

$$3.4. \quad 59. \quad f(x) = 2 \sin x + \sin^2 x$$

$$f'(x) = 2 \cos x + 2 \sin x \cos x$$

$$f'(x) = 0$$

$$-2 \cos x = 2 \sin x \cos x$$

$$-1 = \sin x$$

$$x = -\frac{\pi}{2} + 2k\pi, \quad k \in \mathbb{Z}$$

3.4. 76.

$$y = e^{rx}$$

$$y' = r e^{rx}$$

$$y'' = r^2 e^{rx}$$

$$r^2 e^{rx} - 4r e^{rx} + e^{rx} = 0$$

$$r^2 - 4r + 1 = 0$$

$$r = \frac{4 \pm \sqrt{16-4}}{2} = 2 \pm \frac{1}{2} \sqrt{4 \cdot 3} = 2 \pm \sqrt{3}$$

3.5: 20.  $\tan(x-y) = \frac{y}{1+x^2}$

$$\begin{aligned}\frac{d}{dx} \tan(x-y) &= \frac{d}{dx} \frac{y}{1+x^2} \\ \sec^2(x-y)(1-y') &= \frac{d}{dx} y(1+x^2)^{-1} \\ &= y'(1+x^2)^{-1} + y(-1)(1+x^2)^{-2}(2x) =\end{aligned}$$

$$\sec^2(x-y) - y' \sec^2(x-y)$$

$$\sec^2(x-y) + y(1+x^2)^{-2}(2x) = y'((1+x^2)^{-1} + \sec^2(x-y))$$

$$y' = \frac{\sec^2(x-y) + y(1+x^2)^{-2}(2x)}{\sec^2(x-y) + (1+x^2)^{-1}}$$

3.5: 50.  $y = \tan^{-1}(x^2)$

$$y' = \frac{2x}{1+x^4}$$

3.6: 28.  $f(x) = \sqrt{2+\ln x}$ ,  $x > 0$  and  $2+\ln(x) \geq 0$

$$f'(x) = \frac{1}{2}(2+\ln x)^{-\frac{1}{2}} \left(\frac{1}{x}\right) \quad \ln(x) \geq -2$$

$$= \frac{1}{2} \left( \frac{1}{\sqrt{2+\ln x}} \right) \left( \frac{1}{x} \right) \quad x \geq e^{-2}$$

$$= \left( 2x\sqrt{2+\ln x} \right)^{-1}$$

3.6: 30.  $f(x) = \ln \ln \ln x$   $f'(x) = \frac{1}{\ln \ln x} \frac{1}{\ln x} \frac{1}{x}$

~~for~~  $x > 0$ ,  $\ln x > 0$ ,  $\ln \ln x > 0$ .

$x > 1$ ,  $\ln \ln x > 0$

$e^{\ln \ln x} > e^0$

$\ln x > e^0$

$x > e^e$