

Performance Metrics for Regression Problem

Error = Y (actual) — Y (predicted)

Mean Absolute Error (MAE)

$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i|$$

Where,

N = total number of data points

Y_i = actual value

Ŷ_i = predicted value

the lower the MAE, the less error in your model.

When DSet having outlier MAE is more beneficial

MAE the value should be near to zero. Then model perform well.

MAE more beneficial to outlier.

For outlier MAE is more preferable than MSE.

Mean Squared Error (MSE)

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

Where,

n = total number of data points

Y_i = actual value

\hat{Y}_i = predicted value

Thus, as with MAE, the lower the MSE, the less error in the model.

Root Mean Squared Error (RMSE)

$$\text{RMSE} = \sqrt{\sum_{i=1}^n \frac{(\hat{y}_i - y_i)^2}{n}}$$

Where,

n = total number of data points

Y_i = actual value

\hat{Y}_i = predicted value

lower RMSE → lower error.

R-Squared (R^2)

The R^2 metric gives an indication of how well a model fits your data, but is unable to explain if your model is good or not.

$$R^2 = 1 - \frac{\sum (y_i - \hat{y}_i)^2}{\sum (y_i - \bar{y}_i)^2}$$

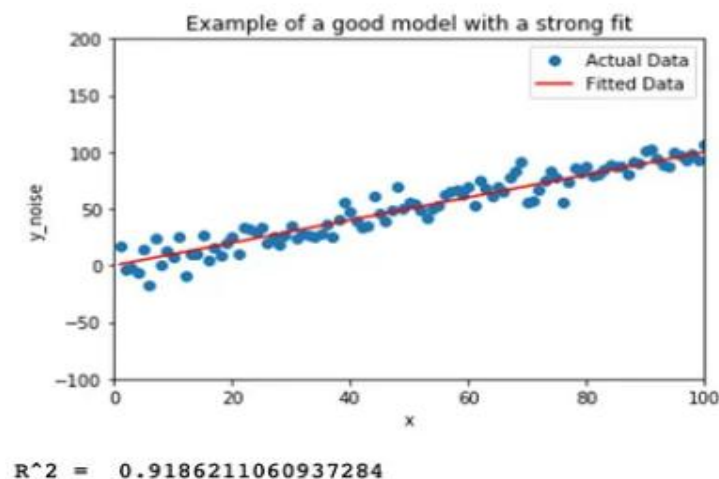
y = dependent variable values, \hat{y} = predicted values from model, \bar{y} = the mean of y

The R^2 value ranges from 0 to 1, with higher values denoting a strong fit, and lower values denoting a weak fit. Typically, it's agreed that:

$R^2 < 0.5 \rightarrow$ Weak fit

$0.5 \leq R^2 \leq 0.8 \rightarrow$ Moderate fit

$R^2 > 0.8 \rightarrow$ Strong fit



The line should maximize the number of points and the distance between the line and data point should be minimum.

in sklearn all is available apart from R^2

When to use regression?

If target variable is a continuous numeric variable (100–2000), then use a regression algorithm.

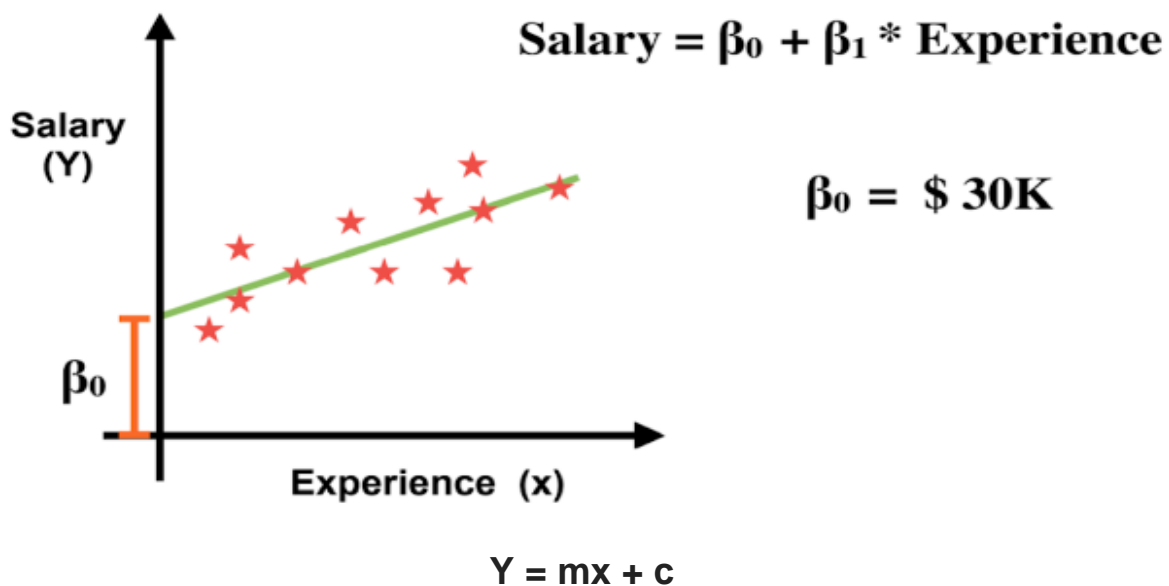
Types of Regression Algorithms:

- Linear regression
- Multiple linear regression
- Polynomial regression
- Ridge regression
- Lasso regression
- ElasticNet regression

Linear Regression

Linear Regression is a statistical model used to predict the relationship between independent and dependent variables denoted by x and y respectively

Simple Linear Regression is where only one independent variable is present and the model has to find the linear relationship of it with the dependent variable



Multiple Linear Regression:

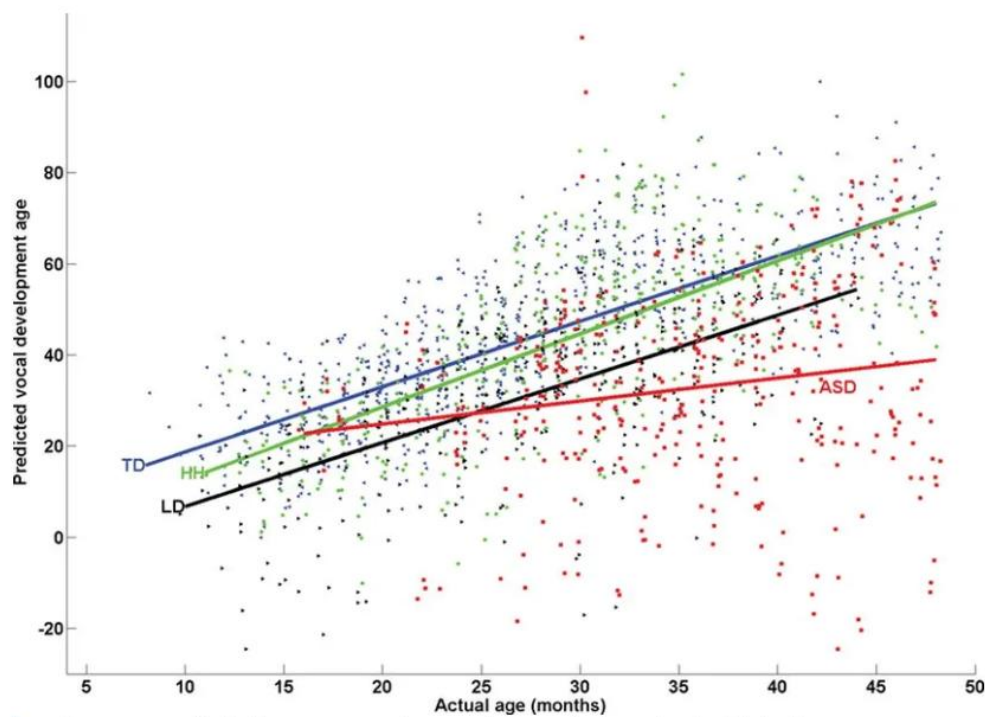
Multiple Linear Regression is one of the important regression algorithms which models the linear relationship between a single dependent continuous variable and more than one independent variable.

Equation for MLR

$$Y = m_1 * x_1 + m_2 * x_2 + m_3 * x_3 + \dots + m_n * x_n + c$$

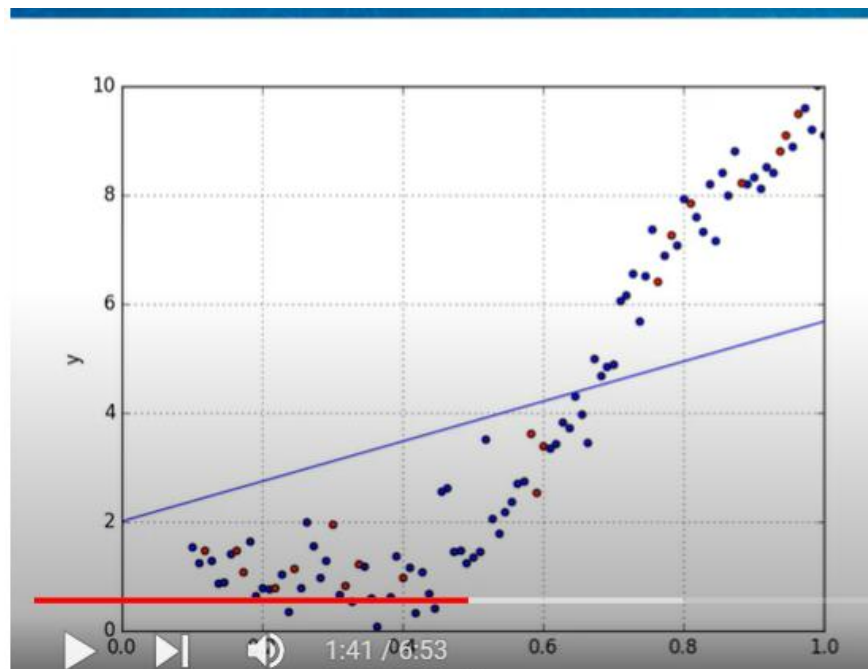
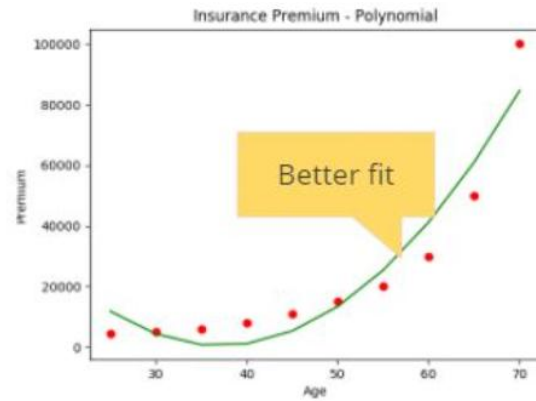
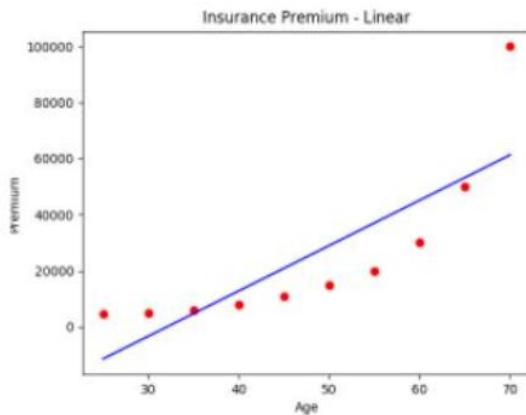
Diagram illustrating the components of the Multiple Linear Regression equation:

- Y : Dependent Variable
- $m_1, m_2, m_3, \dots, m_n$: Slopes
- c : Coefficient



Polynomial Regression:

It is a form of regression analysis in which the relationship between the independent variables and dependent variables are modeled in the **nth degree polynomial**.



Simple
Linear
Regression

$$y = b_0 + b_1x_1$$

Multiple
Linear
Regression

$$y = b_0 + b_1x_1 + b_2x_2 + \dots + b_nx_n$$

Polynomial
Linear
Regression

$$y = b_0 + b_1x_1 + b_2x_1^2 + \dots + b_nx_1^n$$

Polynomials	Form	Degree	Examples
Linear Polynomial	$p(x): ax+b, a \neq 0$	Polynomial with Degree 1	$x + 8$
Quadratic Polynomial	$p(x): ax^2+b+c, a \neq 0$	Polynomial with Degree 2	$3x^2-4x+7$
Cubic Polynomial	$p(x): ax^3+bx^2+cx, a \neq 0$	Polynomial with Degree 3	$2x^3+3x^2+4x+6$

It does not require the relationship between the independent and dependent variables to be linear in the data set.