CHAPTER 3 HW

- 7. For each random variable defined here, describe the set of possible values for the variable, and state whether the variable is discrete.
 - a. X=the number of unbroken eggs in a randomly chosen standard egg carton
 - b. Y= the number of students on a class list for a particular course who are absent on the first day of classes
 - c. U=the number of times a duffer has to swing at a golf ball before hitting it
 - d. X=the length of a randomly selected rattlesnake
 - e. Z= the sales tax percentage for a randomly selected amazon.com purchase.
 - f. Y= the pH of a randomly chosen soil sample
 - g. X= the tension (psi) at which a randomly selected tennis racket has been strung
 - h. X=the total number of times three tennis players must spin their rackets to obtain something other than UUU or DDD (to determine which two play next)
- 13. A mail-order computer business has six telephone lines. Let X denote the number of lines in use at a specified time. Suppose the pmf of X is as given in the accompanying table.

X	0	1	2	3	4	5	6
p(x)	0.10	0.15	0.20	0.25	0.20	0.06	0.04

Calculate the probability of each of the following events.

- a. {at most three lines are in use}
- b. {fewer than three lines are in use}
- c. {at least three lines are in use}
- d. {between two and five lines, inclusive, are in use}
- e. {between two and four lines, inclusive, are not in use}
- f. {at least four lines are not in use}
- 23. A branch of a certain bank in New York City has six ATMs. Let X represent the number of machines in use at a particular time of day. The cdf of X is as follows:

$$F(x) = \begin{cases} 0 & x < 0 \\ 0.06 & 0 \le x < 1 \\ 0.19 & 1 \le x < 2 \\ 0.39 & 2 \le x < 3 \\ 0.67 & 3 \le x < 4 \\ 0.92 & 4 \le x < 5 \\ 0.97 & 5 \le x < 6 \\ 1 & 6 \le x \end{cases}$$

Calculate the following probabilities directly from the cdf:

- a. P(2), that is, P(x=2)
- b. P(X>3)
- c. $P(2 \le X \le 5)$
- d. P(2 < X < 5)
- **24**. An insurance company offers its policyholders a number of different premium payment options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows:

$$F(x) = \begin{cases} 0 & x < 1 \\ 0.30 & 1 \le x < 3 \\ 0.40 & 3 \le x < 4 \\ 0.45 & 4 \le x < 6 \\ 0.60 & 6 \le x < 12 \\ 1 & 12 \le x \end{cases}$$

- a. What is the pmf of X?
- b. Using just the cdf, compute $P(3 \le X \le 6)$ and $P(4 \le X)$.
- 29. The pmf of the amount of memory X (GB) in a purchased flash drive was given in Example 3.13 as

X	1	2	4	8	16
p(x)	0.05	0.10	0.35	0.40	0.10

Compute the following:

- a. E(X)
- b. V(X) directly from the definition
- c. The standard deviation of X
- d. V(X) using the shortcut formula
- **32**. A certain brand of upright freezer is available in three different rated capacities: 16 ft², 18 ft², and 20 ft². Let X=the rated capacity of a freezer of this brand sold at a certain store. Suppose that X has pmf

X	16	18	20	
p(x)	.2	.5	.3	

- a. Compute E(X), $E(X^2)$, and V(X)
- b. If the price of a freezer having capacity X is 70X-650, what is the expected price paid by the next customer to buy a freezer?
- c. What is the variance of the price paid by the next customer?
- d. Suppose that although the rated capacity of a freezer is X, the actual capacity is $h(X) = X-0.008X^2$. What is the expected actual capacity of the freezer purchased by the next customer?
- **39**. A chemical supply company currently has in stock 100 lb of a certain chemical, which it sells to customers in 5-lb batches. Let X= the number of batches ordered by a randomly chosen customer, and suppose that X has pmf

X	1	2	3	4
p(x)	0.2	0.4	0.3	0.1

Compute E(X) and V(X). Then compute the expected number of pounds left after the next customer's order is shipped and the variance of the number of pounds left. [Hint: The number of pounds left is a linear function of X.]

- **47**. The article "Should You Report That Fender-Bender?" (Consumer Reports, Sept.2013:15) reported that 7 in 10 auto accidents involve a single vehicle (the article recommended always reporting to the insurance company an accident involving multiple vehicles). Suppose 15 accidents are randomly selected. Answer the each of the following questions.
 - a. What is the probability that at most 4 involve a single vehicle?
 - b. What is the probability that exactly 4 involve a single vehicle?
 - c. What is the probability that exactly 6 involve multiple vehicles?
 - d. What is the probability that between 2 and 4, including, involve a single vehicle?
 - e. What is the probability that at least 2 involve a single vehicle?
 - f. What is the probability that exactly 4 involve a single vehicle and the other 11 involve multiple vehicles?
- **49**. A company that produces fine crystal knows from experience that 10% of its goblets have cosmetic flaws and must be classified as "seconds."
 - a. Among six randomly selected goblets, how likely is it that only one is a second?
 - b. Among six randomly selected goblets, what is the probability that at least two are seconds?
 - c. If goblets are examined one by one, what is the probability that at most five must be selected to find four that are not seconds?

- **55.** Twenty percent of all telephones of a certain type are submitted for service while under warranty. Of these, 60% can be repaired, whereas the other 40% must be replaced with new units. If a company purchases ten of these telephones, what is the probability that exactly two will end up being replaced under warranty?
- **69.** Each of 12 refrigerators of a certain type has been returned to a distributor because of an audible, high-pitched, oscillating noise when the refrigerators are running. Suppose that 7 of these refrigerators have a defective compressor and the other 5 have less serious problems. If the refrigerators are examined in random order, let X be the number among the first 6 examined that have a defective compressor.
 - a. Calculate P(X=4) and $P(X \le 4)$
 - b. Determine the probability that X exceeds its mean value by more than 1 standard deviation.
 - c. Consider a large shipment of 400 refrigerators, of which 40 have defective compressors. If X is the number among 15 randomly selected refrigerators that have defective compressors, describe a less tedious way to calculate (at least approximately) $P(X \le 5)$ than to use the hypergeometric pmf.
- **71**. A geologist has collected 10 specimens of basaltic rock and 10 specimens of granite. The geologist instructs a laboratory assistant to randomly select 15 of the specimens for analysis.
 - a. What is the pmf of the number of granite specimens selected for analysis?
 - b. What is the probability that all specimens of one of the two types of rock are selected for analysis?
 - c. What is the probability that the number of granite specimens selected for analysis is within 1 standard deviation of its mean value?

d.

- 81. Suppose that the number of drivers who travel between a particular origin and destination during a designated time period has a Poisson distribution with parameter $\mu = 20$ (as suggested in the article "Dynamic Ride Sharing: Theory and Practice," J. of Transp. Engr., 1997: 308–312). What is the probability that the number of drivers will
 - a. Be at most 10?
 - b. Exceed 20?
 - c. Be between 10 and 20, inclusive? Be strictly between 10
 - a. and 20?
 - d. Be within 2 standard deviations of the mean value?
- **83**. An article in the Los Angeles Times (Dec. 3, 1993) reports that 1 in 200 people carry the defective gene that causes inherited colon cancer. In a sample of 1000 individuals, what is the approximate distribution of the number who carry this gene? Use this distribution to calculate the approximate probability that
 - a. Between 5 and 8 (inclusive) carry the gene.
 - b. At least 8 carry the gene.
- 87. The number of requests for assistance received by a towing service is a Poisson process with rate α =4 per hour.
 - a. Compute the probability that exactly ten requests are received during a particular 2-hour period.
 - b. If the operators of the towing service take a 30-min break for lunch, what is the probability that they do not miss any calls for assistance?
 - c. How many calls would you expect during their break?