

Probability

1. Experiment:

An operation which can produce some well-defined outcomes is called an experiment.

2. Random Experiment:

An experiment in which all possible outcomes are known and the exact output cannot be predicted in advance, is called a random experiment.

Examples:

- i. Rolling an unbiased dice.
- ii. Tossing a fair coin.
- iii. Drawing a card from a pack of well-shuffled cards.
- iv. Picking up a ball of certain colour from a bag containing balls of different colours.

Details:

- v. When we throw a coin, then either a Head (H) or a Tail (T) appears.
- vi. A dice is a solid cube, having 6 faces, marked 1, 2, 3, 4, 5, 6 respectively. When we throw a die, the outcome is the number that appears on its upper face.
- vii. A pack of cards has 52 cards.
It has 13 cards of each suit, name **Spades, Clubs, Hearts and Diamonds**.
Cards of spades and clubs are **black cards**.
Cards of hearts and diamonds are **red cards**.
There are 4 honours of each unit.
There are Kings, Queens and Jacks. These are all called face cards.

3. Sample Space:

When we perform an experiment, then the set S of all possible outcomes is called the **sample space**.

Examples:

1. In tossing a coin, $S = \{H, T\}$
2. If two coins are tossed, the $S = \{HH, HT, TH, TT\}$.
3. In rolling a dice, we have, $S = \{1, 2, 3, 4, 5, 6\}$.

Event:

Any subset of a sample space is called an **event**.

Probability of Occurrence of an Event:

Let S be the sample and let E be an event.

Then, $E \subseteq S$.

$$\therefore P(E) = \frac{n(E)}{n(S)}.$$

Results on Probability:

- . $P(S) = 1$
- i. $0 \leq P(E) \leq 1$
- ii. $P(\Phi) = 0$
- iii. For any events A and B we have : $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
- iv. If A denotes (not-A), then $P(A) = 1 - P(A)$.

1. A bag contains 2 yellow, 3 green and 2 blue balls. Two balls are drawn at random. What is the probability that none of the balls drawn is blue?

- A. 1/2 B. 10/21 C. 9/11 D. 7/11

2. A die is rolled twice. What is the probability of getting a sum equal to 9?

- A. 2/3 B. 2/9 C. 1/3 D. 1/9

3. Three coins are tossed. What is the probability of getting at most two tails?

- A. 7/8 B. 1/8 C. 1/2 D. 1/7

4. When tossing two coins once, what is the probability of heads on both the coins?
A. $1/4$ B. $1/2$ C. $3/4$ D. None of these
5. What is the probability of getting a number less than 4 when a die is rolled?
A. $1/2$ B. $1/6$ C. $1/3$ D. $1/4$
6. A bag contains 4 black, 5 yellow and 6 green balls. Three balls are drawn at random from the bag. What is the probability that all of them are yellow?
A. $2/91$ B. $1/81$ C. $1/8$ D. $2/81$
7. One card is randomly drawn from a pack of 52 cards. What is the probability that the card drawn is a face card(Jack, Queen or King)
A. $1/13$ B. $2/13$ C. $3/13$ D. $4/13$
8. A dice is thrown. What is the probability that the number shown in the dice is divisible by 3?
A. $1/6$ B. $1/3$ C. $1/4$ D. $1/2$
9. John draws a card from a pack of cards. What is the probability that the card drawn is a card of black suit?
A. $1/2$ B. $1/4$ C. $1/3$ D. $1/13$
10. There are 15 boys and 10 girls in a class. If three students are selected at random, what is the probability that 1 girl and 2 boys are selected?
A. $1/40$ B. $1/2$ C. $21/46$ D. $7/42$
11. What is the probability of selecting a prime number from 1,2,3,... 10 ?
A. $2/5$ B. $1/5$ C. $3/5$ D. $1/7$
12. 3 balls are drawn randomly from a bag contains 3 black, 5 red and 4 blue balls. What is the probability that the balls drawn contain balls of different colors?
A. $3/11$ B. $1/3$ C. $1/2$ D. $2/11$
13. 5 coins are tossed together. What is the probability of getting exactly 2 heads?
A. $1/2$ B. $5/16$ C. $4/11$ D. $7/16$
14. What is the probability of drawing a "Queen" from a deck of 52 cards?
A. $1/2$ B. $1/13$ C. $1/6$ D. $1/3$
15. A card is randomly drawn from a deck of 52 cards. What is the probability getting an Ace or King or Queen?
A. $3/13$ B. $2/13$ C. $1/13$ D. $1/2$
16. When two dice are rolled, what is the probability that the sum is either 7 or 11?
A. $1/4$ B. $2/5$ C. $1/9$ D. $2/9$
17. A card is randomly drawn from a deck of 52 cards. What is the probability getting either a King or a Diamond?
A. $4/13$ B. $2/13$ C. $1/3$ D. $1/2$
18. John and Dani go for an interview for two vacancies. The probability for the selection of John is $1/3$ and whereas the probability for the selection of Dani is $1/5$. What is the probability that none of them are selected?
A. $3/5$ B. $7/12$ C. $8/15$ D. $1/5$