

AI1103 : Assignment 5

Santosh Dhaladhuli MS20BTECH11007

Download all python codes from

<https://github.com/Santosh-Dhaladhuli2003/AI1103/blob/main/Assignment%205/Assignment%205.py>

and latex codes from

<https://github.com/Santosh-Dhaladhuli2003/AI1103/blob/main/Assignment%205/Assignment%205.tex>

We Know $F_X(x) = \Pr(X \leq x)$

Required Probability is $\Pr(X > 5) = 1 - \Pr(X \leq 5)$

$$\Rightarrow \Pr(X > 5) = 1 - F_X(5)$$

$$= 1 - (1 - e^{-\frac{5}{5}})$$

$$= e^{-\frac{5}{5}}$$

$$= e^{-1} = \frac{1}{e}$$

\therefore The correct answer is **Option 1**

1 GATE IN 2007 QUESTION No. 27

Assume that the duration in minutes of a telephone conversation follows the exponential distribution $f(x) = \frac{1}{5}e^{-\frac{x}{5}}$, $x \geq 0$. The probability that the conversation will exceed five minutes is...

- 1) $\frac{1}{e}$
- 2) $1 - \frac{1}{e}$
- 3) $\frac{1}{e^2}$
- 4) $1 - \frac{1}{e^2}$

2 SOLUTION

Let X be a Random variable defined, that denotes the duration of a telephonic conversation in minutes.

So, $X \in [0, \infty)$

Given, $f_X(x) = \frac{1}{5}e^{-\frac{x}{5}}$

Let CDF of X be $F_X(x)$

$$\begin{aligned} F_X(x) &= \int_{-\infty}^x f_X(t) dt \\ &= \int_{-\infty}^0 f_X(t) dt + \int_0^x f_X(t) dt \end{aligned}$$

$$F_X(x) = \int_0^x f_X(t) dt \because f_X(x) = 0 \forall x < 0$$

$$\therefore F_X(x) = \int_0^x \frac{1}{5}e^{-\frac{t}{5}} dt$$

$$\Rightarrow F_X(x) = 1 - e^{-\frac{x}{5}} \quad (1)$$

