

20/11/18

Unit-1

→ principles of Simulated physics:-

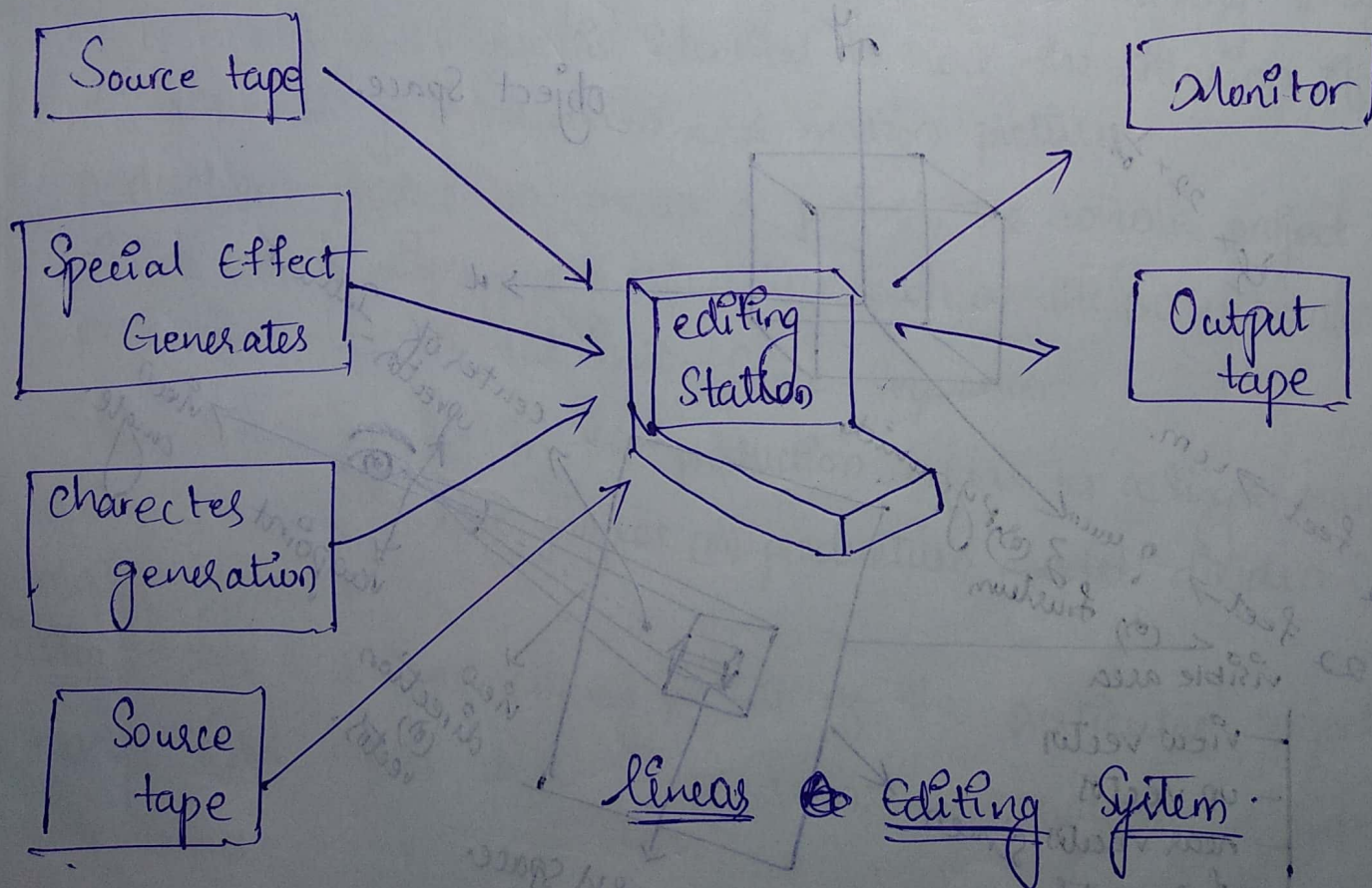
- 1) Squash and stretch stretch. (Compress and expand)
- 2) timing:- large objects move slow (w.r.t time object moves)
- 3) Secondary Action (primary action response)
- 4) Slow-in and Slow-out (zooming and zoom out of opening scenes)
- 5) Arcs:- (movement in linear, curved path) physical changes

→ Designing A Actions:- (Background Sounds, side sounds) directing.
Follow through (previous scenes)

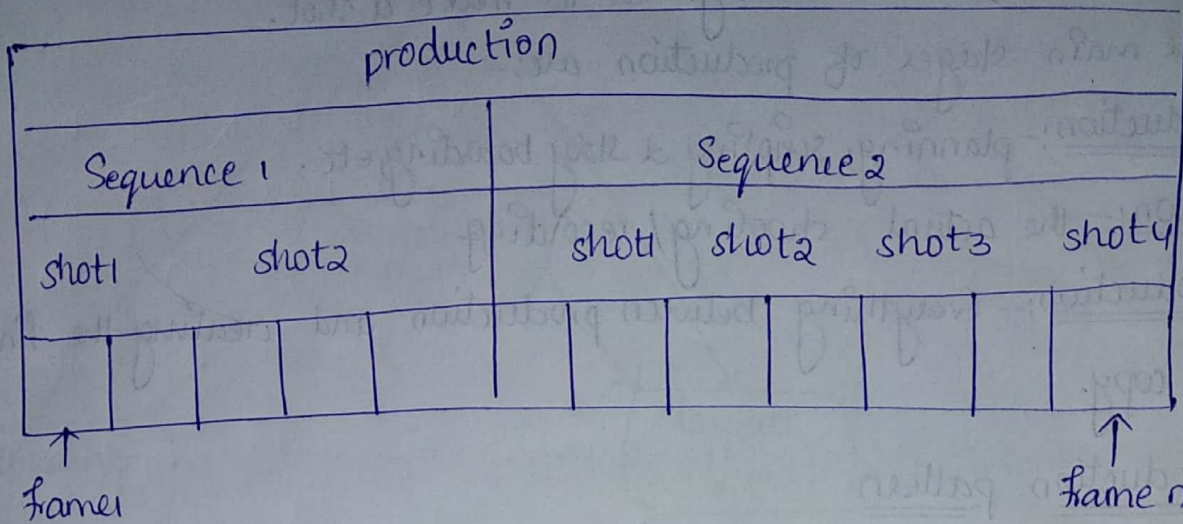
:- Focusing or directing (ambulance lights blinking).

appeal:- making scenes enjoyable

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Up vector: - the vector \perp to view vector.



Animation:- it is the technique of photographing successive drawings (or) positions of models to create an illusion of movement when the film is shown as a sequence.

Computer Animation:- it is the process used for generating animated images. Computer ~~graphic~~ generate both static scenes & dynamic images, while Computer animation only refers to the moving images.

This technique is identical to how the illusion of movement is achieved with television and motion pictures.

production:- production means a project. The whole project to make a picture (or) to display the object is known as the production. This production may be divided into some sequence.

Sequence:- Sequences in the production refers to a single half of animation. The whole project (or) production ~~model~~ divided into 3 major types.

1) Shot: - shot is a single clip or picture of the particular object. In film making a shot refers to a single scene. These shots are divided into some frames.

2. Frame:- A frame means the poster or photo used in each shot is known as a frame. Such no. of frames are joined to make a shot.

the three main stages of production are:-

preproduction:- planning, scripting & story boarding, etc.

production:- the actual shooting/ recording

post production:- Everything between production and creating the final master copy.

production pattern

preliminary story

story board - sketches:- layout of complete animation theme.

model sheet:- a document used to standardize appearance, pose and gesture.

exposure sheet - Audio:- tool, that allows animators to organize their work.

route sheet:- blueprint of manufacturing process in production unit.

animatic/story reel:- entire film in still picture form with sound track.

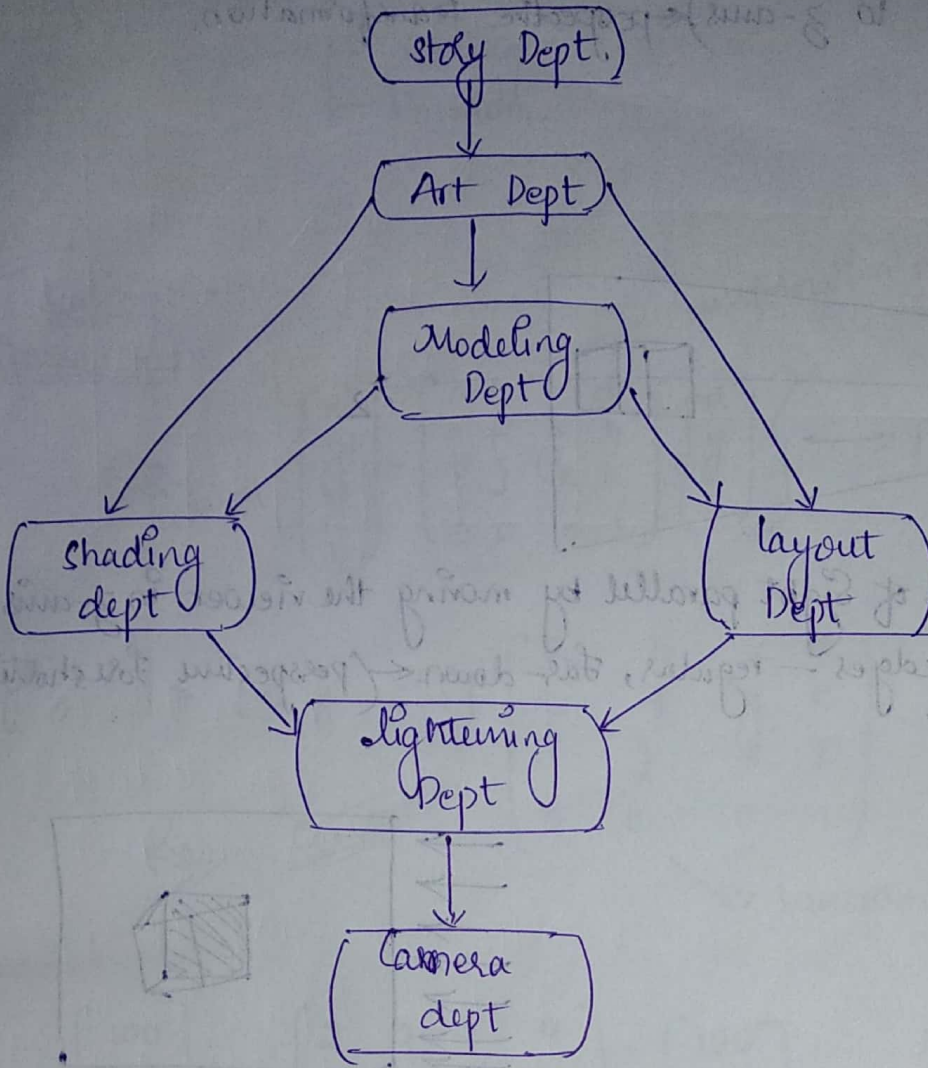
detailed story:- each and every character with getup is explained.

key frames:- starting and ending points of any smooth transition.

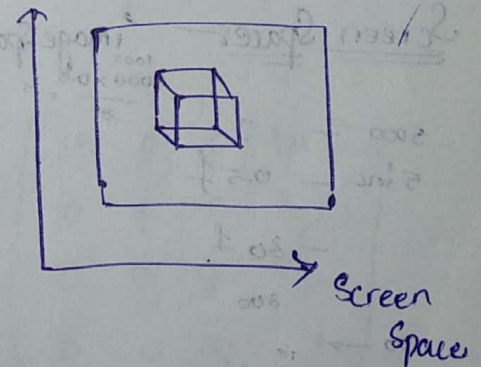
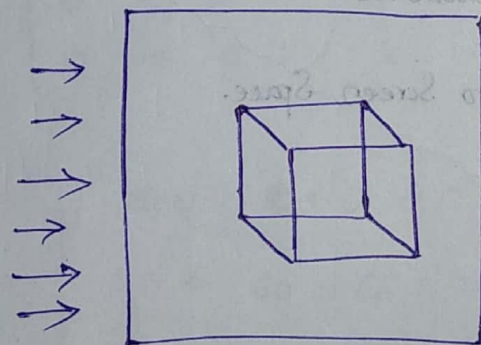
pencil test:- add something more to animation.

Inking:- Colouring to animation.

Opacising:- to create the illumination i.e. "light" or "dark".

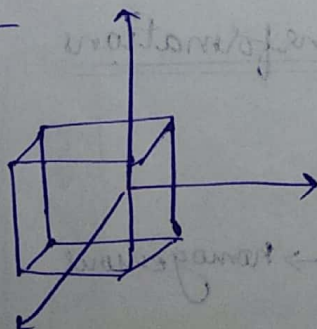


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Display Pipeline:-
Object Space:-



eye Space - (Bring viewer to z-axis) ← perspective transformation.

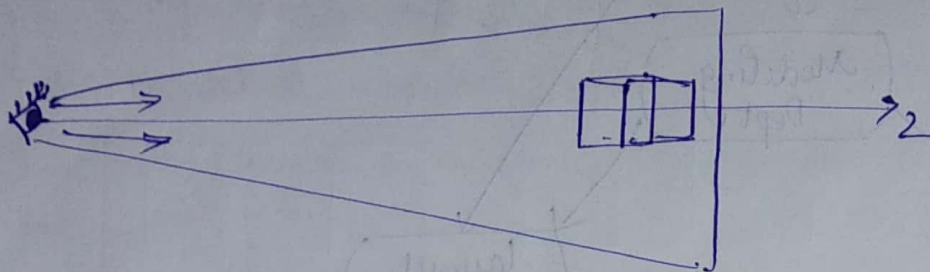
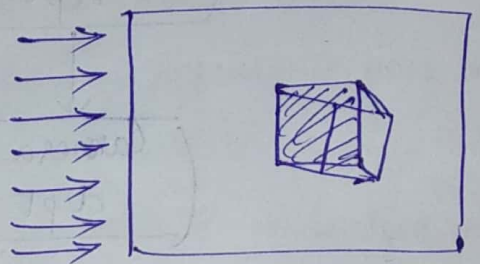
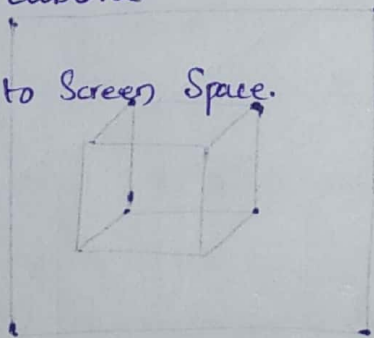
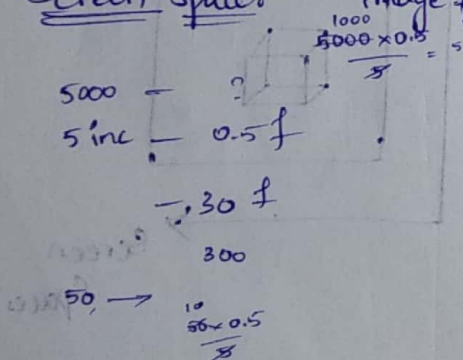


Image Space - make lines of sight parallel by moving the viewer in z-axis to Infinite distance. near edges - regular, far - down. ← (perspective foreshortening)



visible space - view frustum - cuboid.

Screen Space - image space is mapped to Screen Space.



homogeneous Coordinates and transformations

actual coordinates $\left(\frac{x}{w}, \frac{y}{w}, \frac{z}{w}\right) = x, y, z, w$.

Ex: $\left(\frac{100}{10}, \frac{20}{10}, \frac{30}{10}\right) = (100, 20, 30, 10) \rightarrow \text{homogeneous}$

transformations:-

- Translation
- Scaling
- Rotation

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Scaling:-
Translation:-

Column $\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$ } \rightarrow pre-multiplication

transformation matrix

Row $\begin{bmatrix} x' & y' & z' & 1 \end{bmatrix} = \begin{bmatrix} x & y & z & 1 \end{bmatrix} \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ 0 & 0 & 0 & 1 \end{bmatrix}$ } \rightarrow post Multiplication

transformation matrix

$$\begin{bmatrix} 100 \\ 20 \\ 30 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 100 \\ 20 \\ 30 \\ 1 \end{bmatrix}$$

$\frac{1}{2}$
 $\frac{1}{3}$
 $\frac{1}{4}$

$$x' \begin{bmatrix} 200 \\ 60 \\ 120 \\ 1 \end{bmatrix} = \begin{bmatrix} 200 + 0 + 0 + 0 \\ 0 + 60 + 0 + 0 \\ 0 + 0 + 120 + 0 \\ 0 + 0 + 0 + 1 \end{bmatrix} x' \begin{bmatrix} p & 0 & 0 & t_x \\ 0 & p & 0 & t_y \\ 0 & 0 & p & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

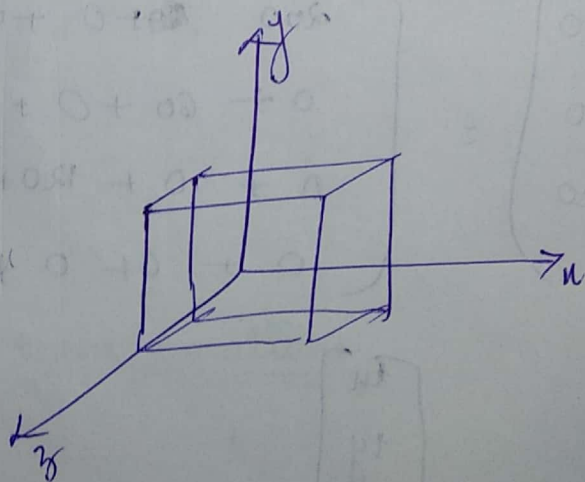
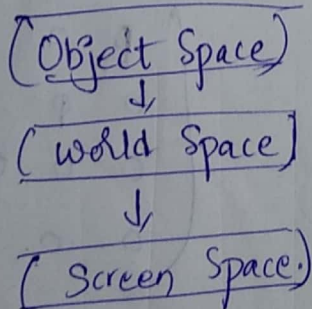
$$\begin{bmatrix} t_x \\ t_y \\ t_z \\ 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

translation

$$= \begin{bmatrix} 0 & 0 & 0 & 2 \\ 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 100 \\ 20 \\ 30 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 102 \\ 23 \\ 34 \\ 1 \end{bmatrix}$$

RayCasting:



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Rotation

along x-axis

$$\begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta & 0 \\ 0 & \sin\theta & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$

along y-axis

$$\begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta & \sin\theta & 0 \\ 0 & -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$

along y-axis

$$\begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix} = \begin{pmatrix} \cos\theta & 0 & \sin\theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta & 0 & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$

along z-axis

$$\begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta & 0 & 0 \\ \sin\theta & \cos\theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$

$$= (100, 20, 30, 10)$$

$$= (10, 2, 3)$$

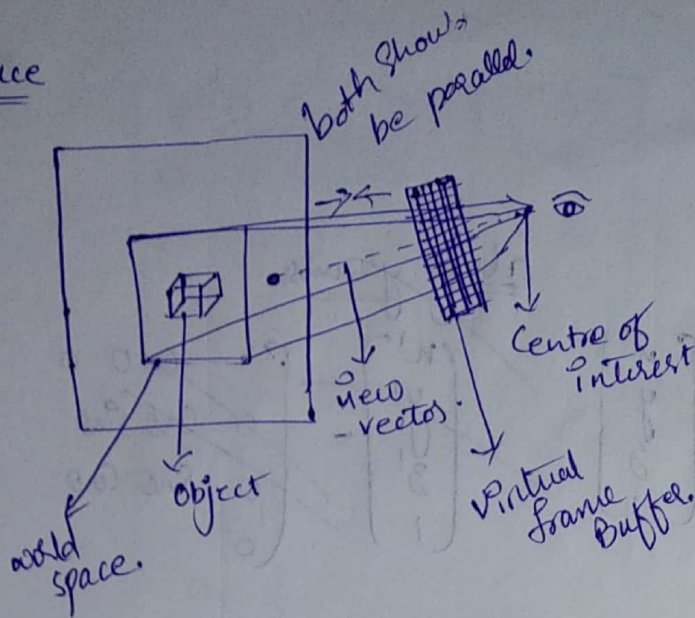
$$= \begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix} = \begin{pmatrix} \cos 90^\circ & 0 & 0 & 0 \\ 0 & \cos 90^\circ & -\sin 90^\circ & 0 \\ 0 & \sin 90^\circ & \cos 90^\circ & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 10 \\ 2 \\ 3 \\ 1 \end{pmatrix} \Rightarrow \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 10 \\ 2 \\ 3 \\ 1 \end{pmatrix}$$

along z

$$= \begin{pmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 10 \\ -3 \\ 2 \\ 1 \end{pmatrix} \Rightarrow \begin{pmatrix} 3 \\ 10 \\ 2 \\ 1 \end{pmatrix}$$

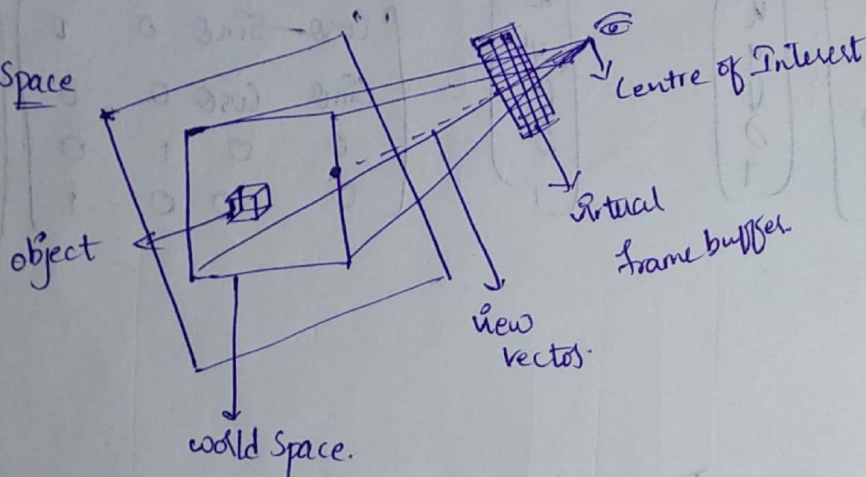
$$\begin{pmatrix} 10 \\ -3 \\ 2 \\ 1 \end{pmatrix}$$

world space

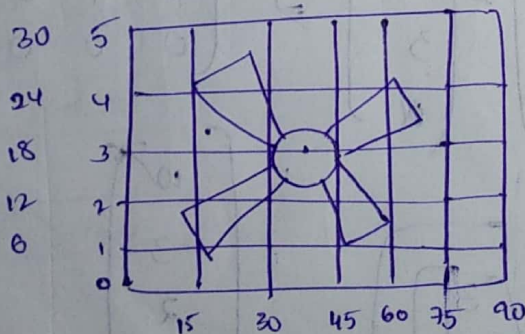


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world space



$$8 \times 5 = 0.5$$

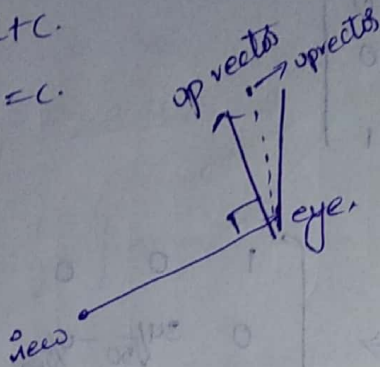


Representing An Arbitrary Orientation

view vector = eye position - Center of Interest (COI)

$$y = -x + c$$

$$x + y = c$$



① → line

② → perpendicular line

③ → Cross product with y-axis.

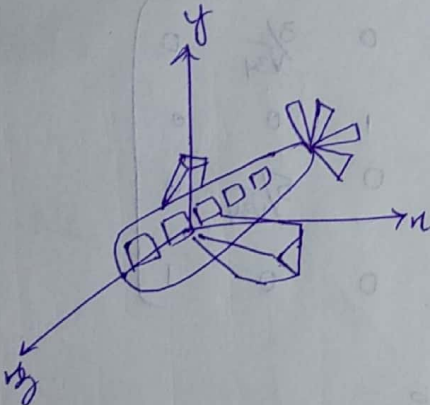
Fixed Angle Representation

Orientation Representation

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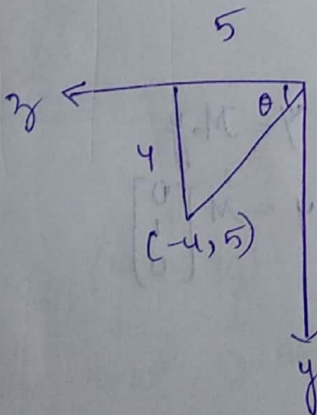
$$(23, -14, 30)$$

$$(20, -10, 35)$$



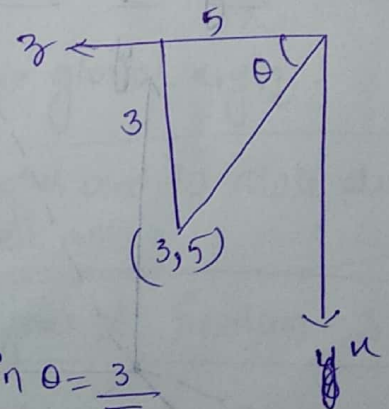
$$(23 - 20, -14 + 10, 30 - 35)$$

$$= (3, -4, -5)$$



$$\sin \varphi = \frac{4}{\sqrt{50}}$$

$$\cos \varphi = \frac{34}{\sqrt{50}}$$



$$\sin \theta = \frac{3}{\sqrt{34}}$$

$$\cos \theta = \frac{5}{\sqrt{34}}$$

transformation matrix along u-axis:-

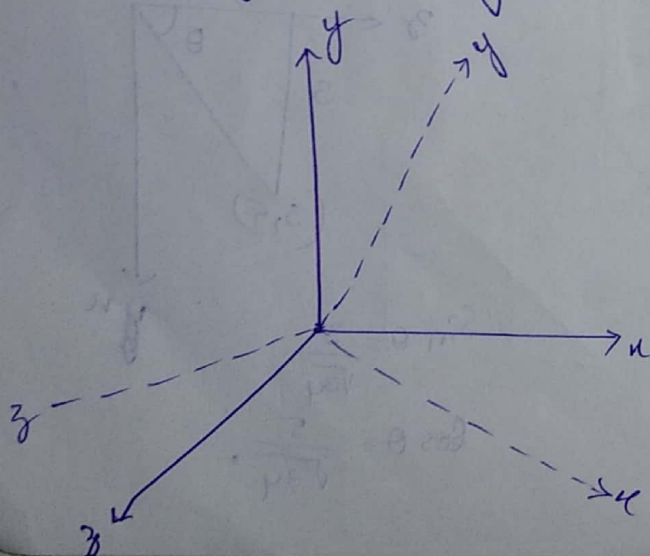
$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\phi & -\sin\phi & 0 \\ 0 & \sin\phi & \cos\phi & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\phi & -\sin\phi & 0 \\ 0 & \sin\phi & \cos\phi & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \frac{34}{\sqrt{50}} & -\frac{4}{\sqrt{50}} & 0 \\ 0 & \frac{4}{\sqrt{50}} & \frac{34}{\sqrt{50}} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

transformation matrix along y-axis:-

$$\begin{bmatrix} \cos\theta & 0 & \sin\theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta & 0 & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \Rightarrow \begin{bmatrix} \frac{5}{\sqrt{34}} & 0 & \frac{3}{\sqrt{34}} & 0 \\ 0 & 1 & 0 & 0 \\ -\frac{3}{\sqrt{34}} & 0 & \frac{5}{\sqrt{34}} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Another ways of finding transformation matrix:-



$$x = M \cdot u$$

$$x = M \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

$$y = M \cdot y$$

$$y = M \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

$$z = M \cdot z$$

$$= M \cdot \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

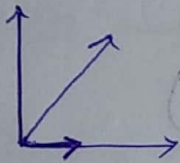
Ortho Normalization

0	1	2	3	----	100
↓	↓	↓	↓	↓	↓
0	0.1	0.2	0.3	0.4	1

$\left. \begin{matrix} 30 & - & 4 \\ 2 & - & ? \end{matrix} \right\} \text{normalization}$

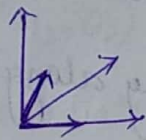
$$30K = \frac{4 \times 2}{30} = \frac{8}{30} = 0.26666$$

$$\frac{30}{20} = 1.5$$



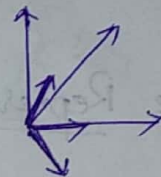
normalize 'n'.

N_n



cross product 'n' with any of the axis, then other axis is obtained

$$N_n \otimes (\otimes y \otimes) \otimes z = N_z$$



cross product both 'n' and obtain axis then third axis is normalized.

$$N_n \otimes N_z = N_y$$

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1) Fixed Angle Representation:-

Fixed angle \rightarrow global x, y, z .

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$$(10, 45, 90)$$

\downarrow
 $x = 10^\circ$

\downarrow
 $y = 45^\circ$

\downarrow
 $z = 90^\circ$

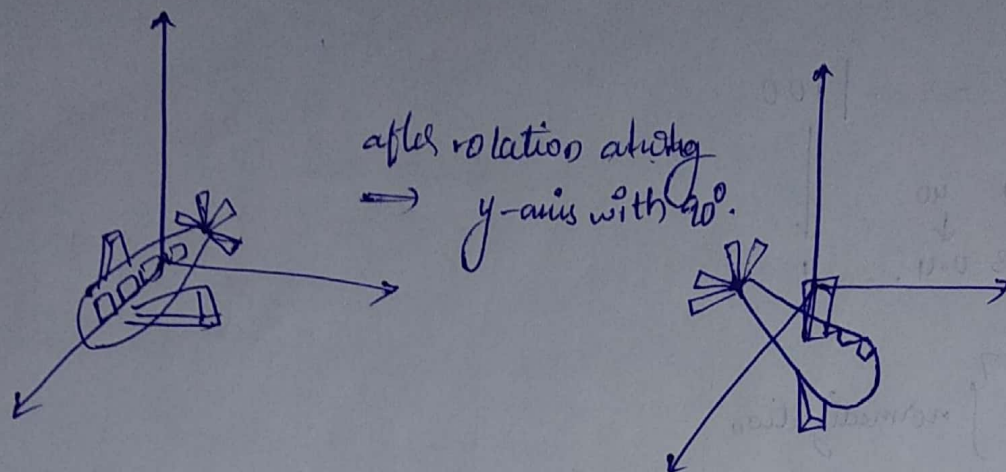
$$R_z^{90} [R_y^{45} (R_x^{10})]$$

* Angles used to rotate about fixed axes

degrees of freedom = 3

positive 90° rotation along y -axis
 negative 90° along y -axis

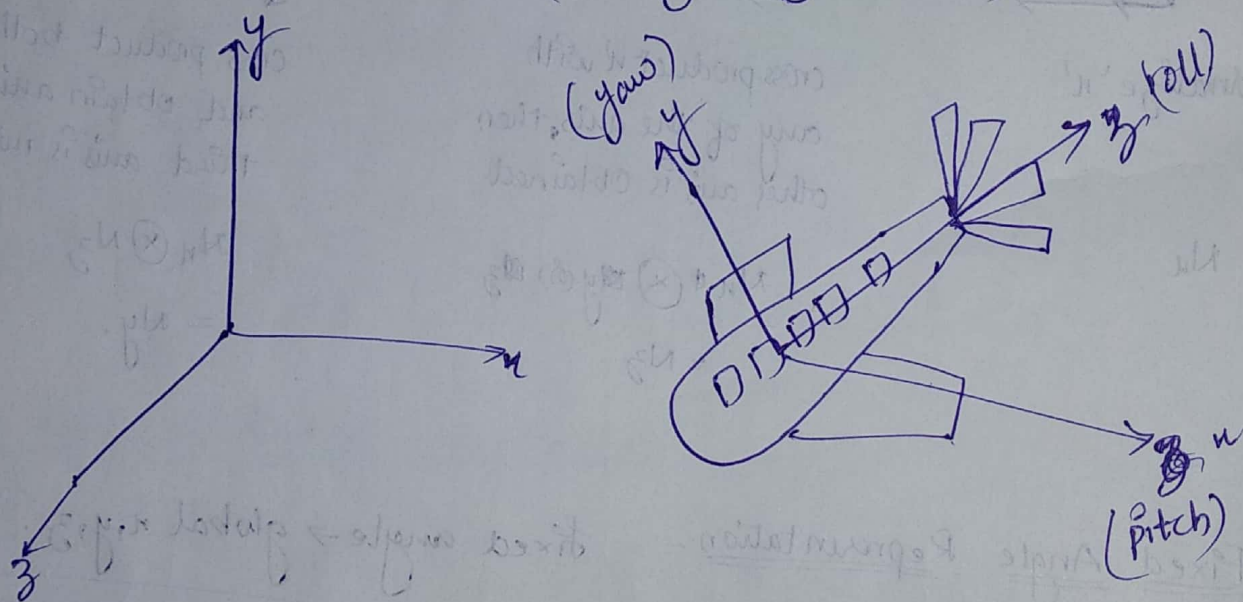
$(n-y-z)$ ✓
 $(n-y-x)$ ✓
 $(n-x-y)$ x meaning less



Gimbal Lock:-

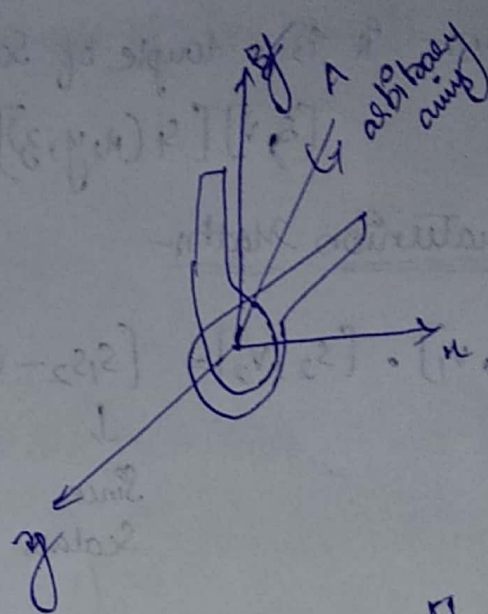
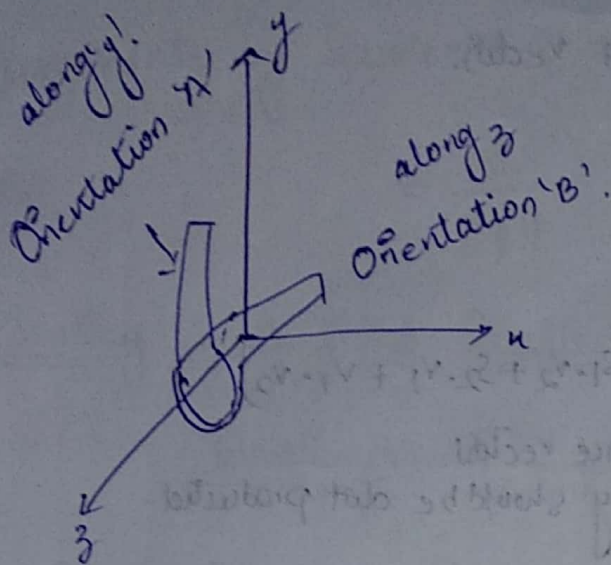
Rotation along y-axis by 90° made 1st axis align with 3rd axis because of this a slight variation in z effect x -axis.

2) Euler Angle Representation:- (rotating along local axis)



3) Angle and Axis

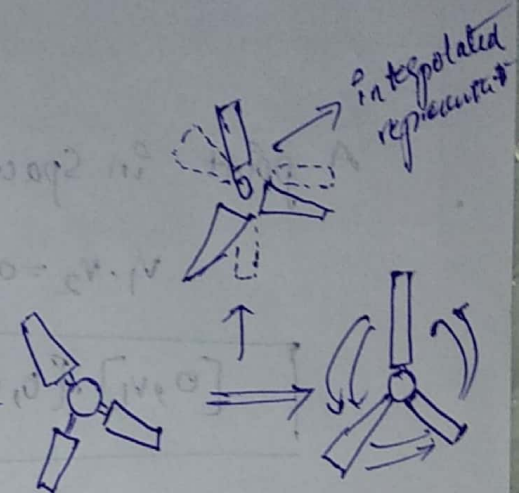
Euler's theorem implies that for any 2 Orientations of an Object one can be produced from another by a Single Rotation about an arbitrary Axis.



Orientation Represented by a 4 tuple
an angle and (x, y, z) (angle, x, y, z)

Interpolation $\rightarrow (A_1, \theta_1) (A_2, \theta_2)$

\hookrightarrow Finding out the intermediate frames.

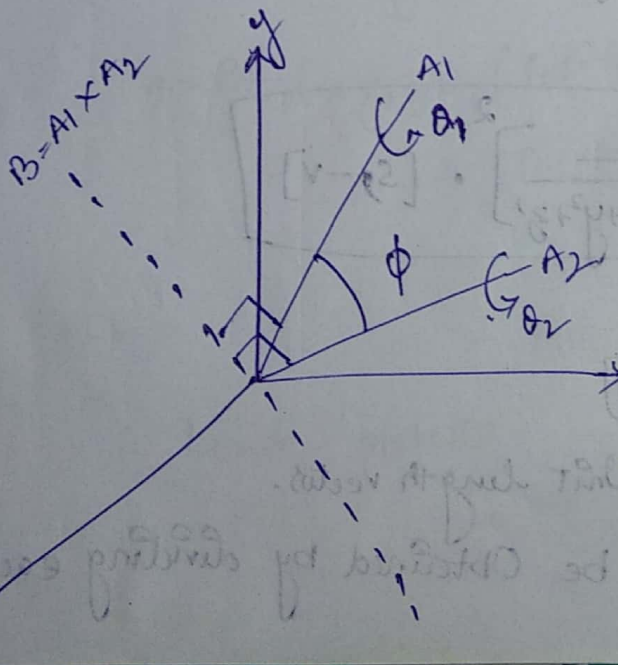


Axis of rotation — Cross product of 2 axes.

Angle b/w Axis — Inverse cosine of dot product of normalized version of axis.

$$\Rightarrow \cos^{-1} \left(\frac{A_1 \cdot A_2}{|A_1| |A_2|} \right) \Rightarrow \cos^{-1} \left(\frac{A_1 \cdot A_2}{|A_1| |A_2|} \right)$$

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$$B = A_1 \times A_2$$

$$\phi = \cos^{-1} \left(\frac{A_1 \cdot A_2}{|A_1| |A_2|} \right)$$

$$A_k = R_B(k, \phi) A_1$$

$$\theta_k = (1+k) \cdot \theta_1 + k \theta_2$$

Quaternion - It is a tuple of scalar and vectors.

$$[s, \vec{v}] [s, (x, y, z)]$$

Basic Quaternion Math

$$[s_1, \vec{v}_1] \cdot [s_2, \vec{v}_2] = [s_1 s_2 - \vec{v}_1 \cdot \vec{v}_2, s_1 \vec{v}_2 + s_2 \vec{v}_1 + \vec{v}_1 \times \vec{v}_2]$$

\downarrow
 Since Scalars \rightarrow Since vectors they should be dot product.

A point in space, 'v'. vector from origin to point is ~~(0, v)~~ $(0, \vec{v})$.

$\vec{v}_1 \cdot \vec{v}_2 = 0$, when \vec{v}_1 and \vec{v}_2 are Orthogonal vectors

$$[0, \vec{v}_1] \cdot [0, \vec{v}_2] = [0, \vec{v}_1 \times \vec{v}_2] \text{ iff } \vec{v}_1 \cdot \vec{v}_2 = 0$$

\Rightarrow Quaternion is Multiplicative Identity

$$[s, \vec{v}] [1, (0, 0, 0)] = [s, \vec{v}]$$

Inverse of Quaternion - It is obtained by negating its vector part and dividing both parts by magnitude square.

Inverse of s, \vec{v} is

$$[s, \vec{v}]^{-1} = \left[\frac{1}{\sqrt{s^2 + x^2 + y^2 + z^2}} \right]^2 \cdot [s, -\vec{v}]$$

$$[1, (0, 0, 0)]^{-1} = [1, (0, 0, 0)]$$

\rightarrow Unit length vectors.

\Rightarrow Unit length Quaternion can be obtained by dividing each of 4

Components by Square root of Sum of Square of Components.

$$= \frac{2}{\|q\|}$$

Rotating Vectors Using Quaternion:

$$\text{Rotation}(v) = v' = q \cdot v \cdot q^{-1}$$

$$\text{Rotation}_2(\text{Rotation}_p(v)) \Rightarrow q \cdot (p \cdot v \cdot p^{-1}) \cdot q^{-1}$$

$$= (qp) \cdot v \cdot (qp)^{-1}$$

$$= \text{Rot}_{qp}(v)$$

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$$\text{Rotation}^{-1}(\text{Rotation}(v)) = q^{-1}(q(v)q^{-1})q = v$$

Representing Rotations Using Quaternions:

$$q = \text{Rot}_\theta(u, y, z) = [\cos(\theta/2), \sin(\theta/2) \cdot (u, y, z)]$$

→ show that Quaternion and its negative $[-s, -\vec{v}]$ ~~also~~ represent same rotation.

$$q = \text{Rot}_\theta(u, y, z) = [\cos(-\theta/2), \sin(-\theta/2) \cdot -(u, y, z)]$$
$$= [\cos \theta/2, -\sin(\theta/2) \cdot -(u, y, z)]$$

$$= [\cos \theta/2, \sin(\theta/2) \cdot (u, y, z)]$$

$$= \text{Rot}_\theta(u, y, z)$$

\therefore hence proved