\hat{y}_{t-1} = \alpha y_{t-2} + (1-\alpha) \hat{y}_{t-2}$$

$$\therefore (1-\alpha)^2 \hat{y}_{t-1} = \alpha (1-\alpha)^2 y_{t-2} + (1-\alpha)^3 \hat{y}_{t-2}$$

$$\alpha y_t + \alpha(1-\alpha)y_{t-1}$$

$$+ \alpha(1-\alpha)^2 y_{t-2} + \dots$$



$$\alpha = 0 \text{ to } 1$$

↓

$$\alpha = 0.3$$

$$1-\alpha = 0 \text{ to } 1$$

$$1-\alpha = 0.7$$

$$\alpha(1-\alpha) = 0.3 \times 0.7 = 0.21$$

$$0.21 < 0.3$$

$$\Rightarrow \alpha(1-\alpha) < \alpha$$