

Part C:

Given Information:

Assumption:

Buses arrival of rate is 2 per hour

In 60 minutes 2 buses will arrive

In 30 minutes rate of bus arrival is 1
from 6:00 AM to 7:30 AM total of 90 min

$$P(X=2) = \frac{e^{-\lambda} \lambda^k}{k!}$$

formula

$$P(X=2) = \frac{\lambda^k e^{-\lambda}}{k!} \quad (k=2)$$

$$e = 2.71828$$

$$\lambda = \frac{30}{2} = 15$$

$$\lambda = \frac{30}{60} = \frac{1}{2}$$

$$\lambda = 2$$

$$P(X=30) = \frac{2^{30} e^{-2}}{30!}$$

$$= \frac{145315329}{30!}$$

$$= 5.147 e^{-25}$$

$$\left| \frac{30}{2} = 15 \right|$$

2) Let x_i be the number of sandwiches that the

$$Y = x_1 + x_2 + \dots + x_{64}$$

goal is to find y .

$$P(Y \leq y) \geq 0.95$$

$$E x_i = \frac{1}{4}(0) + \frac{1}{2}(1) + \frac{1}{4}(2)$$

$$= 1$$

$$E x_i^2 = \frac{1}{4}(0)^2 + \frac{1}{2}(1)^2 + \frac{1}{4}(2)^2$$

$$= \frac{3}{2}$$

$$\text{Var}(x_i) = E x_i^2 - (E x_i)^2$$

$$= \frac{3}{2} - 1$$

$$= \frac{1}{2} \rightarrow$$

$$SD = \frac{1}{\sqrt{2}}$$

$$E Y = 64 \times 1$$

$$= 64$$

$$\text{Var}(Y) = 64 \times \frac{1}{2}$$

$$= 32$$

$$\sigma_Y = 4\sqrt{2}$$

we can use CLT to find y

$$P(Y \leq y) = P\left(\frac{Y - 64}{4\sqrt{2}} \leq \frac{y - 64}{4\sqrt{2}}\right)$$

$$= \Phi\left(\frac{y - 64}{4\sqrt{2}}\right)$$

$$= \Phi\left(\frac{y - 64}{4\sqrt{2}}\right) = 0.95 \quad \text{so} \quad \frac{y - 64}{4\sqrt{2}} = \Phi^{-1}(0.95)$$

$$= 1.6449$$

$$y = 73.5$$

we make 74 sandwiches, we are 95% sure that there is no shortage.