Chapter 1: Measurement and Misc. Formula

Circumference of a circle: $C = 2\pi r$

 $\rho = \frac{m}{V}$ Density:

 $(ax^2 + bx + c = 0)$ Quadratic formula:

 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

 $\omega = \frac{v}{r}$ Angular velocity, ω :

Chapter 2: Motion along a straight line

displacement: $\Delta x = x_2 - x_1$

 $v_{ave} = \frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1}$ Average velocity:

 $s_{ave} = \frac{\text{total distance}}{\Delta t}$ Average speed:

 $v = \lim_{\Delta t \to 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$ Instantaneous velocity:

 $a_{ave} = \frac{\Delta v}{\Delta t} = \frac{v_2 - v_1}{t_2 - t_1}$ Average Acceleration:

 $a = \frac{dv}{dt} = \frac{d^2x}{dt^2}$ Instantaneous acceleration:

For Constant Acceleration

 $a = a_{ave} = \frac{v - v_0}{t - 0}$ constant acceleration:

 $v(t) = v_0 + at$ velocity (with a and t):

 $x(t) = \frac{1}{2}at^2 + v_0t + x_0$ position (with a and t):

 $v^2 = v_0^2 + 2a(x - x_0)$ velocity (with a and x):

 $x(t) = \frac{1}{2}(v_0 + v)t + x_0$ position (with v and t):

 $v_{ave} = \frac{1}{2}(v_0 + v)$ average velocity:

 $v_{ave} = v_0 + \frac{1}{2}at^2$ average velocity:

free fall acceleration: $a_{freefall} = -g$

Constants

Gravitational Acceleration: $g = 9.8 \frac{m}{s^2}$

 $1 \text{ u} = 1.66 \times 10^{-27} \text{kg}$ Atomic Mass Units:

Chapter 3: Vectors

 $\vec{s} = \vec{a} + \vec{b}$ Vector equation:

 $\vec{a} + \vec{b} = \vec{b} + \vec{a}$ Vector commutative law:

 $(\vec{a} + \vec{b}) + \vec{c} = \vec{a} + (\vec{b} + \vec{c})$ Vector associative law:

 $\vec{d} = \vec{a} - \vec{b} = \vec{a} + (-\vec{b})$ Vector subtraction:

 $\vec{a} = a_r \hat{i} + a_u \hat{j}$ Vector components:

 $a_x = a \cos \theta$ and $a_y = a \sin \theta$

 $a = \sqrt{a_x^2 + a_y^2}$ and $\tan \theta = \frac{a_y}{a}$

 $\vec{r} = \vec{a} + \vec{b}$ Vector addition:

 $\vec{r} = r_x \hat{i} + r_y \hat{j} + r_z \hat{k}$

 $r_x = a_x + b_x$

 $r_y = a_y + b_y$

 $r_z = a_z + b_z$

 $2\vec{a} = 2a_x\hat{i} + 2a_y\hat{j} + 2a_z\hat{k}$ vector by scalar multip.:

 $\vec{a} \cdot \vec{b} = ab \cos \phi$ Scalar Product:

 $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z$

 $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{a}$

 $\vec{c} = \vec{a} \times \vec{b}$ Vector Product:

 $|c| = ab \sin \phi$

direction from Right-hand rule

 $\vec{c} = (a_y b_z - a_z b_y)\hat{i} + (a_z b_x - a_x b_z)\hat{j}$

 $+(a_xb_y-a_yb_x)\hat{k}$

 $\vec{a} \times \vec{b} = -(\vec{b} \times \vec{a})$

Geometry

Volume: Surface Area:

square: $l \times w$

Cube: $l \times w \times h$

circle:

 πr^2

Sphere: $\frac{4}{3}\pi r^3$

sphere:

 $4\pi r^2$

Cylinder: $\pi r^2 h$

cylinder:

 $2\pi r^2 + 2\pi rh$

Chapter 4: Motion in two and three dimensions

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Position:	$\vec{r} =$	xi +	yj +	zk

Displacement:
$$\Delta \vec{r} = \vec{r}_2 - \vec{r}_1$$

$$\Delta \vec{r} = (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}$$

Average Velocity:
$$\vec{v}_{ave} = \frac{\Delta \vec{r}}{\Delta t}$$
 Instantaneous Velocity:
$$\vec{v} = \frac{d\vec{r}}{dt}$$

Instantaneous Velocity:
$$\vec{v} = \frac{d\vec{r}}{dt}$$

$$\vec{v} = v_x \hat{i} + v_y \hat{j} + v_z \hat{k}$$

$$v_x = \frac{dx}{dt}, v_y = \frac{dy}{dt}, v_z = \frac{dz}{dt}$$

Average acceleration:
$$\vec{a}_{ave} = \frac{\vec{v}_2 - \vec{v}_1}{\Delta t} = \frac{\Delta \vec{v}}{\Delta t}$$

Instantaneous acceleration:
$$\vec{r} = \frac{d\vec{\iota}}{dt}$$

$$\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$$

$$a_x = \frac{dv_x}{dt}, \ a_y = \frac{dv_y}{dt}, \ a_z = \frac{dv_z}{dt}$$

Projectile Motion

Initial velocity:
$$v_0 = v_{0x}\hat{i} + v_{0y}\hat{j}$$

$$v_{0x} = v_0 \cos \theta$$
 and $v_{0y} = v_0 \sin \theta$

Horizonatal Motion:
$$x(t) = v_{0x}t + x_0$$

Vertical Motion:
$$y(t) = -\frac{1}{2}gt^2 + v_{0y}t + y_0$$

$$v_y = v_{0y}t - gt$$

$$v_y^2 = v_{0y}^2 - 2g(y - y_0)$$

Equation of the path (trajectory):
$$y = (\tan \theta_0)x - \frac{gx^2}{2(v_0 \cos \theta_0)^2}$$

Horizontal Range:
$$R = \frac{v_0^2}{g} \sin 2\theta_0$$

Centripital acceleration:
$$a = \frac{v^2}{r}$$
 (Uniform Circular Motion)

Period of revolution:
$$T = \frac{2\pi r}{v}$$
 (Uniform Circular Motion)

Relative Motion: Labels are for a point P in reference frames A,B

1-dimension:
$$x_{PA} = x_{PB} + x_{BA}$$

$$v_{PA} = v_{PB} + v_{BA}$$

$$a_{PA} = a_{PB}$$

2-dimensions:
$$\vec{r}_{PA} = \vec{r}_{PB} + \vec{r}_{BA}$$

$$\vec{v}_{PA} = \vec{v}_{PB} + \vec{v}_{BA}$$

$$\vec{a}_{PA} = \vec{a}_{PB}$$

Units

Length:
$$1 \text{ m} = 3.28 \text{ ft}$$

$$1 \text{ mi} = 1.61 \text{ km}$$

$$1 \text{ ft} = 12 \text{ in}$$

Time:
$$1 \min = 60 \text{ s}$$

$$60 \min = 1 \text{ hr}$$

$$24 \text{ hr} = 1 \text{ day}$$

$$365 \text{ days} = 1 \text{ year}$$

Speed:
$$1 \text{ m/s} = 3.28 \text{ ft/s}$$

$$1 \text{ km/hr} = 0.621 \text{ mi/hr}$$

SI Prefixes				
Exponent	Prefix	SI Symbol		
10^{-18}	atto	a		
10^{-15}	femto	f		
10^{-12}	pico	p		
10^{-9}	nano	n		
10^{-6}	micro	μ		
10^{-3}	milli	m		
10^{-2}	cento	c		
10^{-1}	deci	d		
10^{1}	deca	da		
10^{2}	hecto	h		
10^{3}	kilo	k		
10^{6}	mega	M		
10^{9}	giga	G		
10^{12}	tera	Т		

Chapter 5: Force and Motion-I

Newton's 1st law: if $\vec{F}_{net} = 0$, then $\vec{a} = 0$

Newton's 2nd law: $\vec{F}_{net} = m\vec{a}$

 $F_{net,x} = ma_x$

 $F_{net,y} = ma_y$

 $F_{net,z} = ma_z$

Superposition of Forces: (Net force) $\vec{F}_{net} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$

Gravitational Force: $F_g = mg$

Weight: W = mg

Newton's 3rd law: (for two objects, B & C) $\vec{F}_{BC} = -\vec{F}_{CB}$

Chapter 6: Force and Motion-II $\,$

Static Friction: $f_{s,max} = \mu_s F_N$

Kinetic Friction: $f_k = \mu_k F_N$

Drag Force: $D = \frac{1}{2} C \rho A v^2$

Terminal speed: $v_t = \sqrt{\frac{2F_g}{C\rho A}}$

Centripetal acceleration: $a = \frac{v_2}{R}$

Centripetal Force: $F = m \frac{v_2}{R}$