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AI1103: Assignment 1

Santosh Dhaladhuli - MS20BTECH11007

Download all python codes from

https://github.com/Santosh-Dhaladhuli2003/ AI1103-Assignment-1/blob/main/ assigment_1.py

and latex codes from

https://github.com/Santosh-Dhaladhuli2003/ AI1103-Assignment-1/blob/main/Assignment %201.tex

PROBLEM 5.12

Random Variable X has the following Probability Distribution

	X	0	1	2	3	4	5	6	7
Ì	P(X)	0	k	2k	2k	3k	k^2	$2k^2$	$7k^2 + k$

Determine:

- 1) k
- 2) P(X < 3)
- 3) P(X > 6)
- 4) P(0 < X < 3)

Solution

(i) It is known that the sum of probabilities of a probability distribution is always one.

$$\therefore 0 + k + 2k + 3k + k^2 + 2k^2 + (7k^2 + k) = 1$$
(5.12.1)

$$\implies 10k^2 + 9k - 1 = 0 \implies (10k - 1)(k + 1) = 0$$
(5.12.2)

$$\implies k = -1, \frac{1}{10}$$
 (5.12.3)

$$\therefore k = \frac{1}{10} (\because k \ge 0) \tag{1}$$

(ii)

$$P(X < 3) = P(X = 2) + P(X = 1) + P(X = 0)$$

$$(5.12.4)$$

$$\implies P(X < 3) = 0 + k + 2k = 3k$$

$$P(X < 3) = \frac{3}{10}$$
 (2)

(iii)

$$P(X > 6) = P(X = 7) = 7k^2 + k$$
 (5.12.6)

$$\implies P(X > 6) = \frac{7}{100} + \frac{1}{10}$$
 (5.12.7)

$$\therefore P(X > 6) = \frac{17}{100} \tag{3}$$

$$P(0 < X < 3) = P(X = 1) + P(X = 2)$$
 (5.12.8)

$$\implies P(0 < X < 3) = k + 2k = 3k \quad (5.12.9)$$

$$\therefore P(0 < X < 3) = \frac{3}{10} \tag{4}$$