

From #3

$$X \sim N(\mu, \sigma) \quad \sigma = 50 \quad Z = \frac{X - \mu}{\sigma}$$

1.  $X \sim N(104, 5^2)$   
 $\sigma = 5$

a)  $P(X=105) \Rightarrow P\left(\frac{X-\mu}{\sigma} = \frac{105-104}{5}\right) \Rightarrow P(Z=0.2)$

b) Probability at a fixed point is 0!  
So,

$$P(X=105) = 0$$

b)  $P(X < 105) \Rightarrow P\left(Z < \frac{105-104}{5}\right) \Rightarrow P(Z < 0.2)$

$P(Z < 0.2) = 0.5793$  \* from z-table

$$P(X < 105) = 0.5793$$

c)  $P(X \leq 105)$

$P(X \leq 105)$  is the same as  $P(X < 105)$  in a normal distribution, so...

$$P(X \leq 105) = 0.5793$$

2.  $X \sim N(0.3, 0.06^2)$   
 $\sigma = 0.06$

a)  $P(X > 0.25) \Rightarrow P\left(Z > \frac{0.25-0.3}{0.06}\right) \Rightarrow P(Z > -0.83)$

$P(Z > -0.83) =$  \* from z-table  
 $Z = -0.83 \Rightarrow 0.2033$

$1 - 0.2033 = 0.7967$

So,

$$P(X > 0.25) = 0.7967$$

(cont'd)

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12-6-22  
Stat 15aCont'db) How would you characterize largest 5% of all  $X$  values?

Above 95th percentile, so

$$z = \frac{x - \mu}{\sigma} \rightarrow 1.645 = \frac{x - 0.3}{0.06}$$

\* from z-table

$$0.06 \cdot 1.645 = \frac{x - 0.3}{0.06} \cdot 0.06 = 0.0987 = \frac{x - 0.3}{0.06}$$

$$x = 0.3987$$

The largest 5% of all  $X$  are above 0.3987

3.  $X \sim N(15, 1.25^2)$   
 $\sigma = 1.25$

$$\begin{aligned} P(|X - 15| \leq 3) &= P(-3 \leq X - 15 \leq 3) \\ &= P(-3 + 15 \leq X \leq 3 + 15) \\ &= P(12 \leq X \leq 18) \\ &= P\left(\frac{12 - 15}{1.25} \leq \frac{X - \mu}{\sigma} \leq \frac{18 - 15}{1.25}\right) \\ &= P(-2.4 \leq Z \leq 2.4) \\ &= P(Z \leq 2.4) - P(Z \leq -2.4) \\ &= 0.9918 - 0.0082 \\ &= 0.9836 \end{aligned}$$

$$P(|X - 15| \leq 3) = 0.9836$$

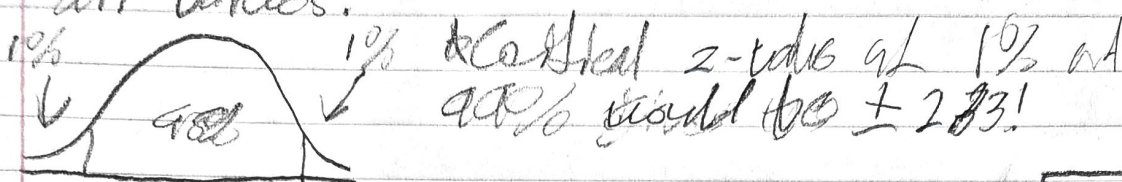


## Exam #3

4.  $X \sim N(6.8, 2.8^2)$

$\sigma = 2.8$

What  $c$  such that interval includes 98% of all values?



$$c = z * \sigma = 2.33 * 2.8 = \boxed{6.524}$$

5. a)  $P(Z < -1.5)$

Area under  $-1.5$  is 0.0668, so what gives us left value?

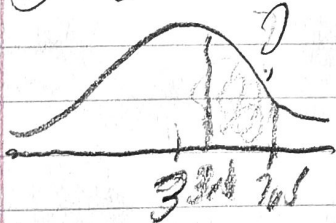
$$\rightarrow \boxed{\text{pnorm}(-1.5)}$$

b)  $P(Z > -1.5)$

$1 - 0.0668 = 0.9332$  ← what gives us right value?

$$\boxed{1 - \text{pnorm}(-1.5)}$$

c)  $P(3.1 < X < 3.3)$ ,  $X \sim N(3, 2)$ ,  $\sigma = 2$



$$\boxed{\text{pnorm}(3.3, 3, 2) - \text{pnorm}(3.1, 3, 2)}$$